# On the possibility to detect the Higgs decay $\boldsymbol{H} \rightarrow \boldsymbol{b} \overline{\boldsymbol{b}}$ in the associated $Z+b \bar{b}$ production at the LHC 

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#### Abstract

We investigate the possibility to detect the scalar Higgs boson decay $H \rightarrow b \bar{b}$ in the associated $Z$ and $b \bar{b}$ production at the LHC using the $k_{T}$-factorization QCD approach. Our consideration is based on the off-shell (i.e. depending on the transverse momenta of initial quarks and gluons) production amplitudes of $q^{*} \bar{q}^{*} \rightarrow Z H \rightarrow Z q^{\prime} \bar{q}^{\prime}$, $q^{*} \bar{q}^{*} \rightarrow Z q^{\prime} \bar{q}^{\prime}$, and $g^{*} g^{*} \rightarrow Z q^{\prime} \bar{q}^{\prime}$ partonic subprocesses supplemented with the Catani-Ciafoloni-FioraniMarchesini (CCFM) dynamics of parton densities in a proton. We argue that the $H \rightarrow b \bar{b}$ signal could be observed at large transverse momenta near the Higgs boson peak despite the overwhelming QCD background, and we point out the important role of angular correlations between the produced $Z$ boson and $b$-quarks.


In 2012, during the search performed by the CMS and ATLAS Collaborations at the LHC, the scalar Higgs boson $H$ with a mass $m_{H}$ near 125 GeV has been discovered [1,2], giving us the confidence in the physical picture of fundamental interactions which follows from the Standard Model Lagrangian. Some time later, the ATLAS Collaboration has reported first measurements of the Higgs boson differential cross sections in the $\gamma \gamma$ decay mode [3]. The measured cross sections were found to be a bit higher than the central next-to-next-to-leading order (NNLO) expectations [4-9] and those matched with a soft-gluon resummation carried out up to next-to-next-to-leading logarithmic accuracy (NNLL) [10, 11], although no significant deviations from the theoretical predictions are observed within the uncertainties [3]. The significant signal was detected also in channels where the Higgs boson decays into the $Z Z$ or $W W$ pairs $[12,13]$. The interaction of the Higgs particle with the massive $Z$ and $W$ bosons indicates that, as expected, it plays a role in electroweak symmetry breaking. However,

[^0]the interaction with the fermions and whether the Higgs field serves as the source of mass generation in the fermion sector still remain to be established. Since the Higgs boson with mass $m_{H} \sim 125 \mathrm{GeV}$ decays mainly into a beauty quarkantiquark pair [14], the observation and study of the $H \rightarrow b \bar{b}$ decay (which involves the direct coupling of the Higgs boson to beauty quarks) is therefore essential in determining the nature of the newly discovered boson.

The most sensitive channel for the $H \rightarrow b \bar{b}$ events at the LHC is the production of a Higgs particle in association with the $Z$ boson [15]. Despite the largest branching fraction ( $\sim 58 \%$ ), the $H \rightarrow b \bar{b}$ final state is more difficult for the experimental observation compared to the signatures provided by the diphoton or diboson decay modes due to the small signal over background ratio. One of the main backgrounds for the associated Higgs and $Z$ boson production is the associated production of $Z$ boson and two $b$-quark jets. The corresponding cross sections, calculated at the NNLO level (see [14]), are several orders of magnitude larger than the Higgs boson signal. However, recently the CMS Collaboration reported [16] an excess of events above the expected background with a local significance of 2.1 standard deviations, which is compatible with a Higgs boson mass of 125 GeV . Earlier, the CDF and D0 Collaborations at the Tevatron also reported [15] evidence for an excess of events in the $115-140 \mathrm{GeV}$ mass range, consistent with the mass of the Higgs boson observed at the LHC.

