

Regular Article - Theoretical Physics

Study of $qqq\bar{q}Q$ pentaquark system in the chiral quark model

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Abstract With the discovery of some hidden-charm pentaquark resonances by the LHCb Collaboration, investigations of pentaquark states containing heavy quarks have aroused the interest of theorists. We study herein $qqq\bar{q}Q$ (q = u or d, Q = c or b) pentaguark system, in the framework of the chiral quark model. In consequence, some charmed and bottomed pentaquarks are considered to exist by five-body dynamical calculations. In the charm sector, $\Sigma_c \pi (IJ^P = 0\frac{1}{2}^-)$ and $\Sigma_c^* \pi (IJ^P = 0\frac{3}{2}^-)$ are possible candidates of $\Lambda_c(2595)$ and $\Lambda_c(2625)$, respectively. Besides, two high-spin states, $\Sigma_c^* \rho(IJ^P = 0\frac{5}{2}^-)$ and $\Delta D^*(IJ^P =$ $1\frac{5}{2}$), are also found in the energy region of 3.2 \sim 3.3 GeV. In the bottom sector, $\Sigma_b \pi (IJ^P = 0\frac{1}{2})$, $\Sigma_b^* \pi (IJ^P = 0\frac{3}{2})$ could be candidates of Λ_b (5912) and Λ_b (5920), respectively. And $\Sigma_b^* \rho(IJ^P = 0\frac{5}{2})$ and $\Delta B^*(IJ^P = 1\frac{5}{2})$ are found in the energy region of 6.5 \sim 6.6 GeV. $\Sigma_c^{(*)}\pi$ and $\Sigma_b^{(*)}\pi$ are expected as compact states, while $\Sigma_c^* \rho$, $\Sigma_b^* \rho$, ΔD^* and ΔB^* are expected as molecular states.

1 Introductin

Although the conventional quark model has achieved great success in describing the properties of ground states in the baryon sector with simple three-quark (qqq) configuration, it encounters difficulties in explaining some excited baryons with one quark in an orbital angular excitation. Faced with this situation, theorists have made an attempt to study the baryon structure with modified physical pictures that go beyond the simple quenched 3-quark models. In fact the spatial excitation energy of excited baryons is already sufficient to pull a $q\bar{q}$ pair from the gluon field, the multiquark system formed by this mechanism is considered to be more favor-

able than the P-wave excitation in the classical three-quark picture [1].

So far, many theoretical explanations for the excited baryons have been proposed from the unquenched picture. In the light baryon sector, the mass order reverse problem of $N^*(1535)$ and $\Lambda^*(1405)$ can be easily understood by considering them to be dynamically generated meson-baryon states [2–8] or states with large pentaquark components [9–11]. In the heavy baryon sector, some charmed baryons discovered in recent years, lie near their S-wave baryon-meson thresholds, which indicates that they are probably molecular pentaguark states with the exception of three-quark baryons in an orbital excitation. For instance, $\Lambda_c(2595)$ and $\Lambda_c(2625)$ are suggested to be a dynamically generated state of $\Sigma_c \pi$ and $\Sigma_c^* \pi$ coupling with other possible higher channels [12-14], while they are also suggested to be generated states dominant by ND and ND^* [15–19]. And the Λ_c (2940) has been broadly discussed as a molecular state composed of a nucleon and D^* meson [20–23], while an isovector state of Σ_c (2800), whose energy is a little below the ND threshold, is still treated as a dynamically generated state from baryon-meson interactions [24–27]. For the bottomed baryons, $\Lambda_b(5912)$ and $\Lambda_b(5920)$ are suggested to be $\Sigma_b \pi$ and $\Sigma_b^* \pi$ [13], while in Refs. [28,29], the dominant coupled channel is identified as $N\bar{B}$ and $N\bar{B}^*$. Despite many theoretical explanations to these excited baryons, their structures and properties are still controversial, thus it requires more efforts to investigate these states. On the experimental side, the several P_c states were observed in the $J/\psi p$ invariant mass distribution of the $\Lambda_b^0 \to J/\psi K^- p$ decay by the LHCb Collaboration [30,31], which triggers an upsurge in investigations of pentaquark states containing heavy quarks.

Based on the above facts, we do a dynamic calculation of molecular five-quark system, composed of $qqq\bar{q}Q$ (q=u or d, Q=c or b), in the framework of the chiral quark model (ChQM). The chiral quark model has been used to study the recently observed hidden-charm pentaquarks [32], and the results are supported by many other theoretical stud-

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224 Page 2 of 12 Eur. Phys. J. C (2021) 81:224

ies. In order to strictly solve Schrödinger equation, a powerful method of few-body system, the Gaussian expansion method (GEM) [33], is employed to deal with orbital wave functions of five-body system. In the present work, because we are interested in the lowest-lying states of five-quark system, only the possible quantum numbers with negative parity are taken into account. In addition, we select the molecular configuration as the starting point of the research because: (1), masses of those charmed baryons with negative parity are very close to the relevant baryon-meson thresholds and molecular configuration is more physically possible compared with other configurations; (2), the energy of hidden color channel is generally higher than that of color-singlet channel, and the molecular configuration is the only possible way constructed by color-singlet structure. Two spatial configurations, $[qqQ][\bar{q}q]$ and $[qqq][\bar{q}Q]$, with all possible color, spin, flavor structures are considered in our calculation. Through the systematical search for bound states or possible resonant states, our purpose is to investigate whether some charmed baryons could be explained from the perspective of pentaquark states. On the other hand, an extension to the bottom case is performed to look for more states that may be observed in future experiments.

The paper is organized as follows. In Sect. 2, a brief introduction of the chiral quark model and the wave functions of the $qqq\bar{q}Q$ are presented. The numerical results are discussed in Sect. 3. In the last section, we give a brief summary of this work.

2 Theoretical framework

2.1 The chiral quark model

The calculation is done in the framework of ChQM, which has been successfully applied in describing hadron spectrum and hadron-hadron interaction [34–37]. The Hamiltonian for multiquark system takes the form,

$$H = \sum_{i=1}^{n} \left(m_i + \frac{\mathbf{p}_i^2}{2m_i} \right) - T_{cm}$$

$$+ \sum_{j>i=1}^{n} \left(V_{ij}^C + V_{ij}^G + V_{ij}^{\pi} \right)$$

$$+ V_{ij}^K + V_{ij}^{\eta} + V_{ij}^{\sigma} \right), \qquad (1)$$

$$V_{ij}^C = \left(\boldsymbol{\lambda}_i^c \cdot \boldsymbol{\lambda}_j^c \right) \left[-a_c \left(1 - e^{-\mu_c r_{ij}} \right) + \Delta \right], \qquad (2)$$

$$V_{ij}^G = \frac{1}{4} \alpha_s \left(\boldsymbol{\lambda}_i^c \cdot \boldsymbol{\lambda}_j^c \right)$$

$$\times \left[\frac{1}{r_{ij}} - \frac{1}{6m_i m_j} \frac{e^{-\frac{r_{ij}}{r_0(\mu_{ij})}} \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j}{r_{ij} r_0^2(\mu_{ij})} \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j \right],$$



$$r_{0}(\mu_{ij}) = \hat{r}_{0}/\mu_{ij}, \qquad (3)$$

$$V_{ij}^{\sigma} = -\frac{g_{ch}^{2}}{4\pi} \frac{\Lambda_{\sigma}^{2}}{\Lambda_{\sigma}^{2} - m_{\sigma}^{2}} m_{\sigma}$$

$$\times \left[Y(m_{\sigma}r_{ij}) - \frac{\Lambda_{\sigma}}{m_{\sigma}} Y(\Lambda_{\sigma}r_{ij}) \right], \qquad (4)$$

$$V_{ij}^{\pi} = \frac{g_{ch}^{2}}{4\pi} \frac{m_{\pi}^{2}}{12m_{i}m_{j}} \frac{\Lambda_{\pi}^{2}}{\Lambda_{\pi}^{2} - m_{\pi}^{2}} m_{\pi} \left[Y(m_{\pi}r_{ij}) - \frac{\Lambda_{\pi}^{3}}{m_{\pi}^{3}} Y(\Lambda_{\pi}r_{ij}) \right] \sigma_{i} \cdot \sigma_{j} \sum_{a=1}^{3} \lambda_{i}^{a} \lambda_{j}^{a}, \qquad (5)$$

