Crossing the Borderline – From Formal to Semi-Formal Specifications

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Abstract. Being part of the systems' documentation state-based formal specifications can play a crucial role in the software development process. However, besides dense mathematical expressions, their semantical compactness and lack in visually appealing notations impede their use and comprehensibility among different stakeholders. One solution to this problem is to enrich the specification by a semi-formal view, in most cases diagrams with a sufficiently understood semantic meaning. However, as control- and data-dependencies within declarative specifications are hard to detect, existing approaches only cover statics-bearing diagrams. As a way out this paper presents an approach for control- and data dependency analysis within declarative formal specifications. Based on these dependencies, UML diagrams showing static and dynamic properties of the specification are generated.

1 Introduction

Formal software specifications are usually recommended as means to produce high-quality software. They can solve the verification problem (“do the system right”). But, even if the system has been refined correctly, there is another problem to be solved: the validation problem (“do the right system”).

What sounds like a requirements elicitation problem also has to do with the problem of choosing a suitable notation. The risky part is that the stakeholders of the project (developers, customers, authorities) have to agree upon the meaning of the formal specification. Here, unclear requirements and specifications lead to futile validations easily. And this, in consequence, leads to a “buggy” system. So, the problem is not the formal notation, as its semantics is well-defined. The problem is the likely misinterpretation of concepts – due to the different habits of the stakeholders.

So why not just combining formal specifications and wide-spread semi-formal approaches? Such a combination would have several advantages. Different views (either of graphical or textual/mathematical nature) convey the concepts much better between different stakeholders. The approaches are not meant to replace each other, but they extend the possibilities of concept description: properties of semi-formal descriptions get deducible (by stepping into the formal world) and formal specifications can be described at an even more abstract level.

Several research teams are working on the issue of mapping graphical approaches (e.g. UML) to formal specification languages. The generated specification is then

Please use the following format when citing this chapter:

Bollin, A., 2006, in IFIP International Federation for Information Processing, Volume 227, Software Engineering Techniques: Design for Quality, ed. K. Sacha, (Boston: Springer), pp. 73–84.

used for consistency checking and test-data generation [1, 2]. Moving the other way round still has its limitations [3]. The reasons are the superficial analysis of state-based specification and missing flow of control. As a result only static class diagrams (that represent state variables of the specification) are generated so far.

With the reconstruction of control- and data- dependencies (via specification transformations [4]) much more gets possible: slices and chunks allow to excerpt pieces of the specification text with well-defined semantics, and cluster generation allows for carving out higher level specification concepts [5]. Finally, and as demonstrated in this contribution, by making use of control dependencies it gets feasible to visualize dynamic behavior of specifications the first time.

The contribution is structured as follows. Section 2 explains the need for bridging the gaps in more detail and presents the state-of-the-art of transforming UML diagrams to formal specifications and vice-versa. It gives special attention to some limitations of existing approaches: the scaling problem, and missing dynamics. Section 3 discusses ways to identify relevant elements within Z specifications [6] which will then be the basis for control- and data-dependency reconstruction. Section 4 then presents rules for the transformation (based on these dependencies). It explains the approach by making use of a small Z specification. The paper concludes with a short summary and an outlook.

2 Bridging the Gap

It would be the dream of every maintenance personnel, but neither does a SW-system, in general, adapt itself to changing situations or domains (retaining or even improving its quality), nor is it just straight-forward to produce new software products of high quality. As Glass [7, p.122] points out, comprehending the requirements and valid (and consistent) documentation is essential, but rarely all documents are available or are of suitable quality. This is one of the main problems during software comprehension¹. A situation that should be improved whenever possible.

2.1 Comprehension Challenges

There are several models describing how to maintain software systems [8, 9], but all of them stress that it is necessary to first comprehend the requirements *and* the relevant parts of the underlying system. Starting from scratch and stepping through the code is very time-consuming. Banker et. al. point out the fact that the time needed to comprehend a system on the basis of software code alone is about 3.5 times longer than comprehending the system by additionally studying its documentation [10]. Thus making use of design documents and specifications helps in saving time. But where are the problems?

Well, formal specifications are closer to the requirements – but comprehension needs special skills, and so stakeholders seem to shy away from them. The problems are manifold and are the result of the following gaps between the two worlds:

P1 Formal specifications are said to be of high perceived complexity.

¹ According to Glass it is second only. The main cause for software comprehension problem is staff turnover.

