Dynamic Fair Electronic Cash Model without Trustees

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Abstract. A new fair electronic cash system is proposed based on group blind signature and secret sharing scheme. Our proposed system is dynamic: we propose a method to delete the dishonest banks that maybe attack the system, which was not mentioned in the previous literatures. Our proposed scheme does not need a trusted third party to trace users: a shop owning suspicious e-coin and the bank having issued the coin can collaborate to find the user using secret sharing scheme, however, any one of them can't trace the user alone. Furthermore, a novel e-coin tracing method is used to prevent criminal activities: under normal situation, the bank issues ordinary e-coin, while under abnormal situation such as blackmailing, kidnapping etc., the bank issues marked e-coin, and at the step of deposit, any bank in the group can recognize the marked e-coin. Also, our scheme is constructed for multiple banks as in the real life, thus it is more practical.

1 Introduction

With the popularization of internet, people are engaged in electronic commerce with high frequency. Secure and efficient electronic payment systems are significant for electronic commerce. As an important electronic payment system, electronic cash (E-cash or digital cash) develops rapidly. Chaum [1] proposed the first electronic cash system with unconditional anonymity by use of blind signature in 1982. However, this unconditional anonymity may be misused for criminal activities such as money laundering, blackmailing, kidnapping etc. [2]. From then, many fair electronic cash systems were proposed which need a trusted third party (TTP) to revoke the anonymity of the users when necessary. Figure 1 is the flow chart of a basic fair electronic cash model with multiple banks.

As a powerful tool, group signature has been widely used to design fair electronic cash system [5-9]. However, any bank in the group is supposed to be

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honest in the previous electronic cash systems based on group signature. But it is possible that there exist dishonest banks probably in the real life, so it is reasonable to consider that there maybe exist dishonest banks in an electronic cash system.

Figure 1 Fair Electronic Cash Model with Multiple Banks

In this paper we propose a member deletion method to CS97 group signature scheme [3] and according to it construct a dynamic fair electronic cash model with multiple banks: a bank can join the group, also, the group manager can delete a bank when he breaks the rules of the group. Our proposed scheme has the following properties: a user can spend his e-cash anonymously, any bank can't trace the user; there is only one public key in the group of the banks, and the length of the public key don't change with the increase of the number of the banks; given an e-cash, nobody but the Central Bank can know by which bank it is issued, which can provide anonymity for the banks; no banks including the Central Bank can issue e-cash on behalf of another bank; the previous e-cash issued by the deleted bank cannot be disclosed and it is impossible for the deleted bank to issue e-cash continuously. In particular, our scheme can realize user tracing without trustees and can prevent users from blackmailing, kidnapping etc... Figure 2 is the flow chart of our proposed model.

Figure 2 Fair Electronic Cash Model without Trustees

2 Dynamic group blind signature

2.1 Signature of knowledge of discrete logarithm

Besides the blind signature of knowledge of double discrete logarithm BSKLOGLOG[$\alpha \mid y = g^{\alpha}$](m) and the signature of knowledge of e-th root of discrete logarithm BSKROOTLOG[$\alpha \mid y = g^{\alpha^e}$](m) as in LR98 [5] group blind signature, we also need the following definition:

Definition An $(l+1)$ -tuple $(c, s_1, \dots, s_l) \in \{0,1\}^k \times Z_n^{*l}$ satisfying $c = H_l(m \parallel y_1 \parallel \dots \parallel y_l \parallel g_1 \parallel \dots \parallel g_l \parallel g_1^{s_1} y_1^{c^{[1]}} \parallel \dots \parallel g_1^{s_l} y_l^{c^{[l]}} \parallel \dots \parallel g_l^{s_1} y_1^{c^{[1]}} \parallel \dots \parallel g_l^{s_l} y_l^{c^{[l]}})$ is a signature of knowledge of a representation of the discrete logarithms of $y_1, \dots, y_l$ to the bases $g_1, \dots, g_l$ on a message m, with security parameter l , denoted: SKREPLOG[$\alpha : y_1 = g_1^{\alpha} \wedge \dots \wedge y_l = g_l^{\alpha}$](m).