$$V_{ij}^{K} = \frac{g_{ch}^{2}}{4\pi} \frac{m_{K}^{2}}{12m_{i}m_{j}} \frac{\Lambda_{K}^{2}}{\Lambda_{K}^{2} - m_{K}^{2}} m_{K} \left[Y(m_{K}r_{ij}) - \frac{\Lambda_{K}^{3}}{m_{K}^{3}} Y(\Lambda_{K}r_{ij}) \right] \sigma_{i} \cdot \sigma_{j} \sum_{a=4}^{7} \lambda_{i}^{a} \lambda_{j}^{a}, \qquad (6)$$

$$V_{ij}^{\eta} = \frac{g_{ch}^{2}}{4\pi} \frac{m_{\eta}^{2}}{12m_{i}m_{j}} \frac{\Lambda_{\eta}^{2}}{\Lambda_{\eta}^{2} - m_{\eta}^{2}} m_{\eta} \left[Y(m_{\eta}r_{ij}) - \frac{\Lambda_{\eta}^{3}}{m_{\eta}^{3}} Y(\Lambda_{\eta}r_{ij}) \right] \sigma_{i} \cdot \sigma_{j}$$

$$\left(\lambda_{i}^{8} \lambda_{j}^{8} \cos \theta_{p} - \lambda_{i}^{0} \lambda_{j}^{0} \sin \theta_{p} \right). \qquad (7)$$

Where m_i is the mass of constituent quarks and T_{cm} is the center-of-mass kinetic energy. The two-body potential includes phenomenology confinement potential V^C , onegluon-exchange potential V^G , Goldstone boson exchange interactions V^{π} , V^{K} , V^{η} , and scalar meson potential V^{σ} . Note herein that the meson exchanges are considered when the two quarks are light, while the color confinement and the one-gluon exchange are flavor blindness. λ and λ^c are SU(3)Gell-Mann matrices of flavor and color respectively, and σ is the SU(2) Pauli matrix. $r_0(\mu_{ij})$ is a regulator that depends on μ_{ij} . The chiral coupling constant g_{ch} is determined from the pion-nucleon coupling constant and Y(x) is the standard Yukawa functions. The specific introduction of the model can be found in Refs. [38–40]. In order to avoid the baryon-meson threshold order reversal, some hadrons should be described well in this work. The two sets of model parameters listed in Table 1 are adjusted by fitting the hadrons that we need. And some mesons and baryons involved in the present work are calculated with these parameters as shown in Table 2.

2.2 The wave function

As shown in Fig. 1, there are two types of spatial configurations for $qqq\bar{q}Q$ system, one is the heavy quark in the 3-quark cluster denoted as $[qqQ][\bar{q}q]$, the other is the heavy quark in the 2-quark cluster denoted as $[qqq][\bar{q}Q]$. The orbital wave function of the five-quark system can be obtained by cou-

Eur. Phys. J. C (2021) 81:224 Page 3 of 12 224

Table 1 Ouark Model Parameters

Quark masses		
$m_q = m_{\bar{q}}(MeV)$	450	430
$m_c(MeV)$	1750	1734
$m_b(MeV)$	5100	5092
Confinement		
$a_c(MeV)$	80	74
$\mu_c(fm^{-1})$	0.7	0.7
$\Delta(MeV)$	46	36
OGE		
$lpha_{\scriptscriptstyle S}^{qq}$	0.67	0.68
$lpha_s^{qc}$	0.61	0.63
$lpha_{\scriptscriptstyle S}^{qb}$	0.59	0.61
$\hat{r}_0(MeV\cdot fm)$	28.17	28.17
Goldstone bosons		
$m_{\pi}(fm^{-1})$	0.7	0.7
$m_K(fm^{-1})$	2.51	2.51
$m_{\eta}(fm^{-1})$	2.77	2.77
$m_{\sigma}(fm^{-1})$	3.42	3.42
$\Lambda_{\pi} = \Lambda_{\sigma}(fm^{-1})$	4.2	4.2
$\Lambda_K = \Lambda_{\eta}(fm^{-1})$	5.2	5.2
$g_{ch}^2/(4\pi)$	0.54	0.54
$\theta_p(^\circ)$	-15	-15

pling the orbital wave function of each relative motion, and is written as follows,

$$\psi_{LM_L} = [[[\psi_{l_1}(\mathbf{r}_{12})\psi_{l_2}(\mathbf{r}_{12,3})]_l\psi_{l_3}(\mathbf{r}_{45})]_{l'}\psi_{l_4}$$

$$(\mathbf{r}_{123,45})]_{LM_L},$$
(8)

where

$$r_{12} = r_1 - r_2,$$

$$r_{12,3} = \frac{m_1 r_1 + m_2 r_2}{m_1 + m_2} - r_3,$$

$$r_{45} = r_4 - r_5,$$

$$r_{123,45} = \frac{m_1 r_1 + m_2 r_2 + m_3 r_3}{m_1 + m_2 + m_3} - \frac{m_4 r_4 + m_5 r_5}{m_4 + m_5}.$$
 (9)

Table 2 The masses of the mesons and baryons involved in the calculation (unit: MeV)

Meson	I	II	Exp. [41]	Baryon	I	II	Exp. [41]
π	156	149	140	N	915	908	939
ρ	795	799	775	Δ	1229	1235	1232
η	660	672	548	Λ_c	2270	2263	2286
ω	773	777	783	Σ_c	2469	2473	2455
D	1867	1866	1869	Σ_c^*	2495	2499	2518
D^*	2031	2034	2007	Λ_b	5586	5589	5620
B	5303	5315	5279	Σ_b	5808	5821	5811
B^*	5350	5362	5325	Σ_b^*	5818	5832	5832

Here $\psi_{l_1}(\mathbf{r}_{12})$, $\psi_{l_2}(\mathbf{r}_{12,3})$, $\psi_{l_3}(\mathbf{r}_{45})$ are the orbital wave functions of relative motions in each cluster respectively, and $\psi_{l_4}(\mathbf{r}_{123,45})$ is the orbital wave function between two clusters, square brackets represent the angular momentum coupling. It is too difficult to obtain the orbital wave function by solving the Schrödinger equation directly, so in our present work, GEM is employed to deal with orbital wave functions of five-body system. In GEM, the orbital wave function is written as the radial part and spherical harmonics, and the radial wave function is expanded by gaussians,

$$\psi_{lm}(\mathbf{r}) = \sum_{n=1}^{n_{max}} c_n \psi_{nlm}^G(\mathbf{r}), \tag{10}$$

$$\psi_{nlm}^{G}(\mathbf{r}) = N_{nl}r^{l}e^{-\nu_{n}r^{2}}Y_{lm}(\hat{\mathbf{r}}), \tag{11}$$

$$N_{nl} = \left(\frac{2^{l+2}(2\nu_n)^{l+\frac{3}{2}}}{\sqrt{\pi}(2l+1)!!}\right)^{\frac{1}{2}},\tag{12}$$

$$v_n = \frac{1}{r_n^2}, r_n = r_{min}a^{n-1}, a = \left(\frac{r_{max}}{r_{min}}\right)^{\frac{1}{n_{max}-1}}.$$
 (13)

Where c_n are expansion coefficients determined by solving the Schrödinger equation; N_{nl} are normalization constants; The Gaussian size r_n is taken as the geometric progression to significantly reduce the dimension of matrix and simplify the calculation. For the present study, $n_{max} = 7$ leads to a convergence result. Both the ground state energy and the radial excitation energy can be obtained by diagonalizing the Hamiltonian matrix.