- P2 Not all stakeholders that are forced to comprehend the systems (and then to decide) are able to read and understand the underlying documents.
- P3 Relating formal specifications with well defined semantics to less formal notations is a loss in precision.
- P4 Creating formal specifications from less formal documents is impeded due to information deficiencies. It needs effort to fill the gaps.

What is easily overseen is that comprehending a system means the reconstruction of the missing documentation anyway. Concerning problem P1, the overall (and inherent) complexity cannot be reduced. But there are approaches to deal with the density of specifications [11]. And the remaining challenges P2 to P4 (understandability and formality) can be dealt with by consciously mapping the relevant representations to each other. The gaps can be bridged.

2.2 Impediments

The statements so far lead to one observation: the better and more extensive the documentation the easier the comprehension process. A less formal or less mathematical document can also serve its purpose. And a further improvement to the situation is to combine the formal and semi-formal documentation, to reconstruct parts of the documentation, and to be able to switch between different types of notation as needed.

As explained below, complexity (problem P1) does not make difficulties. In fact it is in the nature of formal specifications, and it concerns two aspects:

1. Usually there are too few clues for reconstructing the original structure. Putting too much structure into a formal specification is understood to be a hint towards implementation, something that is avoided at the time of writing the specification.
2. The declarative nature also impedes the reconstruction of the behavior. There is no execution-sequence, which is known from programming languages.

Above all, the latter aspect is crucial. As there is no execution order and, in general, there are no control statements, control- and data-dependency are not predominant concepts. Well-known techniques from the field of program comprehension cannot be applied directly. A state-based specification focuses on, naturally, states, and alternative forms of representation are then restricted to just static information, too.

2.3 Related Work

For the reasons mentioned in Section 2.2 the mapping between formal specifications and less formal approaches is limited to static information. Besides formal extensions to existing notations (e.g. VDM-link to UML [12], or Petri-nets with Z extensions [13]), two directions of the mapping are possible.

Firstly, there is a mapping between some graphical notations to formal specifications. As UML is wide-spread, most of them take static UML diagrams and generate formal state descriptions of it (e.g. UML to Z [14, 15], or UML to Z++ [16, 17]). The approaches have in common that formal specification skeletons are generated which then have to be completed by the designer. As a second step the resulting predicates

are simplified, leading, finally, to a full and compact formal specification. This means that semantics has to be added by the designer, but when dealt with it carefully, the specification can be taken to prove properties of the system. Results can then be mapped back to the design documents and deficiencies eliminated.

The other way round is the mapping of formal specification to some graphical notation. An early approach is the Z visualization of Kim [18], who makes use of constraint diagrams (a notation formally defined by Kent [19]). The notation is able to express predicate logic, but there is no integration into existing frameworks. And it is not UML, which does not really ease the understanding among some stakeholders.

However, not all the time the full content has to be imparted, and UML, keeping on spreading, is a good target for the transformation. The approach of Fekih et.al maps B specifications to UML [20]. It takes the state space of the specification and creates an UML class for every abstract set that is element in the domain of relations. The transformation rules are simple but lead to incomplete class diagrams as operations are not regarded. In addition to that the generated classes are not associated. Idani and Ledru improve the approach by mapping occurring relations to UML associations [3]. Furthermore they take operations into account and provide an algorithm for mapping an operation as a method to the most suitable class. Altogether this leads to a more complete static UML diagram.

Contributions mapping formal specifications to UML diagrams follow a pragmatic approach: sets do correspond to classes and relations do correspond to associations. However, as also noted in [3], the resulting diagrams provide less information than the formal specification, and dynamics is not touched at all.

3 Theoretical Background

The reconstruction of dependencies within declarative specification languages is not straight-forward. When looking for control constructs (which will then be the basis for the reconstruction of dynamic behavior), one has to be careful about the basic elements the control is defined about.

3.1 Specification Primes

Specifications are constructed from basic (atomic) units, called specification literals. They can be identified by looking at the grammar of the specification language. As an example, the Z predicate “ $assigned \subseteq Permitted$ ” contains the specification literals “Assigned”, “ $\subseteq$ ”, and “Permitted”. Specification literals are not very expressive when standing alone. It is the combination of literals that makes them rich in content. By aggregating specification literals, *prime objects* of a specification are built.