The experimental searches $[15,16]$ have stimulated us to investigate the associated Higgs (decaying into a $b \bar{b}$ pair) and $Z$ boson production as well as the corresponding main background process, the associated production of $Z$ boson and two $b$-quark jets, ${ }^{1}$ using the $k_{T}$-factorization approach of QCD [17-20]. A detailed description of this formalism can be found, for example, in the reviews in Refs. [21-23].

[^1]
(a)

(c)

(b)

(d)

Fig. 1 Examples of Feynman diagrams corresponding to $q^{*} \bar{q}^{*} \rightarrow$ $Z H \rightarrow Z b \bar{b}(\mathbf{a}), g^{*} g^{*} \rightarrow Z b \bar{b}(\mathbf{b})$ and $q^{*} \bar{q}^{*} \rightarrow Z b \bar{b}(\mathbf{c}, \mathbf{d})$ subprocesses. The full set of diagrams can be obtained by permutations of the quark, gluon, Higgs, and $Z$ boson lines

We only mention that the main part of the higher-order QCD corrections (namely, $\mathrm{NLO}+\mathrm{NNLO}+\mathrm{N}^{3} \mathrm{LO}+\cdots$ contributions, which correspond to the $\log 1 / x$ enhanced terms in perturbative series) is effectively taken into account in the $k_{T}$-factorization approach already at leading order, and it provides a solid theoretical ground for the effects of the initial parton radiation and transverse momenta of the initial quarks and gluons. Recently, the $k_{T}$-factorization QCD approach was successfully applied $[24,25]$ to describe the ATLAS data [3] on the inclusive Higgs production in the diphoton decay mode. ${ }^{2}$

Let us start from a short review of the steps of the calculation. Our consideration is based on the off-shell (depending on the transverse momenta of initial partons) partonic subprocesses:

$$
\begin{align*}
& q^{*}\left(k_{1}\right)+\bar{q}^{*}\left(k_{2}\right) \rightarrow Z+H \rightarrow Z(p)+q^{\prime}\left(p_{1}\right)+\bar{q}^{\prime}\left(p_{2}\right),  \tag{1}\\
& q^{*}\left(k_{1}\right)+\bar{q}^{*}\left(k_{2}\right) \rightarrow Z(p)+q^{\prime}\left(p_{1}\right)+\bar{q}^{\prime}\left(p_{2}\right),  \tag{2}\\
& g^{*}\left(k_{1}\right)+g^{*}\left(k_{2}\right) \rightarrow Z(p)+q^{\prime}\left(p_{1}\right)+\bar{q}^{\prime}\left(p_{2}\right), \tag{3}
\end{align*}
$$

where the four-momenta of all corresponding particles are given in the parentheses (see Fig. 1). The subprocesses (2) and (3) correspond to the main QCD background to the associated Higgs and $Z$ boson production. Note that, to calculate the production amplitudes, we apply the reggeized parton approach [26,27], which is based on the effective action formalism [28,29], currently explored at next-to-leading order

[^2][30-32], and we take into account the virtualities of both initial quarks and gluons. In this point our consideration differs from the one based on the collinear QCD factorization, where these virtualities are not taken into account. The use of effective vertices $[26,27]$ ensures the exact gauge invariance of the calculated amplitudes despite the off-shell initial partons.

The off-shell amplitude of the subprocess (1) reads

$$
\begin{align*}
\mathcal{M}_{1}= & e e_{q} \epsilon^{\mu}(p) \bar{v}_{s_{1}}\left(p_{2}\right) \Gamma_{H q \bar{q}} u_{s_{2}}\left(p_{1}\right) \\
& \times \frac{1}{\left(p_{1}+p_{2}\right)^{2}-m_{H}^{2}-i m_{H} \Gamma_{H}} \\
& \times \Gamma_{Z Z H}^{\mu \nu}\left[g^{\nu \lambda}-\frac{\left(k_{1}+k_{2}\right)^{\nu}\left(k_{1}+k_{2}\right)^{\lambda}}{m_{Z}^{2}}\right] \\
& \times \frac{1}{\hat{s}-m_{Z}^{2}-i m_{Z} \Gamma_{Z}} \bar{v}_{r_{1}}\left(x_{2} l_{2}\right) \Gamma_{q^{*} \bar{q}^{*} Z}^{\lambda} u_{r_{2}}\left(x_{1} l_{1}\right) \tag{4}
\end{align*}
$$