When the angular momenta are not zero, the calculation of Hamiltonian matrix elements is rather complicated. It is convenient to employ the method of infinitesimally shifted Gaussians [33],

$$\psi_{nlm}^{G}(\mathbf{r}) = N_{nl}r^{l}e^{-\nu_{n}r^{2}}Y_{lm}(\hat{\mathbf{r}})
= N_{nl}\lim_{\epsilon \to 0} \frac{1}{(\nu_{n}\epsilon)^{l}} \sum_{k=1}^{k_{max}} C_{lm,k}e^{-\nu_{n}(\mathbf{r}-\epsilon \mathbf{D}_{lm,k})^{2}}.$$
(14)

the coefficients $C_{lm,k}$ and shift-direction vector $\mathbf{D}_{lm,k}$ are determined from the particular spherical harmonics. By



224 Page 4 of 12 Eur. Phys. J. C (2021) 81:224

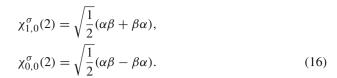
absorbing the spherical harmonics into the shifted gaussians, complicated angular momentum algebra can be avoided.

The total spin wave function $\chi_{S,M_S}^{\sigma}(5)$ are obtained by coupling the spin wave functions of each cluster using Clebsch-Gordan Coefficients. Since the magnetic spin quantum number M_S does not affect the energy of system, it is set to the maximum value here. There are five spin wave functions with $S=\frac{1}{2}$, four spin wave functions with $S=\frac{3}{2}$ and one spin wave function with $S=\frac{5}{2}$, respectively,

$$\begin{split} \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 1}(5) &= \sqrt{\frac{1}{6}} \chi_{\frac{3}{2},-\frac{1}{2}}^{\sigma}(3) \chi_{1,1}^{\sigma}(2) - \sqrt{\frac{1}{3}} \chi_{\frac{3}{2},\frac{1}{2}}^{\sigma}(3) \chi_{1,0}^{\sigma}(2) \\ &+ \sqrt{\frac{1}{2}} \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma}(3) \chi_{1,-1}^{\sigma}(2), \\ \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 2}(5) &= \sqrt{\frac{1}{3}} \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 1}(3) \chi_{1,0}^{\sigma}(2) - \sqrt{\frac{2}{3}} \chi_{\frac{1}{2},-\frac{1}{2}}^{\sigma 1}(3) \chi_{1,1}^{\sigma}(2), \\ \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 3}(5) &= \sqrt{\frac{1}{3}} \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 2}(3) \chi_{1,0}^{\sigma}(2) - \sqrt{\frac{2}{3}} \chi_{\frac{1}{2},-\frac{1}{2}}^{\sigma 2}(3) \chi_{1,1}^{\sigma}(2), \\ \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 4}(5) &= \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 1}(3) \chi_{0,0}^{\sigma}(2), \\ \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 5}(5) &= \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 2}(3) \chi_{1,0}^{\sigma}(2) - \sqrt{\frac{2}{5}} \chi_{\frac{3}{2},\frac{1}{2}}^{\sigma}(3) \chi_{1,1}^{\sigma}(2), \\ \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(5) &= \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(3) \chi_{0,0}^{\sigma}(2), \\ \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(5) &= \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 1}(3) \chi_{1,1}^{\sigma}(2), \\ \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(5) &= \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 1}(3) \chi_{1,1}^{\sigma}(2), \\ \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(5) &= \chi_{\frac{1}{2},\frac{1}{2}}^{\sigma 2}(3) \chi_{1,1}^{\sigma}(2), \\ \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(5) &= \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(3) \chi_{1,1}^{\sigma}(2), \\ \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(5) &= \chi_{\frac{3}{2},\frac{3}{2}}^{\sigma 3}(3) \chi_{1,1}^{\sigma}(2). \end{split}$$

Where $\chi_{S,M_S}^{\sigma}(3)$ and $\chi_{S,M_S}^{\sigma}(2)$ are the spin wave functions of each sub-cluster,

$$\begin{split} \chi^{\sigma}_{\frac{3}{2},\frac{3}{2}}(3) &= \alpha\alpha\alpha, \\ \chi^{\sigma}_{\frac{3}{2},-\frac{3}{2}}(3) &= \beta\beta\beta, \\ \chi^{\sigma}_{\frac{3}{2},-\frac{1}{2}}(3) &= \sqrt{\frac{1}{3}}(\alpha\alpha\beta + \alpha\beta\alpha + \beta\alpha\alpha), \\ \chi^{\sigma}_{\frac{3}{2},-\frac{1}{2}}(3) &= \sqrt{\frac{1}{3}}(\alpha\beta\beta + \beta\alpha\beta + \beta\beta\alpha), \\ \chi^{\sigma 1}_{\frac{1}{2},\frac{1}{2}}(3) &= \sqrt{\frac{1}{6}}(2\alpha\alpha\beta - \alpha\beta\alpha - \beta\alpha\alpha), \\ \chi^{\sigma 2}_{\frac{1}{2},\frac{1}{2}}(3) &= \sqrt{\frac{1}{2}}(\alpha\beta\alpha - \beta\alpha\alpha), \\ \chi^{\sigma 1}_{\frac{1}{2},-\frac{1}{2}}(3) &= \sqrt{\frac{1}{6}}(\alpha\beta\beta + \beta\alpha\beta - 2\beta\beta\alpha), \\ \chi^{\sigma 2}_{\frac{1}{2},-\frac{1}{2}}(3) &= \sqrt{\frac{1}{6}}(\alpha\beta\beta - \beta\alpha\beta), \\ \chi^{\sigma 2}_{\frac{1}{2},-\frac{1}{2}}(3) &= \sqrt{\frac{1}{2}}(\alpha\beta\beta - \beta\alpha\beta), \\ \chi^{\sigma}_{1,1}(2) &= \alpha\alpha, \\ \chi^{\sigma}_{1,-1}(2) &= \beta\beta, \end{split}$$



Where α and β denote spin-up and spin-down states, respectively.

The flavor wave function of five-quark system $\chi_{I,M_I}^f(5)$, can be obtained in the same way as the spin wave function. Here we take quark content $qqq\bar{q}c$ as an example,

$$\begin{split} \chi_{0,0}^{f1}(5) &= \chi_{0,0}^{f}(3)\chi_{0,0}^{f}(2), \\ \chi_{0,0}^{f2}(5) &= \sqrt{\frac{1}{2}}\chi_{\frac{1}{2},\frac{1}{2}}^{f1}(3)\chi_{\frac{1}{2},-\frac{1}{2}}^{f}(2) - \sqrt{\frac{1}{2}}\chi_{\frac{1}{2},-\frac{1}{2}}^{f1}(3)\chi_{\frac{1}{2},\frac{1}{2}}^{f}(2), \\ \chi_{0,0}^{f3}(5) &= \sqrt{\frac{1}{2}}\chi_{\frac{1}{2},\frac{1}{2}}^{f2}(3)\chi_{\frac{1}{2},-\frac{1}{2}}^{f}(2) - \sqrt{\frac{1}{2}}\chi_{\frac{1}{2},-\frac{1}{2}}^{f2}(3)\chi_{\frac{1}{2},\frac{1}{2}}^{f}(2), \\ \chi_{0,0}^{f4}(5) &= \sqrt{\frac{1}{3}}\chi_{1,1}^{f}(3)\chi_{1,-1}^{f}(2) - \sqrt{\frac{1}{3}}\chi_{1,0}^{f}(3)\chi_{1,0}^{f}(2) \\ &+ \sqrt{\frac{1}{3}}\chi_{1,-1}^{f}(3)\chi_{1,1}^{f}(2), \\ \chi_{1,1}^{f1}(5) &= \chi_{0,0}^{f}(3)\chi_{1,1}^{f}(2), \\ \chi_{1,1}^{f2}(5) &= \chi_{1,1}^{f}(3)\chi_{0,0}^{f}(2), \\ \chi_{1,1}^{f3}(5) &= \sqrt{\frac{1}{2}}\chi_{1,1}^{f}(3)\chi_{1,0}^{f}(2) - \sqrt{\frac{1}{2}}\chi_{1,0}^{f}(3)\chi_{1,1}^{f}(2), \\ \chi_{1,1}^{f4}(5) &= \chi_{\frac{1}{2},\frac{1}{2}}^{f1}(3)\chi_{\frac{1}{2},\frac{1}{2}}^{f}(2), \\ \chi_{1,1}^{f5}(5) &= \chi_{\frac{1}{2},\frac{1}{2}}^{f2}(3)\chi_{\frac{1}{2},-\frac{1}{2}}^{f}(2) - \sqrt{\frac{1}{4}}\chi_{\frac{3}{2},\frac{1}{2}}^{f}(3)\chi_{\frac{1}{2},\frac{1}{2}}^{f}(2), \\ \chi_{1,1}^{f6}(5) &= \sqrt{\frac{3}{4}}\chi_{\frac{3}{2},\frac{3}{2}}^{f}(3)\chi_{\frac{1}{2},-\frac{1}{2}}^{f}(2) - \sqrt{\frac{1}{4}}\chi_{\frac{3}{2},\frac{1}{2}}^{f}(3)\chi_{\frac{1}{2},\frac{1}{2}}^{f}(2), \\ \chi_{2,2}^{f2}(5) &= \chi_{1,1}^{f}(3)\chi_{1,1}^{f}(2), \\ \chi_{2,2}^{f2}(5) &= \chi_{\frac{3}{2},\frac{3}{2}}^{f}(3)\chi_{\frac{1}{2},-\frac{1}{2}}^{f}(2). \end{split}$$