Definition 1 *A specification prime object represents the basic entity of a specification. It is built out of specification literals and forms logic, syntactic, or semantic units.*

Schema	Approximation via Conditions	Related Primes
S	$post\ S \Rightarrow_c pre\ S$	$pos \Rightarrow_c prs$
$\neg S$	$post_s(\neg S) \Rightarrow_c pre_w(\neg S)$	$pos \Rightarrow_c prs$
$S \vee T$	$post(S \vee T) \Rightarrow_c pre(S \vee T)$	$(pos \cup pot) \Rightarrow_c (prs \cup prt)$
$S \Rightarrow T$	$post_s(S \Rightarrow T) \Rightarrow_c pre_w(S \Rightarrow T)$	$(pos \cup pot) \Rightarrow_c (prs \cup prt)$
$S \wedge T$	$post(S \wedge T) \Rightarrow_c pre_w(S \wedge T)$	$(pos \cup pot) \Rightarrow_c (prs \cup prt)$
$S \Leftrightarrow T$	$post_s(S \Leftrightarrow T) \Rightarrow_c pre_w(S \Leftrightarrow T)$	$(pos \cup pot) \Rightarrow_c (prs \cup prt)$
$S \upharpoonright T$	$post(S \upharpoonright T) \Rightarrow_c pre_w(S \upharpoonright T)$	$(pos \cup pot) \Rightarrow_c (prs \cup prt)$
$S \circ T$	$post_s(S \circ T) \Rightarrow_c pre(S \circ T)$	$(pos \cup pot) \Rightarrow_c prs$
$S \gg T$	$post_s(S \gg T) \Rightarrow_c pre(S \gg T)$	$(pos \cup pot) \Rightarrow_c prs$

Tab. 1. The table summarizes the control dependencies occurring between pre- and postcondition primes in Z schema operations.

In specification languages prime objects can be expressions or predicates, but they can also be generic type or schema type definitions. When looking at the decoration of identifiers ($\square'$ or $\square!$ for after-states), post condition primes can easily be identified.

Definition 2 A Z-specification prime p is considered a post-condition prime, if prime p contains an after state identifier. Otherwise it is considered a pre-condition prime.

The following two predicates of the *AssignResource* operation schema in the *AccessControl Z Specification* (see App. A) can be assigned to one pre- and one post-condition prime,

$$\begin{array}{ll}
 user? \notin \text{dom Assigned} & \% \text{Precondition Prime} \\
 Assigned' = Assigned \cup \{user? \mapsto resource?\} & \% \text{Postcondition Prime}
 \end{array}$$

as the second prime contains an after-state identifier (*Assigned'*). The identification of control-dependencies is then based on these definitions.

3.2 Dependencies

The approach is based on the following simple idea: Preconditions determine whether predicates in the postcondition part are evaluated or not. Thus in specifications post-conditions are control dependent on pre-conditions, and the problem of the identification of control dependencies is reduced to the problem of the identification of pre- and post-conditions.

Not all specification languages do make pre- and post-conditions explicit. Additionally, when schema operations are used, pre- and post-conditions have to be calculated by performing a semantic analysis, a time- and resource-consuming task which cannot be fully automated. In [11] a syntactic approximation to the semantic analysis (see Tab. 1) is suggested and it is formally shown that this approximation yields suitable results.

Definition 3 Let S be a schema of a Z specification. Furthermore, let pr_s be the set of pre-condition primes of S and pos the set of post-condition primes of S . There is control dependency ($pos \Rightarrow_c prs$) within schema S , if pr_s and pos are not empty.

Type	Symbol	A	B	Type	Symbol	A	B
Relation	$A \leftrightarrow B$	*	*	Part. Surj.	$A \dashrightarrow B$	1..*	0..1
Partial	$A \nrightarrow B$	*	0..1	Total Surj.	$A \twoheadrightarrow B$	1..*	1
Total	$A \rightarrow B$	*	1	Total Bij.	$A \twoheadrightarrow B$	1	1
Part. Inj.	$A \dashrightarrow B$	0..1	0..1	Total Inj.	$A \twoheadrightarrow B$	0..1	1

Fig. 1. According to [3], relations between sets A and B are mapped to associations with given multiplicities.

Table 1 summarizes the dependencies among the predicates in the schemata. When there is flow of control, data-dependencies are easily detected:

Definition 4 A specification prime p is data dependent on a specification prime q ($p \Rightarrow_d q$) if (i) there exists at least one identifier v (literal denoting a data element) that occurs in both p and q , and (ii) v is defined in q and used in p , and (iii) either p and q are in the same scope, or p is control dependent on q .

4 Semi-Formal Transformation

With the reconstruction of dependencies within declarative specifications it gets possible to exploit both, static *and* dynamic diagrams of UML. In the following the Access Control system (see App. A) is taken to illustrate the transformation process.

