

## Measurements of charged kaon semileptonic decay branching fractions $K^\pm \rightarrow \pi^0 \mu^\pm \nu$ and $K^\pm \rightarrow \pi^0 e^\pm \nu$ and their ratio

The NA48/2 Collaboration

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**Abstract.** In an earlier paper [1], the background for  $K_{e3}$  was over estimated due to an erroneous calculation of the electron identification efficiency. The correct ratios of the partial widths involving this channel are  $\mathcal{R}_{K_{e3}/K2\pi} = 0.2470 \pm 0.0009$  (stat)  $\pm 0.0004$  (syst) and  $\mathcal{R}_{K\mu3/K_{e3}} = 0.663 \pm 0.003$  (stat)  $\pm 0.001$  (syst). Assuming the PDG value [2] for the  $K_{2\pi}$  branching ratio, the measured branching fraction of  $\text{Br}(K_{e3})$  continues to exceed the current PDG value [2]. The extracted value of  $|V_{us}|f_+(0)$  is in agreement with the CKM unitary prediction; thus, our conclusions in [1] do not change.

### Erratum to:

Eur. Phys. J. C 50, 329–340 (2007)  
DOI 10.1140/epjc/s10052-007-0253-3

In the analysis of charged kaon semileptonic decays presented in an earlier paper [1], the background for  $K_{e3}$  was unfortunately overestimated due to an erroneous calculation of the electron identification efficiency. The average electron identification efficiency is corrected to be  $(98.59 \pm 0.09)\%$ , see Fig. 4a, and this is the only input into the calculation that has been modified. Table 1 lists the corresponding quantities needed to evaluate the branching fractions, and Table 2 lists the expected background, based on the corrected electron identification efficiency.

The updated results of Table 4 in [1] for  $\mathcal{R}_{K_{e3}/K2\pi}$  and  $\mathcal{R}_{K\mu3/K_{e3}}$  are

$$\begin{aligned}\mathcal{R}_{K_{e3}/K2\pi} &= 0.2476 \pm 0.0011 \text{ (stat)} \pm 0.0005 \text{ (syst)} & [K^+], \\ \mathcal{R}_{K_{e3}/K2\pi} &= 0.2460 \pm 0.0015 \text{ (stat)} \pm 0.0006 \text{ (syst)} & [K^-], \\ \mathcal{R}_{K\mu3/K_{e3}} &= 0.6605 \pm 0.0040 \text{ (stat)} \pm 0.0017 \text{ (syst)} & [K^+]\end{aligned}$$

and

$$\mathcal{R}_{K\mu3/K_{e3}} = 0.6661 \pm 0.0055 \text{ (stat)} \pm 0.0019 \text{ (syst)} \quad [K^-].$$

The results for  $K^+$  and  $K^-$  combined are

$$\mathcal{R}_{K_{e3}/K2\pi} = 0.2470 \pm 0.0009 \text{ (stat)} \pm 0.0004 \text{ (syst)}$$

and

$$\mathcal{R}_{K\mu3/K_{e3}} = 0.663 \pm 0.003 \text{ (stat)} \pm 0.001 \text{ (syst)},$$

and they are shown in Figs. 8 and 9, respectively. The result for  $\mathcal{R}_{K\mu3/K2\pi}$  remains unchanged [1].

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The online version of the original article can be found at  
<http://dx.doi.org/10.1140/epjc/s10052-007-0253-3>.