Where $\chi_{I,M_I}^f(3)$ and $\chi_{I,M_I}^f(2)$ are the flavor wave functions of each sub-cluster based on the SU(2) flavor symmetry,

$$\chi_{0,0}^{f}(3) = \sqrt{\frac{1}{2}}(ud - du)c,$$

$$\chi_{\frac{1}{2}, \frac{1}{2}}^{f1}(3) = \sqrt{\frac{1}{6}}(2uud - udu - duu),$$

$$\chi_{\frac{1}{2}, \frac{1}{2}}^{f2}(3) = \sqrt{\frac{1}{2}}(udu - duu),$$

$$\chi_{\frac{1}{2}, -\frac{1}{2}}^{f1}(3) = \sqrt{\frac{1}{6}}(udd + dud - 2ddu),$$

$$\chi_{\frac{1}{2}, -\frac{1}{2}}^{f2}(3) = \sqrt{\frac{1}{2}}(udd - dud),$$

$$\chi_{1,1}^{f2}(3) = uuc,$$

$$\chi_{1,-1}^{f}(3) = ddc,$$



Eur. Phys. J. C (2021) 81:224 Page 5 of 12 224

$$\chi_{1,0}^{f}(3) = \sqrt{\frac{1}{2}}(ud + du)c,$$

$$\chi_{\frac{3}{2},\frac{3}{2}}^{f}(3) = uuu,$$

$$\chi_{\frac{3}{2},\frac{1}{2}}^{f}(3) = \sqrt{\frac{1}{3}}(uud + udu + duu),$$

$$\chi_{0,0}^{f}(2) = \sqrt{\frac{1}{2}}(\bar{d}d + \bar{u}u),$$

$$\chi_{\frac{1}{2},\frac{1}{2}}^{f}(2) = \bar{d}c,$$

$$\chi_{\frac{1}{2},-\frac{1}{2}}^{f}(2) = -\bar{u}c,$$

$$\chi_{1,1}^{f}(2) = \bar{d}u,$$

$$\chi_{1,-1}^{f}(2) = -\bar{u}d,$$

$$\chi_{1,0}^{f}(2) = \sqrt{\frac{1}{2}}(\bar{d}d - \bar{u}u).$$
(18)

The physical pentaquark states must be colorless, but the way of reaching this condition can be acquired through the coupling of two colorless clusters or two colorful clusters. Therefore, there are two kinds of color structures, one is the color singlet-singlet $1 \otimes 1$ structure, and another is color octet-octet $8 \otimes 8$ structure. Color singlet wave function χ_1^c , hidden color wave functions χ_2^c and χ_3^c , can be found in Ref. [42].

Finally, the total channel wave function of the five-quark system will be the product of orbit, spin, flavor and color components,

$$\Psi_{JM_JIM_I}^{ijk} = \mathcal{A}\left[\left[\psi_L \chi_S^{\sigma i}\right]_{JM_J} \chi_I^{fj} \chi_k^c\right]. \tag{19}$$

The i, j, k are the index of spin, flavor and color wave functions, respectively. Here, \mathcal{A} is the antisymmetry operator, which ensures the antisymmetry of the total wave function when identical particles exchange. For the configuration of $[qqQ][\bar{q}q]$ in Fig. 1, the antisymmetry operator is,

$$A = 1 - (15) - (25), \tag{20}$$

and for the configuration of $[qqq][\bar{q}Q]$,

$$A = 1 - (13) - (23). \tag{21}$$

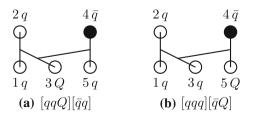


Fig. 1 The molecular structures of $qqq\bar{q}\,Q$ system. The hollow circles stand for quark and the black circle stands for antiquark

All possible physical channels for the $qqq\bar{q}c$ pentaquark system are listed in Table 3. Superscript S and H, denote color singlet channel and hidden color channel, respectively. The i, j, k are the index in Eq. (19).

The eigen-energy is obtained by solving the Schrödinger equation,

$$H\Psi_{JM_IIM_I} = E\Psi_{JM_IIM_I} \tag{22}$$

with the Rayleigh-Ritz variational principle.

3 Numerical results

First, we study odd parity charmed and bottomed baryons that have been experimentally observed from three-quark system in an orbital excitation. The wave function is constructed in the same way as described above. Nevertheless, the orbital wave function of the three-quark system is written as $\psi_{lm_l} = [\psi_{l_1}(\boldsymbol{r}_{12})\psi_{l_2}(\boldsymbol{r}_{12,3})]_l$, the wave functions of two relative motions, $\psi_{l_1}(\boldsymbol{r}_{12})$ and $\psi_{l_2}(\boldsymbol{r}_{12,3})$, are expanded by infinitesimally shifted gaussian function according to Eq. (14). For the P-wave three-quark system, two low-lying excitation modes are considered in the calculation. One is the excitation in the first relative motion, denoted as $(l_1, l_2) = (1, 0)$; the other is the excitation in the second relative motion, denoted as $(l_1, l_2) = (0, 1)$. The energy of P-wave baryon is obtained by coupling the two excitation modes.

The low-lying orbital excited energies of qqQ baryons with two sets of parameters are calculated and listed in Table 4. The energies of two excitation modes and their coupling are given respectively, while for Σ_c^* and Σ_b^* states, only one excitation mode is allowed in order to fulfill the Pauli principle. When the orbital angular momentum is set to one, the spin can couple with it to give total quantum numbers $J^P = \frac{1}{2}^-$, $J^P = \frac{3}{2}^-$ or $J^P = \frac{5}{2}^-$, we obtain the same energy for these states because the spin-orbit interaction is not involved in the present model. So only states with $J^P = \frac{1}{2}^-$ are given. Considering small effect of spinorbit interaction, it is enough to make a qualitative analysis. Although ground states of qqQ baryons in Table 2 are described well in this work, the results in Table 4 show that the energies of P-wave excitation are about 130 MeV lower than the experimental states with $J^P = \frac{1}{2}$. With regard to states with $J^P = \frac{3}{2}^-$, we also judge that there is a big deviation between the theoretical calculation and the experimental values even if the spin-orbit interaction is included. Therefore, we consider that it is inappropriate to explain these odd-parity excited states from the quenched three quark picture within our framework. Next we turn to the pentaquark system. In the present work, because we are interested in the lowest-lying states of five-quark system, the angular momentum of each relative motion is set to zero. The calculation