where $e$ and $e_{q}$ are the electron and incoming quark (fractional) electric charges, $\epsilon^{\mu}$ is the polarization 4 -vector of produced $Z$ boson, $\hat{s}=\left(k_{1}+k_{2}\right)^{2}, k_{i}=x_{i} l_{i}+k_{i T}$ (with $i=1$ or 2 ), $l_{1}$ and $l_{2}$ are the 4 -momenta of colliding protons, $x_{1}$ and $x_{2}$ are the corresponding momentum fractions and $\Gamma_{H}$ is the full decay width of the Higgs boson, $m_{Z}$ and $\Gamma_{Z}$ are the mass and full decay width of the $Z$ boson. We will take the propagators of intermediate $Z$ and Higgs bosons in the Breit-Wigner form to avoid any artificial singularities in the numerical calculations. The fermion and gauge boson to Higgs vertices are the usual
$\Gamma_{H q \bar{q}}=-\frac{e}{\sin 2 \theta_{W}} \frac{m_{q^{\prime}}}{m_{Z}}$,
$\Gamma_{Z Z H}^{\mu \nu}=\frac{e}{\sin 2 \theta_{W}} g^{\mu v} m_{Z}$,
where $m_{q^{\prime}}$ is the mass of the produced quark or antiquark, and $\theta_{W}$ is the Weinberg mixing angle. We will neglect the masses of the initial quarks compared to the masses of final state particles but keep their non-zero transverse momenta: $\mathbf{k}_{1 T}^{2}=$ $-k_{1 T}^{2} \neq 0, \mathbf{k}_{2 T}^{2}=-k_{2 T}^{2} \neq 0$. The effective vertex $\Gamma_{q^{*} \bar{q}^{*} Z}^{\mu}$, which describes the effective coupling of an off-shell quark and antiquark to the $Z$ boson, reads $[26,27]$ (see also [33])

$$
\begin{equation*}
\Gamma_{q^{*} \bar{q}^{*} Z}^{\mu}=\left[\gamma^{\mu}-\hat{k}_{1} \frac{l_{1}^{\mu}}{\left(l_{1} \cdot k_{2}\right)}-\hat{k}_{2} \frac{l_{2}^{\mu}}{\left(l_{2} \cdot k_{1}\right)}\right]\left(C_{V}^{q}-C_{A}^{q} \gamma^{5}\right) \tag{7}
\end{equation*}
$$

where $C_{V}^{q}$ and $C_{A}^{q}$ are the corresponding vector and axial coupling constants. The effective vertex $\Gamma_{q^{*} \bar{q}^{*} Z}^{\mu}$ satisfies the Ward identity $\Gamma_{q^{*} \bar{q}^{*} Z}^{\mu}\left(k_{1}+k_{2}\right)_{\mu}=0$. The off-shell amplitude of the subprocess (2) reads

$$
\begin{aligned}
\mathcal{M}_{2}= & e e_{q^{\prime}} g^{2} t^{a} \delta^{a b} t^{b} \epsilon^{\mu}(p) \bar{v}_{s_{1}}\left(p_{2}\right) F_{1}^{\mu v} u_{s_{2}}\left(p_{1}\right) \\
& \times \frac{g^{\nu \lambda}}{\left(k_{1}+k_{2}\right)^{2}} \bar{v}_{r_{1}}\left(x_{2} l_{2}\right) \Gamma_{q^{*} \bar{q}^{*} g}^{\lambda} u_{r_{2}}\left(x_{1} l_{1}\right)
\end{aligned}
$$