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<sup>b</sup> Funded by the U.K. Particle Physics and Astronomy Research Council

<sup>c</sup> Funded by the German Federal Minister for Education and research under contract 05HK1UM1/1

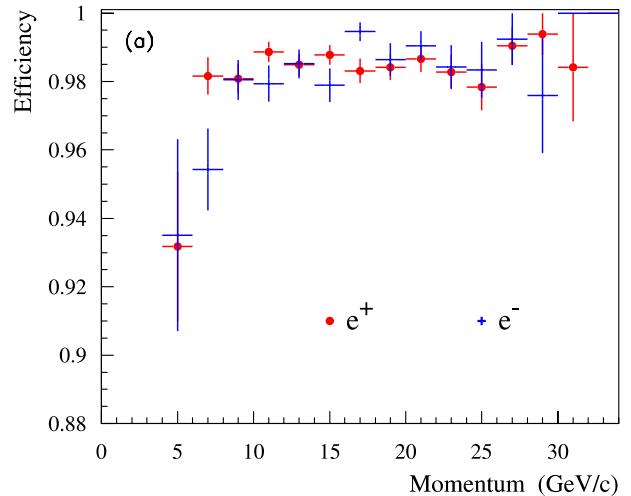
<sup>d</sup> Funded by the German Federal Minister for Research and Technology (BMBF) under contract 056SI74

<sup>e</sup> Funded by the Austrian Ministry for Traffic and Research under the contract GZ 616.360/2-IV GZ 616.363/2-VIII, and by the Fonds für Wissenschaft und Forschung FWF Nr. P08929-PHY

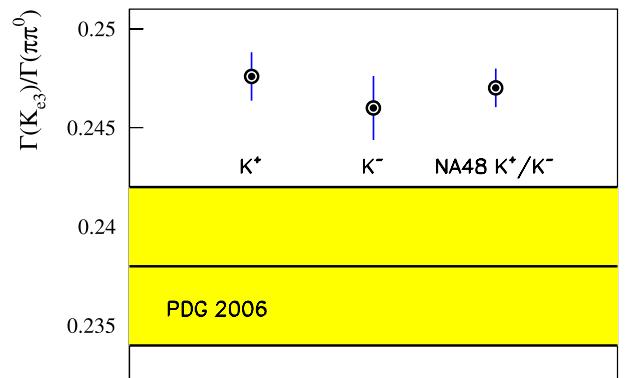
Taking the current PDG value for the  $K_{2\pi}$  branching fraction [2], the branching fraction for  $K_{e3}$  is found to be  $\text{Br}(K_{e3}) = 0.05168 \pm 0.00019$  (stat)  $\pm 0.00008$  (syst)  $\pm 0.00030$  (norm). Using this branching fraction and the input values listed in [1], the  $|V_{us}|$  matrix element times the vector form factor  $f_+(0)$  is found to be

$$\begin{aligned}|V_{us}|f_+(0) &= 0.2193 \pm 0.0012 \quad [K_{e3}] \\ &= 0.21928 \pm 0.00039 \text{ (stat)} \pm 0.00017 \text{ (syst)} \\ &\quad \pm 0.00062 \text{ (norm)} \pm 0.00096 \text{ (ext)}.\end{aligned}\quad (1)$$

Combining this  $|V_{us}|f_+(0)$  value for  $K_{e3}$  with the corresponding value for  $K_{\mu3}$  in [1] and shown in Fig. 10, we



**Fig. 4. a** The  $E/\text{pc}$  particle identification efficiency for electrons from clean subsamples of  $K_{e3}$  decays



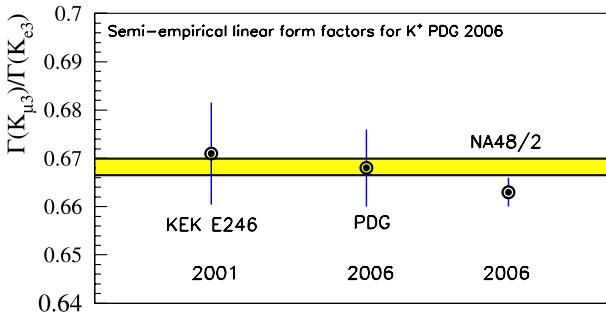
**Fig. 8.**  $\mathcal{R}_{K_{e3}/K2\pi}$  result compared to the corresponding PDG value [2]. The  $\mathcal{R}_{K\mu3/K2\pi}$  result is unchanged and shown in Fig. 8 of [1]