We can obtain the blind one, denoted BSKREPLOG[$\alpha : y_1 = g_1^{\alpha} \wedge \dots \wedge y_l = g_l^{\alpha}$](m), as follows:

User Round 0: User wants message m signed and sends a sign request to the signer.

Signer Round 1: For $1 \leq i \leq l$, generate random $2^{\lambda} \leq r_i \leq 2^{\lambda+\mu}-1$, set $P_{ji} = g_j^{r_i}$ and send $\{P_{ji}\}$ to the user, $j=1, \dots, t$.

User Round 2: Obtain a random permutation $\sigma : \{1, \dots, l\} \rightarrow \{1, \dots, l\}$ and set $Q_{ji} = P_{j\sigma(i)}$, for $1 \leq i, j \leq l$, generate random $2^{\lambda+\mu} \leq a_i \leq 2^{\lambda+2\mu}-1$, and set $R_{ji} = Q_{ji} g_j^{a_i}$, calculate $c = H_l(m \parallel y_1 \parallel \dots \parallel y_l \parallel g_1 \parallel \dots \parallel g_l \parallel R_{11} \parallel \dots \parallel R_{1l} \parallel \dots \parallel R_{l1} \parallel \dots \parallel R_{ll})$, calculate c' such that $c'[i] = c[\sigma^{-1}(i)]$, send c' to the signer.

Signer Round 3: Compute, for $1 \leq i \leq l$, $t_i = r_i$, if $c'[i] = 0$; $t_i = r_i - x$, if $c'[i] = 1$, send $\{t_i\}$ to the user.

User Round 4: Verify that $P_{ji} = g_j^{r_i} y_j^{c^{[i]}}$, compute $s_i = t_{\sigma(i)} + a_i$, $1 \leq i \leq l$, output BSKREPLOG[$\alpha : y_1 = g_1^{\alpha} \wedge \dots \wedge y_l = g_l^{\alpha}$](m) : $(c, s_1, \dots, s_l)$.

2.2 Dynamic group blind signature

The main idea is: the group manager issues the membership keys of the deleted members on a bulletin board, every group member must prove with zero knowledge that his membership key is not on the bulletin board when he signs a message. Our scheme is based on LR98 [5] group blind signature. We mainly introduce the steps of **revoke** and **sign** because the steps of **setup**, **join** and **open** are the same as that in LR98 [5].

Setup The group manager constructs the group's public key $(n, e, G, g, a, \lambda, \mu)$.

Join A group member picks a secret key x , calculates $y = a^x \pmod n$ and the membership key $z = g^y$, obtains his membership certificate $v = (y+1)^{1/e} \pmod n$ from the group manager.

Revoke When a member is deleted, the group manager issues his membership key $z = g^y$ on a bulletin board.

Sign signer: Look up the bulletin board issued by the group manager, suppose that there are t deleted members: $z_1, z_2, \dots, z_t$. Obtain $q \in_R Z_n^*$ and set $\tilde{g} = g^q$, $\tilde{z} = \tilde{g}^y$, $P_i^{LOG} = \tilde{g}^{a^i}$, $P_i^{ROOT} = \tilde{g}^{v_i^e}$, $v_i = (z/z_1)^q, \dots, v_t = (z/z_t)^q$, send them to U.

U: Check $v_i \neq 1$, obtain $b \in_R \{0,1,\dots, 2^{\lambda}-1\}$, $f \in_R Z_n^*$, set $\omega = (af)^{eb} \pmod q$, $\hat{g} = \tilde{g}^{\omega}$, $\hat{z} = \tilde{z}^{\omega}$, $\hat{P}_i^{LOG} = (P_i^{LOG})^{\omega}$, $\hat{P}_i^{ROOT} = (P_i^{ROOT})^{\omega}$, $v_i' = v_i^{\omega}, \dots, v_t' = v_t^{\omega}$, $z_1' = z_1^{\omega}, \dots, z_t' = z_t^{\omega}$, take $\hat{P}_i^{ROOT}$ and $\hat{P}_i^{LOG}$ as input, execute BSKROOTLOG and BSKLOGLOG, and execute BSKREPLOG taking $\hat{z}/v_i'$, z_i' as y_i, g_i respectively,