Table 3 Physical channels for $qqq\bar{q}c$ pentaquark system

IJ^P	[i;j;k]	Channel	IJ^P	[i;j;k]	Channel
$0\frac{1}{2}^{-}$	[4; 4; 1]	$(\Sigma_c\pi)^S$	$1\frac{1}{2}^{-}$	[5; 1; 1]	$(\Lambda_c\pi)^S$
	[4, 5; 4; 2, 3]	$(\Sigma_c\pi)^H$		[4, 5; 1; 2, 3]	$(\Lambda_c\pi)^H$
	[5; 1; 1]	$(\Lambda_c \eta)^S$		[4; 3; 1]	$(\Sigma_c\pi)^S$
	[4, 5; 1; 2, 3]	$(\Lambda_c\eta)^H$		[4, 5; 3; 2, 3]	$(\Sigma_c\pi)^H$
	[3; 1; 1]	$(\Lambda_c \omega)^S$		[4; 2; 1]	$(\Sigma_c \eta)^S$
	[2, 3; 1; 2, 3]	$(\Lambda_c \omega)^H$		[4, 5; 2; 2, 3]	$(\Sigma_c \eta)^H$
	[2; 4; 1]	$(\Sigma_c ho)^S$		[3; 1; 1]	$(\Lambda_c \rho)^S$
	[2, 3; 4; 2, 3]	$(\Sigma_c ho)^H$		[2, 3; 1; 2, 3]	$(\Lambda_c \rho)^H$
	[1; 4; 1]	$(\Sigma_c^* \rho)^S$		[2; 3; 1]	$(\Sigma_c \rho)^S$
	[1; 4; 3]	$(\Sigma_c^* ho)^H$		[2, 3; 3; 2, 3]	$(\Sigma_c \rho)^H$
	[4, 5; 2, 3; 1]	$(ND)^S$		[2; 2; 1]	$(\Sigma_c \omega)^S$
	[4, 5; 2, 3; 2, 3]	$(ND)^H$		[2, 3; 2; 2, 3]	$(\Sigma_c \omega)^H$
	[2, 3; 2, 3; 1]	$(ND^*)^S$		[1; 3; 1]	$(\Sigma_c^* \rho)^S$
	[2, 3; 2, 3; 2, 3]	$(ND^*)^H$		[1; 3; 3]	$(\Sigma_c^* \rho)^H$
$0\frac{3}{2}^{-}$	[2; 4; 1]	$(\Sigma_c^*\pi)^S$		[1; 2; 1]	$(\Sigma_c^*\omega)^S$
	[2; 4; 3]	$(\Sigma_c^*\pi)^H$		[1; 2; 3]	$(\Sigma_c^*\omega)^H$
	[4; 1; 1]	$(\Lambda_c \omega)^S$		[4, 5; 4, 5; 1]	$(ND)^S$
	[3, 4; 1; 2, 3]	$(\Lambda_c \omega)^H$		[4, 5; 4, 5; 2, 3]	$(ND)^H$
	[3; 4; 1]	$(\Sigma_c \rho)^S$		[2, 3; 4, 5; 1]	$(ND^*)^S$
	[3, 4; 4; 2, 3]	$(\Sigma_c ho)^H$		[2, 3; 4, 5; 2, 3]	$(ND^*)^H$
	[1; 4; 1]	$(\Sigma_c^* \rho)^S$		[1; 6; 1]	$(\Delta D^*)^S$
	[1; 4; 3]	$(\Sigma_c^* ho)^H$		[1; 6; 3]	$(\Delta D^*)^H$
	[3, 4; 2, 3; 1]	$(ND^*)^S$	$1\frac{3}{2}^{-}$	[2; 3; 1]	$(\Sigma_c^*\pi)^S$
	[3, 4; 2, 3; 2, 3]	$(ND^*)^H$		[2; 3; 3]	$(\Sigma_c^*\pi)^H$
$0\frac{5}{2}^{-}$	[1; 4; 1]	$(\Sigma_c^* \rho)^S$		[4; 1; 1]	$(\Lambda_c \rho)^S$
2	[1; 4; 3]	$(\Sigma_c^* \rho)^H$		[3, 4; 1; 2, 3]	$(\Lambda_c \rho)^H$
$2\frac{1}{2}^{-}$	[4; 1; 1]	$(\Sigma_c\pi)^S$		[2; 2; 1]	$(\Sigma_c^*\eta)^S$
2	[4, 5; 1; 2, 3]	$(\Sigma_c\pi)^H$		[2; 2; 3]	$(\Sigma_c^* \eta)^H$
	[2; 1; 1]	$(\Sigma_c \rho)^S$		[3; 3; 1]	$(\Sigma_c \rho)^S$
	[2, 3; 1; 2, 3]	$(\Sigma_c \rho)^H$		[3, 4; 3; 2, 3]	$(\Sigma_c \rho)^H$
	[1; 1; 1]	$(\Sigma_c^* \rho)^S$		[3; 2; 1]	$(\Sigma_c \omega)^S$
	[1; 1; 3]	$(\Sigma_c^* \rho)^H$		[3, 4; 2; 2, 3]	$(\Sigma_c \omega)^H$
	[1; 2; 1]	$(\Delta D^*)^S$		[1; 3; 1]	$(\Sigma_c^* \rho)^S$
	[1; 2; 3]	$(\Delta D^*)^H$		[1; 3; 3]	$(\Sigma_c^* \rho)^H$
$2\frac{3}{2}^{-}$	[2; 1; 1]	$(\Sigma_c^*\pi)^S$		[1; 2; 1]	$(\Sigma_c^*\omega)^S$
2	[2; 1; 3]	$(\Sigma_c^*\pi)^H$		[1; 2; 3]	$(\Sigma_c^*\omega)^H$
	[3; 1; 1]	$(\Sigma_c \rho)^S$		[3, 4; 4, 5; 1]	$(ND^*)^S$
	[3, 4; 1; 2, 3]	$(\Sigma_c ho)^H$		[3, 4; 4, 5; 2, 3]	$(ND^*)^H$
	[1; 1; 1]	$(\Sigma_c^* \rho)^S$		[2; 6; 1]	$(\Delta D)^S$
	[1; 1; 3]	$(\Sigma_c^* ho)^H$		[2; 6; 3]	$(\Delta D)^H$
	[2; 2; 1]	$(\Delta D)^S$		[1; 6; 1]	$(\Delta D^*)^S$
	[2; 2; 3]	$(\Delta D)^H$		[1; 6; 3]	$(\Delta D^*)^H$
	[1; 2; 1]	$(\Delta D^*)^S$	$1\frac{5}{2}^{-}$	[1; 3; 1]	$(\Sigma_c^* \rho)^S$
	[1; 2; 3]	$(\Delta D^*)^H$	- 2	[1; 3; 3]	$(\Sigma_c^* \rho)^H$



Eur. Phys. J. C (2021) 81:224 Page 7 of 12 224

Table 3 continued

IJ^P	[i;j;k]	Channel	IJ^P	[i;j;k]	Channel
$2\frac{5}{2}^{-}$	[1; 1; 1]	$(\Sigma_c^* ho)^S$		[1; 2; 1]	$(\Sigma_c^*\omega)^S$
	[1; 1; 3]	$(\Sigma_c^* ho)^H$		[1; 2; 3]	$(\Sigma_c^*\omega)^H$
	[1; 2; 1]	$(\Delta D^*)^S$		[1; 6; 1]	$(\Delta D^*)^S$
	[1; 2; 3]	$(\Delta D^*)^H$		[1; 6; 3]	$(\Delta D^*)^H$

Table 4 The low-lying orbital excited energies of $qq\,Q$ baryons (unit: MeV)

State	IJ^P	(l_1, l_2)	I	II	Exp. [41]
Λ_c	$0\frac{1}{2}^{-}$	(1, 0)	2667	2665	
	-	(0, 1)	2465	2456	
		Coupling	2465	2456	2592
Σ_c	$1\frac{1}{2}^{-}$	(1, 0)	2671	2669	
		(0, 1)	2629	2628	
		Coupling	2628	2628	
Σ_c^*	$1\frac{1}{2}^{-}$	(0, 1)	2633	2632	
Λ_b	$0\frac{1}{2}^{-}$	(1, 0)	6006	6012	
	_	(0, 1)	5783	5785	
		Coupling	5783	5785	5912
Σ_b	$1\frac{1}{2}^{-}$	(1, 0)	6008	6015	
		(0, 1)	5954	5963	
		Coupling	5954	5963	
Σ_b^*	$1\frac{1}{2}^{-}$	(0, 1)	5956	5965	

of energy spectrums is performed and the channel-coupling effect of different physical channels are considered. Moreover, the energy components are calculated to identify which terms in the Hamiltonian making the state to be bound, and the root-mean-square (RMS) distances between quark pairs are also calculated to unravel the structure of the state. We first investigate the $qqq\bar{q}c$ system with all possible negative-parity quantum numbers, and analyze the results in detail in the following.