4.1 Static Diagrams

The mapping to static class diagrams is based on the idea of looking for global type definitions. It follows mainly the approach of Idani et. al. [3], but omits assigning the operations to derived (and hard to find pertinent) classes. Instead it introduces a system class and assigns the operations to it.

Rule 1 Every state schema corresponds to a root class with the stereotype $\ll\text{system}\gg$ and the name of the schema.

Rule 2 In a Z specification “given sets” correspond to classes in the UML specification. They are connected to the system class by using a “use” association.

Typically this exactly is the view of a specification’s designer: having a state and relevant operations. Abstract types are mapped to classes, and these classes are associated to the system class.

A specification also consists of several identifiers holding the state. When they describe relations between given sets, then they are resolved as associations. Subset relations ($\subset$ or $\subseteq$) are made explicitly. Finally, operation names are added, and for the description of the diagram unique names for the associations are introduced:

Rule 3 Every variable representing relationships between entities in the state schema is translated to associations. It holds that (i) multiplicity is resolved by the mapping rules presented in Fig. 1, and (ii) subsets between relations are resolved by a subset constraint.

Fig. 2. Applying Rules 1 to 6 leads to a static UML Diagram for the Access Control system specification (see Appendix A).

Rule 4 Every variable representing a subset of entities in the state schema is translated to a specialization class and connected to its root class.

Rule 5 Associations do get role-names. They are built by combining the first characters of the source class and association name.

Rule 6 Every operation schema is added as a method to those system root class, which has been included in the operations' declaration part. The initialization schema is mapped as a constructor to this class.

Fig. 2 presents the result of the transformation. The system class contains the operations. As there are three given set definitions (Users, Resources, Addresses), three classes are introduced and connected to the system class. *Unused* is modelled as a subset of *Resources*, and *Assigned* and *Permitted* are enriched by a subset constraint.

In fact, the above algorithm leads to class/attribute candidates. Still some problems with the transformation remain. It works well when there is only a small set of given sets. With larger specifications the approach of taking given sets as classes leads to a huge static UML diagram. Carving out higher-level concepts [5] and grouping them into extra diagrams might be a way out.

4.2 Dynamics

UML also allows for dynamic diagrams, and as there is also some sort of dynamics within specifications it should be represented in a convenient way. The approach makes use of UML's activity diagrams and focusses on the above defined notion of control and data dependencies.

Rule 7 Every schema operation is represented by an activity diagram. Logical operations are resolved as boolean expressions. Sequential operations are transformed to sequential control arcs.

Fig. 3. (a) Applying rules 7 and 8 leads to two UML Activity Diagrams, (b) applying rule 9 leads to an annotated static UML Diagram that makes use of OCL-like annotations.

Rule 8 Control dependencies between two operations are mapped to activity diagrams with control flow vertices. Data dependencies are mapped to activity diagrams by using object flow nodes with the label of the relevant identifier(s).

The specification has one schema operation called *ActiveAccessControl*. It contains a sequential schema operation and the logical combination of the remaining operation schemata. Fig. 3(a), left side, presents the result of rule 7. It puts the initialization in sequence to the operations, which are logically combined by an OR-operation.

According to the definition of control dependency and the rules in Tab. 1 there is, e.g., control dependency between the two schemata *AccessControl* and *AddPermission* (as *AddPermission* includes the state schema and has post-condition primes which get dependent on the *AddPermission*'s pre-condition primes). Another diagram is added and thus makes the control dependency explicit. Due to the fact that there is also data-dependency (the value of *Permitted* is relevant), *Permitted* is added as an object flow node. Finally, the more formal part of the specification must not be forgotten. By using OCL constraints, the relevant pre- and post-condition predicates can be included.

Rule 9 Pre- and Post-conditions of operation schemata are mapped to pre and post OCL comments to the system class; the predicates of the state schema are mapped to the class as OCL invariants. For Z operations expressive function names are to be chosen, their semantics is to be explained in a legend box.

Fig. 4. Parts of the ASRN net representation and source of the AccessControl specification. Primes are mapped to vertices and annotations are used for the transformation process.

Fig. 3(b) demonstrates the result of the transformation to a set of OCL comments. The constructor (initialization schema) gets a postcondition constraint, the three operation schemata get a pre- and post-condition each. The post-condition of *ListUsers*, e.g., tells us that the application does not change the set of resources ($r == r \bullet pre$, the after-state is the same as the before state). The system class is associated with the class invariant. Typically as is, predicate logic, Z functions, and operations are difficult to express in OCL. Here it is suggested to choose mnemonic names instead.