$$
\begin{align*}
& +e e_{q} g^{2} t^{a} \delta^{a b} t^{b} \epsilon^{\mu}(p) \bar{v}_{s_{1}}\left(p_{2}\right) F_{2}^{\mu \lambda} u_{s_{2}}\left(p_{1}\right) \\
& \times \frac{g^{\nu \lambda}}{\left(p_{1}+k_{2}\right)^{2}} \bar{v}_{r_{1}}\left(x_{2} l_{2}\right) \gamma^{\nu} u_{r_{2}}\left(x_{1} l_{1}\right) \tag{8}
\end{align*}
$$

where $e_{q^{\prime}}$ is the produced quark (fractional) electric charge, $g$ is the strong charge, $a$ and $b$ are the eight-fold color indices, and

$$
\begin{align*}
F_{1}^{\mu \nu}= & \Gamma_{q q Z}^{\mu} \frac{\hat{p}+\hat{p}_{1}+m_{q^{\prime}}}{\left(p+p_{1}\right)^{2}-m_{q^{\prime}}^{2}} \gamma^{\nu} \\
& +\gamma^{\nu} \frac{-\hat{p}-\hat{p}_{2}+m_{q^{\prime}}}{\left(-p-p_{2}\right)^{2}-m_{q^{\prime}}^{2}} \Gamma_{q q Z}^{\mu},  \tag{9}\\
F_{2}^{\mu \lambda}= & \Gamma_{q^{*} q g}^{(+) \lambda}\left(k_{2}, p_{1}+p_{2}\right) \frac{\hat{k}_{1}-\hat{p}}{\left(k_{1}-p\right)^{2}} \Gamma_{q^{*} q Z}^{(-) \mu}\left(k_{1}, p\right) \\
& +\Gamma_{q^{*} q Z}^{(+) \mu}\left(k_{2}, p\right) \frac{-\hat{k}_{2}-\hat{p}}{\left(-k_{2}-p\right)^{2}} \Gamma_{q^{*} q g}^{(-) \lambda}\left(k_{1}, p_{1}+p_{2}\right) \\
& +\Delta^{\mu \lambda}\left(k_{1},-k_{2}, p, p_{1}+p_{2}\right) . \tag{10}
\end{align*}
$$

The on-shell quark coupling to the $Z$ boson is taken in a standard form:
$\Gamma_{q q Z}^{\mu}=\gamma^{\mu}\left(C_{V}^{q}-C_{A}^{q} \gamma^{5}\right)$.
The effective vertices can be written as $[26,27]$
$\Gamma_{q^{*} \dot{q}^{*} g}^{\mu}=\gamma^{\mu}-\hat{k}_{1} \frac{l_{1}^{\mu}}{\left(l_{1} \cdot k_{2}\right)}-\hat{k}_{2} \frac{l_{2}^{\mu}}{\left(l_{2} \cdot k_{1}\right)}$,
$\Gamma_{q^{*} q g}^{(+) \mu}(k, q)=\gamma^{\mu}-\hat{k} \frac{l_{1}^{\mu}}{\left(l_{1} \cdot q\right)}$,
$\Gamma_{q^{*} q g}^{(-) \mu}(k, q)=\gamma^{\mu}-\hat{k} \frac{l_{2}^{\mu}}{\left(l_{2} \cdot q\right)}$.
The corresponding couplings of the off-shell quark or antiquark to the usual on-shell quark and $Z$ boson are constructed as was done earlier [33]:
$\Gamma_{q^{*} q Z}^{( \pm) \mu}(k, q)=\Gamma_{q^{*} q g}^{( \pm) \mu}(k, q)\left(C_{V}^{q}-C_{A}^{q} \gamma^{5}\right)$.
The induced term $\Delta^{\mu \nu}\left(k_{1}, k_{2}, q_{1}, q_{2}\right)$ has the form [34]

$$
\begin{align*}
\Delta^{\mu \nu}\left(k_{1}, k_{2}, q_{1}, q_{2}\right)= & \hat{k}_{1} \frac{l_{1}^{\mu} l_{1}^{\nu}}{\left(q_{1} \cdot l_{1}\right)\left(q_{2} \cdot l_{1}\right)} \\
& +\hat{k}_{2} \frac{l_{2}^{\mu} l_{2}^{v}}{\left(q_{1} \cdot l_{2}\right)\left(q_{2} \cdot l_{2}\right)} . \tag{16}
\end{align*}
$$