then the signature is $(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3)$, where $V_1 = \text{SKLOGLOG}[x : \hat{z} = \hat{g}^{a^x}](m)$, $V_2 = \text{SKROOTLOG}[v : \hat{z} \hat{g} = \hat{g}^{v^q}](m)$, $V_3 = \text{BSKREPLOG}[q : \hat{z}/v_1' = z_1'^{q_1} \wedge \dots \wedge \hat{z}/v_t' = z_t'^{q_t}](m)$.

Open Given a signature $(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3)$, the group manager can determine the signer by testing if $\hat{g}^{y^r} = \hat{z}$ for every group member P.

Validity of the revocation: From V_3 , we obtain $\hat{z}/v_i' = z_i'^{q_i}$, that is, $\hat{z}^w/v_i^w = z_i'^{wq_i}$, so $v_i^w = \hat{z}^w/z_i'^{wq_i} = z_i'^{wq_i}/z_i'^{wq_i} = (z_i/z_i')^{wq_i}$, however, $v_i \neq 1$, thus $(z/z_i)^{wq_i} \neq 1$, this concludes $z \neq z_i$.

3. Dynamic electronic cash system without trustees

All banks form a group, the group manager is the Central Bank of the country.

Setup: The Central Bank chooses a security parameter l , and computes an RSA public key (n, e) , where the length of n is at least $2l$ bits; chooses a cyclic subgroup $G = \langle g \rangle$ of order n of Z_p^* ; selects $a \in Z_p^*$ where a has large multiplicative order modulo all the prime factors of n ; chooses an upper bound λ on the length of the secret keys and a constant $\mu > 1$. The group's public key is $(n, e, G, g, a, \lambda, \mu)$.

A bank can obtain his certificate from the Central Bank as follows: the bank picks a secret key $x \in_R \{0, 1, \dots, 2^\lambda - 1\}$, calculates $y = a^x \pmod{n}$ and the membership key $z = g^y$, sends (y, z) to the Central Bank, obtains his membership certificate $v = (y+1)^{1/e} \pmod{n}$ from the group manager.

The Central Bank need issue the deleted banks' membership keys $z_1, z_2, \dots, z_l$ on a bulletin board.

Withdrawal: A user U has an account in a bank B_i , U takes $u \in_R Z_p^*$ as his secret key, sends $I = g^u$ to B_i and takes I as his identity.

1 U chooses $1 \neq r \in_R Z_p^*$, $c_0 = I^r$, $c_1 = r$, $f(x) = c_0 + c_1 x \pmod{q}$, and chooses $x_1 \in_R Z_p^*$, computes $f(x_1)$, $C_0 = g^{c_0} \pmod{p}$, $C_1 = g^{c_1} \pmod{p}$. After authenticated by B_i , U sends a withdrawal request and $\langle x_1, f(x_1) \rangle, C_0, C_1$ to the bank and with a proof: $\text{SKREPLOG}[\gamma : I = g^r \wedge C_0 = g^{C_1^r}]$.

2 B_i checks the validity of $\text{SKREPLOG}[\gamma : I = g^r \wedge C_0 = g^{C_1^r}]$ and $C_0 C_1^{x_1} = g^{f(x_1)}$, then chooses $X \in_R Z_q^*$, computes $\alpha = g^X \pmod{p}$ and sends α to U .

3 (1) Under the normal situation, U calculates $\alpha' = \alpha^r$ and sends α' to B_i . B_i validates $\alpha' = C_1^{X^r}$, let $\beta = \alpha'$, then B_i signs U 's withdrawal message m with group blind signature as the step of **sign** in section 2.2, then the e-coin is $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, C_0, C_1, \alpha, \beta)$;

(2) Under the abnormal situation such as blackmailing, kidnapping etc., U selects $\delta \neq r$, sends $\alpha' = \alpha^\delta$ to B_i . B_i validates $\alpha' \neq C_1^{X^r}$, selects $t \in_R Z_q^*$ and computes $\beta = \alpha'$, then B_i signs U 's withdrawal message m with group blind signature as the step of **sign** in section 2.2. Then the e-coin is $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, C_0, C_1, \alpha, \beta)$.