 $I(J^P) = 0(\frac{1}{2}^-)$ The results of the single channel and channel coupling calculations are shown in Table 5. Two spatial structures considered are clearly marked in the first column. The second column gives the physical channels involved in the present work. The third column shows the single channel eigen-energy by solving the Schrödinger equation. The forth column refers to the theoretical value of non-interacting baryon-meson threshold. The values of binding energies $E_B = E - E_{th}(Theo.)$ are listed in the fifth column only if $E_B < 0$. In order to reduce the theoretical error that appeared in the calculation of the mesons and baryons, we shift the energy of state to $E' = E_{th}(Exp.) + E_B$ in the sixth column, where $E_{th}(Exp.)$ is the experimental value of noninteracting baryon and meson. The last

two rows are energies of the channel coupling calculation and the percentages of dominant channels. For the channel coupling calculation, the corrected energy is given as $E' = E + \sum_{i} p_i [E_{th}^i(Exp.) - E_{th}^i(Theo.)],$ where p_i is the percentage of various physical channels. One can see in Table 5 that all physical channels are unbound except the lowest channel of $\Sigma_c \pi$ in the single channel calculation, which has the binding energy of -13 MeV. Therefore, a bound state with $\Sigma_c \pi$ configuration should be considered to exist in this quantum number sector. Nevertheless, Σ_c can decay into Λ_c and π through strong interaction, so this bound state will appear as a resonance by experimental observation. After correction, the energy of $\Sigma_c \pi$ state is 2582 MeV, which is close to the $\Lambda_c(2595)$ with mass $M = 2592.25 \pm 0.28$ MeV. In fact, the channels of the system influence each other, thus it is necessary to take into account the channel coupling effect. For the channel coupling calculation, the lowest state $\Sigma_c \pi$ is pushed down about 20 MeV when coupling with other higher channels. After calculation of the composition, we find that the color singlet channel of $\Sigma_c \pi$ is the main component with the percentage of 90.6%, while the hidden color channel of $\Lambda_c \omega$ and the color singlet channel of ND are the minor components, accounting for 6.2% and 2.2%, respectively. Since the $\Lambda_c(2595)$ is located very close to the $\Sigma_c \pi$ threshold, this observation leads us naturally to consider a predominant baryon-meson structure of this lowest-lying odd parity charmed baryon. In our present calculation, we conclude that this state dominated by the $\Sigma_c \pi$ can be a candidate of the charmed baryon $\Lambda_c(2595)$. To identify which terms in the Hamiltonian making the state to be bound, the contributions from each term of Hamiltonian for the color singlet channel of $\Sigma_c \pi$, are given in Table 6. $\Sigma_c + \pi$ represents the noninteracting Σ_c baryon and π meson. The difference between the pentaquark state and two free corresponding hadrons is denoted as Δ_E , which stands for contributions of interaction between two clusters. Since identical light q quarks can be exchanged in two clusters, kinetic energy of relative motion between two clusters provides major repulsion, with the contribution about 55.1 MeV. However, considerable attraction from one-gluon-exchange and σ meson exchange can cancel out the whole repulsion, and the rest of the attraction makes two hadrons to be bound. Besides, confinement potential and π meson exchange provide a weak attraction between two clusters, while η meson exchange provides slight repulsion.



224 Page 8 of 12 Eur. Phys. J. C (2021) 81:224

Table 5 The energies of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P) = 0(\frac{1}{2}^-)$ (unit: MeV)

Structure	Channel	E	E_{th} (Theo.)	E_B	E'
$[qqc][\bar{q}q]$	$(\Sigma_c\pi)^S$	2612	2625	-13	2582
	$(\Sigma_c\pi)^H$	3273			
	$(\Lambda_c\eta)^S$	2931	2930	0	2834
	$(\Lambda_c\eta)^H$	3119			
	$(\Lambda_c \omega)^S$	3044	3043	0	3069
	$(\Lambda_c \omega)^H$	3006			
	$(\Sigma_c \rho)^S$	3264	3264	0	3230
	$(\Sigma_c \rho)^H$	3285			
	$(\Sigma_c^* \rho)^S$	3290	3290	0	3293
	$(\Sigma_c^* \rho)^H$	3262			
$[qqq][\bar{q}c]$	$(ND)^S$	2782	2782	0	2808
	$(ND)^H$	3191			
	$(ND^*)^S$	2947	2946	0	2946
	$(ND^*)^H$	3180			
Coupling		2591	2625	-34	2566
	$(\Sigma_c\pi)^S$:90	0.6%;($(\Lambda_c \omega)^H$:6.2%;	others:	3.2%

Table 6 The energy components of $\Sigma_c \pi$ state (unit: MeV)

	rest mass	kinetic	V^C	V^G
$\Sigma_c\pi$	3550.0	4136.9	-233.9	-4667.7
$\Sigma_c + \pi$	3550.0	4081.8	-232.2	-4635.0
Δ_E	0.0	55.1	-1.7	-32.7
	V^{π}	V^K	V^{η}	V^{σ}
$\Sigma_c \pi$	-279.8	0.0	214.4	-107.9
$\Sigma_c + \pi$	-278.0	0.0	212.1	-73.6
Δ_E	-1.8	0.0	2.3	-34.3

There is no contribution from the K meson exchange because no s quark involved in this system. Therefore, one-gluon-exchange and σ meson exchange contribute to the binding of the $\Sigma_c \pi$ state.

The spacial configurations of the states are determined by the dynamical calculation. The root-mean-square (RMS) distances between any two quarks for the system are calculated and shown in Table 7. We do the channel coupling calculation for two spatial structures $[qqc][\bar{q}q]$ and $[qqq][\bar{q}c]$, respectively. From the results in Table 7 we can see that: (1), for $[qqc][\bar{q}q]$, the distances between any two quarks are around 1 fm. Similar distances between any two quarks owe to action of the antisymmetry operator, which makes identical quarks exchange between two clusters. As we can't distinguish the identical quarks in two sub-clusters, the distances r_{qq} , $r_{q\bar{q}}$ and r_{qc} , is actually an average effect. The real distances among the sub-cluster are estimated to be less than 1

Table 7 The RMS distances of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P) = 0(\frac{1}{2})$ (unit: fm)

Structure	r_{qq}	$r_{qar{q}}$	r_{qc}	$r_{car{q}}$
$[qqc][\bar{q}q]$	1.2	1.1	1.0	1.2
$[qqq][ar{q}c]$	0.7	2.9	2.8	0.6
Coupling	1.1	1.0	0.9	1.0

fm, however, the distance between non-identical quarks, $r_{c\bar{q}}$, can be treated as the distance between two clusters; (2), for $[qqq][\bar{q}c]$, identical quarks are restricted in one cluster, the distances among the sub-cluster are less than 1 fm, while the distances between two clusters are about 3 fm, which indicates that the ND state should be a molecular state with large separation. The formation of this structure is related to the weak interaction between two clusters; (3), for the coupling of two spatial structures, the system will automatically select a more favorable structure, because of its lowest energy. Meanwhile, the result indicates that the influence of channel coupling will pull the two clusters closer. This feature implies that the lowest state $\Sigma_c \pi$ has a relatively compact structure.