The summation on the produced $Z$ boson polarizations is carried out with the usual covariant formula:

$$
\begin{equation*}
\sum \epsilon^{\mu}(p) \epsilon^{* \nu}(p)=-g^{\mu \nu}+\frac{p^{\mu} p^{\nu}}{m_{Z}^{2}} \tag{17}
\end{equation*}
$$

In according to the $k_{T}$-factorization prescription [17-20], the summation over the polarizations of the incoming offshell gluons is carried out with $\sum \epsilon^{\mu} \epsilon^{* \nu}=\mathbf{k}_{T}^{\mu} \mathbf{k}_{T}^{\nu} / \mathbf{k}_{T}^{2}$. In the collinear limit, when $\left|\mathbf{k}_{T}\right| \rightarrow 0$, this expression converges to the ordinary one after averaging on the azimuthal angle. According to the use of the effective vertices, the spin density matrix for off-shell spinors in the initial state is taken in the usual form $\sum u\left(x_{i} l_{i}\right) \bar{u}\left(x_{i} l_{i}\right)=x_{i} \hat{l}_{i}+m$ (where $i=1$ or 2 , and we omitted the spinor indices). Further calculations are straightforward and in other respects follow the standard QCD Feynman rules. The evaluation of the traces was performed using the algebraic manipulation system FORM [35]. We do not list here the obtained lengthy expressions because of lack of space. The off-shell amplitude of the gluon-gluon fusion subprocess (3) was derived in our previous paper [36] (see also [37]).

The cross section of any process in the $k_{T}$-factorization approach is calculated as a convolution of the off-shell partonic cross section and the unintegrated, or transverse momentum dependent (TMD), parton densities in a proton. The cross sections of the subprocesses (1) and (2) read

$$
\begin{align*}
\sigma= & \sum_{q} \int \frac{1}{256 \pi^{3}\left(x_{1} x_{2} s\right)^{2}}\left|\overline{\mathcal{M}}_{1,2}\right|^{2} \\
& \times f_{q}\left(x_{1}, \mathbf{k}_{1 T}^{2}, \mu^{2}\right) f_{q}\left(x_{2}, \mathbf{k}_{2 T}^{2}, \mu^{2}\right) \\
& \times \mathrm{d} \mathbf{k}_{1 T}^{2} \mathrm{~d} \mathbf{k}_{2 T}^{2} \mathrm{~d} \mathbf{p}_{1 T}^{2} \mathbf{p}_{2 T}^{2} \mathrm{~d} y \mathrm{~d} y_{1} \mathrm{~d} y_{2} \\
& \times \frac{\mathrm{d} \phi_{1}}{2 \pi} \frac{\mathrm{~d} \phi_{2}}{2 \pi} \frac{\mathrm{~d} \psi_{1}}{2 \pi} \frac{\mathrm{~d} \psi_{2}}{2 \pi} \tag{18}
\end{align*}
$$

where $f_{q}\left(x_{i}, \mathbf{k}_{i T}^{2}, \mu^{2}\right)$ is the TMD quark density in a proton, $y$ is the rapidity of the produced $Z$ boson, $s$ is the total energy, $\mathbf{p}_{1 T}, \mathbf{p}_{2 T}, y_{1}, y_{2}, \psi_{1}$, and $\psi_{2}$ are the transverse momenta, rapidities, and azimuthal angles of the final state quarks, respectively. The incoming quarks have azimuthal angles $\phi_{1}$ and $\phi_{2}$. The cross sections of the subprocess (3) can be written as