(3) B_i stores $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, \alpha, \beta, x_1, f(x_1))$ into his database and stores t into the tracing database of the group manager.

Pay and deposit:

1 U chooses $x_2 \in_R Z_p^*$, computes $f(x_2)$, sends $\langle x_2, f(x_2) \rangle$ and $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, C_0, C_1, \alpha, \beta)$ to the shop.

2 Shop checks the validity of $(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3)$ and $C_0 C_1^{x_2} = g^{f(x_2)}$, then sends $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, C_0, C_1, \alpha, \beta)$ to his bank B_j .

3 B_j validates $(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3)$, checks if $\alpha = \beta^{t_i}$ for all t_i in the tracing database managed by the group manager. If for all $t_i, \alpha \neq \beta^{t_i}$, checks if the e-coin is double-spent via the online database of the group manager, if not, then deposits $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, C_0, C_1, \alpha, \beta)$ into the shop's account and informs the shop, the shop sends the merchandise to U; If there exists some t_i such that $\alpha = \beta^{t_i}$, then freezes $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, C_0, C_1, \alpha, \beta)$ and informs the shop, the shop refuses sending the merchandise to U.

Identity revocation: If the shop or B_j checks that there's something suspicious on the e-coin, such as $\alpha = \beta^{t_i}$ for some t_i , B_j sends $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, C_0, C_1, \alpha, \beta)$ to the group manager, the group manager opens $(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3)$ using the **open** technique in the group blind signature and finds the bank B_i , sends the e-coin to B_i . B_i looks up his database and finds $m(\hat{g}, \hat{z}, v_1', \dots, v_t', V_1, V_2, V_3, \alpha, \beta, C_0, C_1, x_1, f(x_1))$, then B_i and the shop can recover $f(x) = c_0 + c_1 x$ by use of Shamir's secret sharing scheme with $\langle x_1, f(x_1) \rangle$ and $\langle x_2, f(x_2) \rangle$. B_i can find U's identity by testing if $c_0 = I^{\alpha_i}$ for every user I .

4. Analysis

Prevention of blackmailing: When a user U is blackmailed, he selects $\delta \neq r$, sends $\alpha' = \alpha^\delta$ to B_i , B_i can find the deference α' from α^δ and gives U the marked e-coin, but, the blackmailer can't find the deference α' from α^δ , and he is cheated successfully. Later, he can't buy back anything because any bank can identify the marked coin and freezes it. Also, the kind shop and the bank issuing the coin can identify the victim by using the **identity revocation** technique in the proposed scheme and give back the coin to the victim.

Anonymity of coins: Nobody but the Central Bank can know by which bank the e-coin is issued because of the anonymity of the group signature. However, the anonymity is conditional under an abnormal situation, i.e., the marked coin can be recognized.

Anonymity of users: A user can spend his e-coin anonymously; no bank or shop can trace the user alone without the help of the group manager because the coin is issued using blind signature.

Traceability: With the help of the group manager, the bank issuing the e-coin and the shop owning the coin can collaborate to find the user of the e-coin by use of Shamir's secret sharing scheme.

Revocation of dishonest banks: A dishonest bank can be deleted by the group manager via issuing his membership key on a bulletin board. The deleted bank can't issue e-coin continuously with his old certificate because he can't prove that his identity is not on the bulletin board; the previous e-coin issued by a deleted bank will not be disclosed because any other party can't obtain his secret key x and certificate v by his published identity z due to RSA assumption.

5. Conclusions

In this paper, we propose a fair electronic cash system with member deletion. Besides having the general functions in other e-cash systems based on group signature, our scheme can also revoke the dishonest banks without disclosing their previous data. Also, in our scheme the bank uses a novel method to issue e-coin in order to prevent from blackmailing, kidnapping etc. Furthermore, our scheme is a system without trustees and is constructed for multiple banks as in the real life, thus it is more practical.

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