**Table 1.** Updated information used to extract the branching ratio, where track =  $e^\pm, \pi^\pm$  for  $i = K_{e3}^\pm, K_{2\pi}^\pm$

Decay type	Raw number of events ( $N_i$ )	Acceptance × particle ID ( $\text{Acc}_i \times \epsilon_{\text{track}_{i\text{ID}}}$ )	Backgrounds/signal ( $\Delta_i$ )	Trigger efficiency ( $\text{Trig}_i$ )
$K_{e3}^+$	56.196	$0.0698 \pm 0.0001$	$(0.0200 \pm 0.0008)\%$	$0.9990 \pm 0.0005$
$K_{e3}^-$	30.898	$0.0694 \pm 0.0001$	$(0.0209 \pm 0.0010)\%$	$0.9982 \pm 0.0008$
$K_{2\pi}^+$	461.837	$0.1418 \pm 0.0001$	$(0.2893 \pm 0.0058)\%$	$0.9987 \pm 0.0002$
$K_{2\pi}^-$	256.619	$0.1412 \pm 0.0001$	$(0.2896 \pm 0.0058)\%$	$0.9990 \pm 0.0002$

**Table 2.** Recalculated percentage of expected background from Monte Carlo simulation for  $K_{e3}$  and  $K_{2\pi}$  from the main contributors to their total background

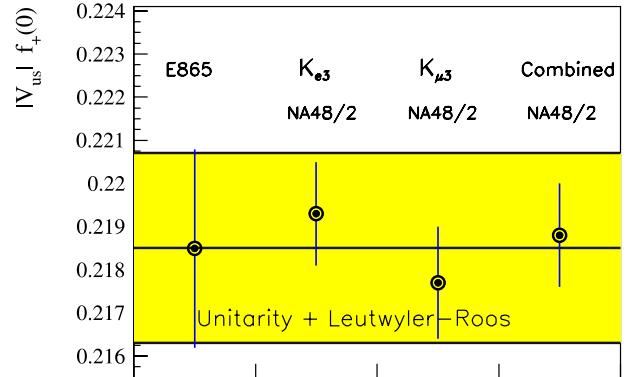
Contributing channel	$K^+$	$K^-$
$K_{e3}$		
$K_{\pi^\pm \pi^0 \pi^0}$	$(0.0130 \pm 0.0007)\%$	$(0.0139 \pm 0.0009)\%$
$K_{2\pi}$	$(0.0070 \pm 0.0003)\%$	$(0.0071 \pm 0.0004)\%$
$K_{2\pi}$		
$K_{\mu 3}$	$(0.2848 \pm 0.0058)\%$	$(0.2846 \pm 0.0058)\%$
$K_{e3}$	$(0.0045 \pm 0.0006)\%$	$(0.0050 \pm 0.0008)\%$



**Fig. 9.**  $\mathcal{R}_{K\mu 3/Ke3}$  results compared to KEK-246 results [4], the corresponding PDG value of 2006 [2] and to the predictions assuming  $\mu-e$  universality, (6) in [1], with the  $\lambda_+$  and  $\lambda_0$  values given for  $K^\pm$  in the PDG of 2006 [2]

obtain

$$|V_{us}|f_+(0) = 0.2188 \pm 0.0012, \quad (2)$$



**Fig. 10.** Comparison of the NA48 measurement of  $|V_{us}|f_+(0)$  from  $K_{e3}$  data in (1) and from  $K_{\mu 3}$  data in [1], and the  $K_{e3}$  BNL-E865 result [3]. The theoretical prediction shown is obtained assuming unitarity of the CKM matrix and using the values for  $V_{ud}$  and  $V_{ub}$  as input and the choice of  $f_+(0)$  all as described in [1]

$$|V_{us}| = 0.2277 \pm 0.0013 \text{ (other)} \pm 0.0019 \text{ (theo)}, \quad (3)$$

which is consistent with the unitarity prediction as calculated in [1], namely,  $|V_{us}|_{\text{unitary}} = 0.2274 \pm 0.0013$ .

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