$$
\begin{align*}
\sigma= & \int \frac{1}{256 \pi^{3}\left(x_{1} x_{2} s\right)^{2}}\left|\overline{\mathcal{M}}_{3}\right|^{2} \\
& \times f_{g}\left(x_{1}, \mathbf{k}_{1 T}^{2}, \mu^{2}\right) f_{g}\left(x_{2}, \mathbf{k}_{2 T}^{2}, \mu^{2}\right) \mathrm{d} \mathbf{k}_{1 T}^{2} \mathrm{~d} \mathbf{k}_{2 T}^{2} \\
& \times \mathrm{d} \mathbf{p}_{1 T}^{2} \mathbf{p}_{2 T}^{2} \mathrm{~d} y \mathrm{~d} y_{1} \mathrm{~d} y_{2} \\
& \times \frac{\mathrm{d} \phi_{1}}{2 \pi} \frac{\mathrm{~d} \phi_{2}}{2 \pi} \frac{\mathrm{~d} \psi_{1}}{2 \pi} \frac{\mathrm{~d} \psi_{2}}{2 \pi}, \tag{19}
\end{align*}
$$

where $f_{g}\left(x_{i}, \mathbf{k}_{i T}^{2}, \mu^{2}\right)$ is the TMD gluon density in a proton, and $\mathcal{M}_{3}$ is the off-shell amplitude of the subprocess (3).

Concerning the TMD parton densities in a proton, we concentrate on the approach based on the CCFM evolution equation [38-41]. The CCFM parton shower, based on the principle of color coherence, describes only the emission of gluons, while real quark emissions are left aside. It implies that the CCFM equation describes only the distinct evolution of


Fig. 2 The associated $Z+b \bar{b}$ cross sections in $p p$ collisions calculated as a function of invariant mass of $b \bar{b}$ quarks at $\sqrt{s}=8 \mathrm{TeV}$ (left panel) and $\sqrt{s}=14 \mathrm{TeV}$ (right panel). The solid, dashed

and dash-dotted histograms correspond to the contributions from the $q^{*} \bar{q}^{*} \rightarrow Z H \rightarrow Z b \bar{b}, q^{*} \bar{q}^{*} \rightarrow Z b \bar{b}$, and $g^{*} g^{*} \rightarrow Z b \bar{b}$ subprocesses, respectively. No cuts are applied
splitting function at lowest order for $\left|\mathbf{q}_{T}\right| \rightarrow 0$. The scale $\bar{\mu}^{2}$ is defined [48] from the angular ordering condition, which is natural from the point of view of the CCFM evolution: $\bar{\mu}^{2}=\Delta^{2} /(1-z)^{2}+\mathbf{q}_{T}^{2} /(1-z)$.

Other essential parameters were taken as follows: renormalization scale $\mu_{R}^{2}=m_{Z}^{2}+p_{T}^{2}$, factorization scale $\mu_{F}^{2}=$ $\hat{s}+\mathbf{Q}_{T}^{2}$ (with $\mathbf{Q}_{T}$ being the transverse momentum of initial parton pair), beauty quark mass $m_{b}=4.75 \mathrm{GeV}$, $m_{Z}=91.1876 \mathrm{GeV}, m_{H}=125 \mathrm{GeV}, \Gamma_{Z}=2.4952 \mathrm{GeV}$, $\Gamma_{H}=4.3 \mathrm{MeV}, \sin ^{2} \theta_{W}=0.23122$, and we use the LO formula for the strong coupling constant $\alpha_{s}\left(\mu^{2}\right)$ with $n_{f}=4$ active quark flavors at $\Lambda_{\mathrm{QCD}}=200 \mathrm{MeV}$, so that $\alpha_{s}\left(m_{Z}^{2}\right)=0.1232$. To take into account the non-logarithmic loop corrections to the production cross sections, we apply the effective $K$-factor, as was done in [49-51]:
$K=\exp \left[C_{F} \frac{\alpha_{S}\left(\mu^{2}\right)}{2 \pi} \pi^{2}\right]$,
where the color factor $C_{F}=4 / 3$. A particular choice of the scale, $\mu^{2}=p_{T}^{4 / 3} m_{Z}^{2 / 3}$, was proposed [49-51] to eliminate sub-leading logarithmic terms. Note that we choose this scale to evaluate the strong coupling constant in (22) only. Everywhere the multidimensional integration has been performed by means of the Monte Carlo technique, using the routine VEGAS [52]. The corresponding C++ code is available from the authors on request.