 $I(J^P) = 0(\frac{3}{2})$ Table 8 lists the results of the single channel and channel coupling calculations. For the single channel calculation, we have found that the $\Sigma_c^* \pi$, ND^* and $\Sigma_c \rho$ states can form to be bound among all possible physical channels, and the corrected energies of these three states are 2648 MeV, 2943 MeV and 3224 MeV, respectively. For the channel coupling calculation, we obtain a lowest state of system, whose main component is the color singlet channel of $\Sigma_c^*\pi$, taking the percentage of 97.6%. This state with the energy of 2639 MeV, is not far from the mass of $\Lambda_c(2625)$ with $J^P = \frac{3}{2}$. So for this charmed baryon, besides the description of three quark baryon in an orbital excitation, pentaquark component also becomes a possibility within the quark model calculation. Especially, we shift the energy of ND^* state to 2943 MeV, which is close to the mass of $\Lambda_c(2940)$. Our results support the existence of $\Lambda_c(2940)$ as a state composed by a nucleon and D^* meson with $J^P = \frac{3}{2}^-$, as similar conclusions obtained in Ref [20–23]. Furthermore, another state $\Sigma_c \rho$ has disappeared in the channel coupling calculation, and the reason is that the channel coupling will push the higher state above the threshold. Different from the previous situation, the ND^* state of $[qqq][\bar{q}c]$ structure can be bound in the single channel calculation. We analyze its energy components and present the result in Table 9. Since the three identical quarks are restricted in the 3-quark cluster, kinetic energy of relative motion between two clusters provides less repulsion than the previous case, and contributions of confinement potential and one-gluon-exchange nearly all come from two subclusters, which shows that the benefit of confinement potential and one-gluon-exchange of forming



Eur. Phys. J. C (2021) 81:224 Page 9 of 12 224

Table 8 The energies of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P) = 0(\frac{3}{2})$ (unit: MeV)

Structure	Channel	Е	E_{th} (Theo.)	E_B	E'
$[qqc][\bar{q}q]$	$(\Sigma_c^*\pi)^S$	2641	2651	-10	2648
	$(\Sigma_c^*\pi)^H$	3293			
	$(\Lambda_c \omega)^S$	3044	3043	0	3069
	$(\Lambda_c \omega)^H$	3056			
	$(\Sigma_c \rho)^S$	3258	3264	-6	3224
	$(\Sigma_c \rho)^H$	3332			
	$(\Sigma_c^* \rho)^S$	3290	3290	0	3293
	$(\Sigma_c^* \rho)^H$	3271			
$[qqq][ar{q}c]$	$(ND^*)^S$	2943	2946	-3	2943
	$(ND^*)^H$	3193			
Coupling		2633	2651	-18	2639
	$(\Sigma_c^*\pi)^S:9^c$	7.6%;($ND^*)^S:1.2\%$; others	:1.2%

Table 9 The energy components of ND^* state (unit: MeV)

	Rest mass	Kinetic	V^C	V^G
ND^*	3550.0	1021.2	-166.6	-1097.0
$N + D^*$	3550.0	986.5	-167.2	-1096.4
Δ_E	0.0	34.7	0.6	-0.6
	V^{π}	V^K	V^{η}	V^{σ}
ND^*	-332.2	0.0	62.8	-95.1
$N + D^*$	-319.5	0.0	63.6	-71.2
Δ_E	-12.7	0.0	-0.8	-23.9

Table 10 The RMS distances of $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P)=0(\frac{3}{2}^-)$ (unit: fm)

Structure	r_{qq}	$r_{qar{q}}$	r_{qc}	$r_{c\bar{q}}$
$[qqc][\bar{q}q]$	1.4	1.3	1.1	1.4
$[qqq][ar{q}c]$	0.7	2.6	2.5	0.8
Coupling	1.4	1.3	1.1	1.3
$[qqq][\bar{q}c]$	0.7	2.6	2.5	0.8

a bound state can be neglected here. Nevertheless, both π meson exchange and σ meson exchange play an important role in binding a nucleon and D^* meson together. As one can see in Table 10, in which the RMS distances of the two structures and their coupling are calculated, similar results are obtained as before. For the $[qqq][\bar{q}c]$ structure, the distances between two hadrons are about twice as much as the $[qqc][\bar{q}q]$ structure. This motivates the possibility of finding molecular baryon-meson structure for ND^* state. When coupling two structures, the system is stable in a structure with lower energy.

 $I(J^P) = 0(\frac{5}{2}^-)$ In this case there are only two channels needed to be considered: the color singlet channel and

Table 11 The energies of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P) = 0(\frac{5}{2}^-)$ (unit: MeV)

Structure	Channel	Е	E_{th} (Theo.)	E_B	E'	
$[qqc][\bar{q}q]$	$(\Sigma_c^* \rho)^S$	3283	3290	-7	3286	
	$(\Sigma_c^* \rho)^H$	3388				
Coupling		3282	3290	-8	3285	
		$(\Sigma_c^* \rho)^S$:99.7%; $(\Sigma_c^* \rho)^H$:0.3%				

Table 12 The RMS distances of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P) = 0(\frac{5}{2})$ (unit: fm)

Structure	r_{qq}	$r_{qar{q}}$	r_{qc}	$r_{car{q}}$
$[qqc][\bar{q}q]$	2.0	2.0	1.5	2.2

the hidden color channel of $\Sigma_c^* \rho$. The results of the calculations are shown in Table 11. When taking into account only the color singlet channel of $\Sigma_c^* \rho$, the calculation shows that Σ_c^* baryon and ρ meson can be attracted together to form a slightly bound state, with the binding energy of -7 MeV. When coupling to its hidden color channel, the energy of $\Sigma_c^* \rho$ decreases just 1 MeV. This indicates that the contribution of the hidden color configuration to the bound state wave function is negligible, which only takes the percentage of 0.3%. As a consequence, we predict the existence of a high-spin state, $\Sigma_c^* \rho$, with a mass of 3285 MeV in the iso-scalar sector. Because of the instability of ρ meson, it is considered to be a wide pentaguark resonance. The RMS distances shown in Table 12 indicate that the configuration of $\Sigma_c^* \rho$ state with $J^P = \frac{5}{2}$ is different from the preliminary analysis of $\Sigma_c^{(*)}\pi$ state, quark distances are around 2 fm because of the weak binging energy. As mentioned above, the real distances among the sub-cluster should be less than 1 fm, while the distance between two clusters is about 2.2 fm. We remark herein that this characteristic could point to have a state of molecular nature.

 $I(J^P) = 1(\frac{1}{2})$ Table 13 indicates that there exist almost no bound states in all possible single channels except the weekly bound ND^* state with the binding energy of -1MeV. When doing the channel coupling calculation, the lowest state of the system, $\Lambda_c \pi$, has not been pushed down below its corresponding threshold, which indicates that $\Lambda_c \pi$ is a scattering state. Moreover, the ND^* state is pushed above its threshold through the channel coupling calculation. Therefore, we find no bound state of the system in this quantum number sector. Nevertheless, nearby the ND threshold, we find an energy of 2773 MeV. By analyzing its composition, we find that the color singlet channels of ND, $\Lambda_c \pi$ and $\Sigma_c \pi$ account for 67.6%, 18.3% and 13.2%, respectively. This implies that there is a possibility to exist the resonance of systems with large ND component. After correction, we obtain an energy of 2786 MeV, which is close to the mass



224 Page 10 of 12 Eur. Phys. J. C (2021) 81:224

Table 13 The energies of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P) = 1(\frac{1}{2}^-)$ (unit: MeV)

Structure	Channel	E	E_{th} (Theo.)	E_B	E'
$[qqc][\bar{q}q]$	$(\Lambda_c\pi)^S$	2428	2426	0	2426
	$(\Lambda_c\pi)^H$	3067			
	$(\Sigma_c\pi)^S$	2625	2625	0	2595
	$(\Sigma_c\pi)^H$	3328			
	$(\Sigma_c\eta)^S$	3130	3129	0	3003
	$(\Sigma_c \eta)^H$	3357			
	$(\Lambda_c \rho)^S$	3065	3065	0	3061
	$(\Lambda_c \rho)^H$	3042			
	$(\Sigma_c \rho)^S$	3264	3264	0	3230
	$(\Sigma_c \rho)^H$	3312			
	$(\Sigma_c \omega)^S$	3242	3242	0	3238
	$(\Sigma_c \omega)^H$	3314			
	$(\Sigma_c^* \rho)^S$	3291	3290	0	3293
	$(\Sigma_c^* \rho)^H$	3258			
	$(\Sigma_c^*\omega)^S$	3268	3268	0	3301
	$(\Sigma_c^*\omega)^H$	3284			
$[qqq][\bar{q}c]$	$(ND)^S$	2782	2782	0	2808
	$(ND)^H$	3191			
	$(ND^*)^S$	2945	2946	-1	2945
	$(ND^*)^H$	3174			
	$(\Delta D^*)^S$	3261	3260	0	3239
	$(\Delta D^*)^H$	3559			
Coupling		2428	2426	0	2426
		$(\Lambda_c\pi)$	S:100.0%		
		2773	2782	-9	2786
		$(ND)^{S}$:67.6%; $(\Lambda_{c}\pi)^{S}$:18.3%;			
		$(\Sigma_c\pi)$	S:13.2%; othe	rs:0.9%	6

Table 14 The RMS distances of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P)=1(\frac{1}{2}^-)$ (unit: fm)

		_		
Structure	r_{qq}	$r_{qar{q}}$	r_{qc}	$r_{c\bar{q}}$
$[qqc][\bar{q}q]$	4.3	4.3	3.1	5.2
$[qqq][ar{q}c]$	0.7	3.5	3.5	0.6
Coupling	4.3	4.3	3.1	5.2

of iso-vector charmed baryon $\Sigma_c(2800)$. On the other side, $\Sigma_c(2800)$ was also investigated in Refs. [25–27], with the conclusion that it can be identified with a dynamically generated resonance with a dominant ND configuration. The calculation of distances in Table 14 reveals the molecular nature of $[qqq][\bar{q}c]$ structure as before, but obviously large distances of $[qqc][\bar{q}q]$ structure indicate that the lowest state $\Lambda_c\pi$ can not form a bound state, and the coupling of two structures does not play a significant role.