4.3 Automatic Generation

Specification primes are the basic, semantics-bearing elements of a specification. In [4, 11] it is described that state-based specifications can be mapped to a graph representation called ASRN (*Augmented Specification Relationship Net*), and that this graph can be used to detect dependencies by just breaking down the task to reachability conditions. This net is now used to simplify the transformation to UML. A small part of the AccessControl ASRN net can be found in Fig. 4.

The basic idea behind the net is that higher level primes are made up of a set of start and end vertices – which contain prime elements. Every vertex gets annotated (line numbers, text, and definition and use information of literals), and references and dependencies to other primes are expressed by (classified) edges between these primes.

The mapping process to UML is then straight-forward. Rules 1, 2, and 6 are based on the identification of state and operation schemata. Relevant start vertices have to contain

type-declarations ($T\{\text{some_id}\}$). By looking at their successor vertices, operations and state schemata get separated (as only operations contain Delta and Xi annotations referencing other state schemata) and the corresponding UML diagrams can be generated. When all state schemata are identified, rules 3, 4, and 5 are resolved. Associations are resolved by looking at related prime vertices that contain type-declarations and relevant specification annotations (like $\leftrightarrow$ or $\rightarrow$, according to Tab. 1).

The same approach is used for the generation of activity diagrams (rules 7 and 8). As the ASRN also contains control and data-dependency arcs, they are easily mapped to transitions in activity diagrams. Finally, for the generation of the OCL text (rule 9), again the annotations connected to the primes ($A(\text{source})$) are parsed and printed.

Mapping the rules (on the basis of the ASRN) to a program is straight forward and the transformation can be done in reasonable time. However, the problem is still the neat visualization of all the diagrams - and for an optimal positioning of all the objects on the screen some user action is still needed.

5 Conclusion

Comprehension is an inevitable task during software maintenance and development phases, and specifications, when kept up-to-date, are valid sources. However, due to their complexity it is not surprising that formal specifications languages are said to be write-only languages.

This paper discusses ways in transforming formal Z specifications to UML in order to open the documents to a wider range of stakeholders. Existing approaches only cover static information, but state-based specifications also deal with state changes – and thus dynamics. In contrary to existing approaches (which the pure focus on class diagrams) this paper suggests to make also use of activity diagrams. It explains how to identify control dependencies, which are then the basis for the latter reconstruction of dynamic behavior within declarative specifications.

There are still some limitations that should not be concealed. As with other approaches the issue of scalability is not solved, and in addition to that it is still hard to decide whether a class candidate is a pertinent class or not. To test the applicability of the approach a framework for dealing with large Z specifications (combining slicing, chunking, and UML transformation) is under further development.

The approach does, by far, not lead to a perfect UML representation of the specification. But it provides a good picture of *what is in* the specification. In fact it can at least be used to speed up the re-construction of concepts behind. And as dynamics is at least as important as statics, this approach should be a step further into the direction of a more useable framework and increase the use of formal specification.

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Appendix A - Access Control Specification

[*USERS*, *RESOURCES*, *ADDRESSES*]

AccessControl

Permitted : *USERS* $\leftrightarrow$ *RESOURCES*

Assigned : *USERS* $\rightarrow$ *RESOURCES*

IpAddress : *ADDRESSES* $\rightarrow$ *RESOURCES*

Unused : $\mathbb{P}$ *RESOURCES*

Assigned $\subseteq$ *Permitted*

Unused $\cap$ ($\text{ran } \textit{Assigned}$) = $\emptyset$

InitAccessControl

AccessControl

Permitted = $\emptyset$

Assigned = $\emptyset$

IpAddress = $\emptyset$

AddPermission

$\Delta \textit{AccessControl}$

user? : *USERS*

resource? : *RESOURCES*

(*user?* $\mapsto$ *resource?*) $\notin$ *Permitted*

Permitted' = *Permitted* $\cup$ {*user?* $\mapsto$ *resource?*}

ListUsers

$\exists \textit{AccessControl}$

resource? : *RESOURCE*

st! : $\mathbb{P}$ *USERS*

st! = $\text{dom}(\textit{Permitted} \triangleright \{\textit{resource?}\})$

AssignResource

$\Delta \textit{AccessControl}$

user? : *USERS*

resource? : *RESOURCES*

(*user?* $\mapsto$ *resource?*) $\in$ *Permitted*

user? $\notin$ $\text{dom } \textit{Assigned}$

Assigned' = *Assigned* $\cup$ {*user?* $\mapsto$ *resource?*}

ActiveAccessControl == *InitAccessControl* ;
(*AddPermission* $\vee$ *ListUsers* $\vee$ *AssignResource*)