We now are in a position to present our numerical predictions. The differential cross sections of the associated $Z b \bar{b}$ production in $p p$ collisions as a function of $M$, the invariant mass of the final beauty quarks, and $Z$ boson transverse momentum at $\sqrt{s}=8$ and 14 TeV are shown in Figs. 2 and 3 . The solid, dashed, and dash-dotted histograms correspond to the contributions from the subprocesses (1), (2), and (3),


Fig. 3 The associated $Z+b \bar{b}$ cross sections in $p p$ collisions calculated as a function of $Z$ boson transverse momentum at $\sqrt{s}=8 \mathrm{TeV}$ (left panel) and $\sqrt{s}=14 \mathrm{TeV}$ (right panel). The notation of all histograms is the same as in Fig. 2. No cuts are applied


Fig. 4 The associated $Z+b \bar{b}$ cross sections in $p p$ collisions calculated as a function of $Z$ boson transverse momentum at $\sqrt{s}=8 \mathrm{TeV}$ (left panel) and $\sqrt{s}=14 \mathrm{TeV}$ (right panel) at $120<M<130 \mathrm{GeV}$. The notation of all histograms is the same as in Fig. 2


Fig. 5 The associated $Z+b \bar{b}$ cross sections in $p p$ collisions calculated as a function of angle $\theta$ between the produced $Z$ boson and beauty quark in the Collins-Soper frame at $\sqrt{s}=8 \mathrm{TeV}$ (left panel) and

$\sqrt{s}=14 \mathrm{TeV}$ (right panel) at $120<M<130 \mathrm{GeV}$. An additional cut $p_{T}>200(300) \mathrm{GeV}$ is applied for $\sqrt{s}=8(14) \mathrm{TeV}$. The notation of all histograms is the same as in Fig. 2


Fig. 6 The associated $Z+b \bar{b}$ cross sections in $p p$ collisions calculated as a function of azimuthal angle difference $\Delta \phi$ between the produced beauty quarks in the $p p$ center-of-mass frame at $\sqrt{s}=8 \mathrm{TeV}$ (left

panel) and $\sqrt{s}=14 \mathrm{TeV}$ (right panel) at $120<M<130 \mathrm{GeV}$. An additional cut $p_{T}>200(300) \mathrm{GeV}$ is applied for $\sqrt{s}=8(14) \mathrm{TeV}$. The notation of all histograms is the same as in Fig. 2
lar distributions predicted by the off-shell amplitudes of the subprocesses (2) and (3). Moreover, the beauty quarks, originating from the Higgs boson decay, populate mostly low $\Delta \phi$ (see Fig. 6), whereas the leading QCD background, as given by the gluon-gluon fusion subprocess (3), has a flatter $\Delta \phi$ distribution. So, the different angular correlations between the final state particles in the associated $Z b \bar{b}$ production are very sensitive to the source of the $b \bar{b}$ pairs, and therefore future experimental investigations of such observables at the LHC with increased luminosity can give clear information as regards the Higgs signal.