Table 15 The energies of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P) = 1(\frac{5}{2}^-)$ (unit: MeV)

Structure	Channel	E	E_{th} (Theo.)	E_B	E'
$[qqc][\bar{q}q]$	$(\Sigma_c^* \rho)^S$	3290	3290	0	3293
	$(\Sigma_c^* \rho)^H$	3340			
	$(\Sigma_c^*\omega)^S$	3269	3268	0	3301
	$(\Sigma_c^*\omega)^H$	3312			
$[qqq][\bar{q}c]$	$(\Delta D^*)^S$	3259	3260	-1	3238
	$(\Delta D^*)^H$	3564			
Coupling		3252	3260	-8	3239
	$(\Delta D^*)^S$:82.3%; $(\Sigma_c^* \omega)^S$:11.3%; others:6.4%				

Table 16 The RMS distances of the $qqq\bar{q}c$ pentaquark system with quantum numbers $I(J^P)=1(\frac{5}{2}^-)$ (unit: fm)

Structure	r_{qq}	$r_{qar{q}}$	r_{qc}	$r_{car{q}}$
$[qqc][\bar{q}q]$	4.3	4.3	3.1	5.2
$[qqq][ar{q}c]$	1.2	3.4	3.3	0.9
Coupling	1.2	1.9	1.7	1.0

 $I(J^P) = 1(\frac{3}{2}^-)$ We omit the numerical results herein because that no bound states are found among all possible physical channels, and the channel coupling does not play a crucial role in the formation of bound states.

 $I(J^P) = 1(\frac{5}{2})$ As shown in Table 15, there only exists the bound state in the ΔD^* configuration among all possible single channels, with the slight binding energy of -1MeV. When coupling to other higher channels, the binding energy of ΔD^* state is deepened to -8 MeV. Besides, the component calculation indicates that the channel coupling plays an important role in forming a bound state in this case. Be similar to the case of $\Sigma_c^* \rho$ with $I(J^P) = 0(\frac{5}{2})$, the ΔD^* appears as a wide pentaquark resonance because of the instability of Δ baryon in our present study. This result is consistent with the conclusion of Refs. [20,43], in which the ΔD^* with $I(J^P) = 1(\frac{5}{2}^-)$ was considered to be an attractive state. As we can see from the Table 16, the pure ΔD^* state is a molecular state with large separation, however, the distances between two clusters are significantly pulled close because of the strong influence of structural coupling.

 $I(J^P) = 2(\frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-)$ The numerical results and the detailed discussion is omitted when isospin I=2. The reason is that we find no bound states both in the single channel calculation and the channel coupling calculation. Moreover, we are not particularly interested in states with such higher isospin.

Because of the heavy flavor symmetry, we also extend the study to the bottom case of $qqq\bar{q}b$ system, possible pentaquarks of which are listed in Table 17. In iso-scalar sector,



Eur. Phys. J. C (2021) 81:224 Page 11 of 12 224

Table 17 Possible pentaquarks of $qqq\bar{q}b$ system (unit: MeV)

$I(J^P)$	Main channel	Ε	E_{th} (Theo.)	E_B	E'
$0(\frac{1}{2}^{-})$	$\Sigma_b\pi$	5934	5964	-30	5922
$0(\frac{3}{2}^{-})$	$\Sigma_b^*\pi$	5951	5974	-23	5950
$0(\frac{5}{2}^{-})$	$\Sigma_b^* ho$	6604	6613	-9	6598
$1(\frac{5}{2}^{-})$	ΔB^*	6567	6579	-12	6545

Table 18 The RMS distances of the $qqq\bar{q}b$ pentaquark system (unit: fm)

$I(J^P)$	Main channel	r_{qq}	$r_{qar{q}}$	r_{qb}	$r_{bar{q}}$	
$0(\frac{1}{2}^{-})$	$\Sigma_b\pi$	1.2	1.1	0.9	1.1	
$0(\frac{3}{2}^{-})$	$\Sigma_b^*\pi$	1.3	1.2	1.0	1.2	
$0(\frac{5}{2}^{-})$	$\Sigma_b^* ho$	1.8	1.8	1.3	1.9	
$1(\frac{5}{2}^{-})$	ΔB^*	1.2	1.6	1.4	0.9	

we have found $\Sigma_b \pi$, $\Sigma_b^* \pi$ and $\Sigma_b^* \rho$ states, while in the isovector sector, only found the ΔB^* state. Noting that $\Sigma_b \pi$ and $\Sigma_b^* \pi$ could be the candidates of two odd parity bottomed baryons, $\Lambda_b(5912)$ and $\Lambda_b(5920)$, respectively. The RMS distances are listed in Table 18. We consider these bottomed pentaquarks are more compact than those of the charm case.

In addition, we repeat the above calculations with another set of parameters to test the parameter sensitivity of the results. We find that although the binding energy has a small change, the qualitative conclusion of the existence of pentaquarks is independent of the parameters.

4 Summary

In this work, we perform a dynamical calculation of $qqq\bar{q}Q$ (q=u or d, Q=c or b) five-quark system in the framework of the chiral quark model (ChQM) with Gaussian expansion method (GEM).

We first systematically study the system of $qqq\bar{q}c$, and then extend the calculation to the bottom case. Several charmed and bottomed pentaquarks with negative parity have been identified. Some excited charmed or bottomed baryons composed of qqQ (q=u or d, Q=c or b), have a possibility to be pentaquark states except the explanation of three-quark baryons in an orbital excitation. Our results show that: (1), $\Sigma_c\pi(IJ^P=0\frac{1}{2}^-)$ and $\Sigma_c^*\pi(IJ^P=0\frac{3}{2}^-)$ are possible resonances in our quark model calculation, and could be candidates of $\Lambda_c(2595)$ and $\Lambda_c(2625)$, respectively. Moreover, two high-spin pentaquark states, $\Sigma_c^*\rho(IJ^P=0\frac{5}{2}^-)$ and $\Delta D^*(IJ^P=1\frac{5}{2}^-)$, are found in the energy region of 3.2 \sim 3.3 GeV; (2), With extension to the bottom case,

 $\Sigma_b\pi(IJ^P=0\frac{1}{2}^-), \ \Sigma_b^*\pi(IJ^P=0\frac{3}{2}^-)$ could be candidates of $\Lambda_b(5912)$ and $\Lambda_b(5920)$, respectively. And $\Sigma_b^*\rho(IJ^P=0\frac{5}{2}^-)$ and $\Delta B^*(IJ^P=1\frac{5}{2}^-)$ are also found as resonances in the energy region of 6.5 \sim 6.6 GeV; (3), The calculation of RMS distances reveals the compact nature for $\Sigma_c^{(*)}\pi$ and $\Sigma_b^{(*)}\pi$ states, and the molecular nature for $\Sigma_c^*\rho$, $\Sigma_b^*\rho$, ΔD^* and ΔB^* states.

Finally, we hope that more efforts could be devoted to investigating these excited baryons, and the pentaquarks predicted in this work are worth searching in future experiments. In addition, it is worthwhile to mention that the P-wave baryon will mix with the S-wave pentaquark. Therefore, study of baryons within the unquenched quark model, including the high Fock components, is our future work.

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224 Page 12 of 12 Eur. Phys. J. C (2021) 81:224

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