Finally, we study the size of the theoretical uncertainties of our calculations connected with the hard scale. As usual, in order to estimate these uncertainties we vary the scales by a factor of 2 around their default values. Also, we use the CCFM set $\mathrm{A} 0+$ and A 0 - instead of the default TMD gluon density A0. These two PDF sets represent a variation of the hard scale involved in (18) and (19). The A0+ stands for a variation of $2 \mu$, while set $\mathrm{A} 0-$ reflects $\mu / 2$. We observe a deviation of about $50 \%$ with both $\mathrm{A} 0+$ and $\mathrm{A} 0-$ sets (see Fig. 7) for the QCD background (as given by the sum of gluon-gluon fusion and quark-antiquark annihilation subprocesses considered above). Despite the relatively large band of uncertainties, this does not change our conclusions. Additionally, to investigate the role of higher-order QCD corrections, in Fig. 7 we present the results for the QCD background obtained in the framework of collinear QCD factorization at LO. We find that in the kinematical region where the possible Higgs signal could be observed these corrections are important.

To conclude, in the present note we applied the $k_{T}$ factorization approach of QCD to study the possibility to detect the scalar Higgs boson decay $H \rightarrow b \bar{b}$ in the associated $Z$ and $b \bar{b}$ production at the LHC. Our considera-





Fig. 7 The associated $Z+b \bar{b}$ cross sections in $p p$ collisions calculated as a function of $Z$ boson transverse momentum $p_{T}$, angle $\theta$, and azimuthal angle difference $\Delta \phi$ at $\sqrt{s}=8 \mathrm{TeV}$ (left panel) and $\sqrt{s}=14 \mathrm{TeV}$ (right panel) at $120<M<130 \mathrm{GeV}$. The solid and dash-dotted histograms correspond to the QCD background (sum of the gluon-gluon fusion and quark-antiquark annihilation subprocesses) calculated in the framework of the $k_{T}$-factorization approach
tion was based on the off-shell production amplitudes of $q^{*} \bar{q}^{*} \rightarrow Z H \rightarrow Z q^{\prime} \bar{q}^{\prime}, q^{*} \bar{q}^{*} \rightarrow Z q^{\prime} \bar{q}^{\prime}$, and $g^{*} g^{*} \rightarrow Z q^{\prime} \bar{q}^{\prime}$ partonic subprocesses supplemented with the CCFM dynam-

and collinear approximation of QCD at LO, respectively. The upper and lower dashed histograms correspond to the scale variations in the $k_{T^{-}}$ factorization predictions, as described in the text. The dotted histograms correspond to the contributions from the $q^{*} \bar{q}^{*} \rightarrow Z H \rightarrow Z b \bar{b}$ subprocess. An additional cut $p_{T}>200(300) \mathrm{GeV}$ is applied for $\sqrt{s}=8$ (14) TeV in the $\theta$ and $\Delta \phi$ distributions
ics of parton densities in a proton. The main part of the higher-order QCD corrections (corresponding to the $\log 1 / x$ enhanced terms in a perturbative series) is effectively taken
into account in our consideration. We demonstrated that the $H \rightarrow b \bar{b}$ signal can be observed at large transverse momenta near the Higgs boson peak despite the overwhelming QCD background, and we pointed out the important role of the angular correlations between the produced $Z$ boson and $b$-quarks. The gauge invariant off-shell amplitudes of $q^{*} \bar{q}^{*} \rightarrow Z H \rightarrow Z q^{\prime} \bar{q}^{\prime}$ and $q^{*} \bar{q}^{*} \rightarrow Z q^{\prime} \bar{q}^{\prime}$ partonic subprocesses, calculated for the first time, can be implemented in different Monte Carlo event generators, like, for example, CASCADE [53,54].

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[^1]:    ${ }^{1}$ Other background processes, like the $t \bar{t}$ pair, diboson or QCD multijet production are beyond our present consideration.

[^2]:    ${ }^{2}$ In our opinion, the results [25] suffer from the problem of double counting and contain the wrong numerical factor.

