### Silicide Nanopowders as Low-Cost and High-Performance Thermoelectric Materials

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Thermoelectric devices directly convert heat into electricity and are very attractive for waste heat recovery and solar energy utilization. If thermoelectric devices can be made sufficiently efficient and inexpensive, then they will become a transformative energy technology that can tap a significant portion (10–20%) of the vast amount of heat existing in nature as well as industrial processes. Nanopowders of Earth-abundant, silicide-based materials, such as Mg<sub>2</sub>Si and its alloys, provide a unique opportunity to realize this goal. This article will present an overview of recent advances in the synthesis and thermoelectric properties of silicide-based nanostructured materials.

#### INTRODUCTION

Thermal energy plays a very significant role in energy conversion: More than 80% of the world's electrical power is from heat engines (mostly by burning fossil fuels) and more than 60% of energy is used in heating and cooling. When the heat source temperature is high and the heat flux is large (such as heat from the sun¹ and car exhaust²), it is extremely desirable to generate electricity from these heat sources as one of the new forms of carbon-free energy. In this respect, thermoelectric (TE) energy conversion has attracted an increasing amount of attention recently³,⁴ due to its potential applications for direct heat to electricity energy conversion for solar energy utilization¹ and waste heat recovery.⁵

A typical thermoelectric generator (TEG) for direct heat to electricity conversion is shown in Fig. 1a, where *n*- and *p*-type semiconductor elements are connected in series electrically and in parallel thermally. As the heat is absorbed from the top plate, electrons and holes flow from the hot to the cold sides, thereby creating a continuous electrical current flow through an external load. In essence, the TEG works as a traditional thermodynamic heat engine (such as a Rankine cycle), but it uses electrons and holes as the working fluids rather than fluidic molecules. As such, the TEGs are purely solid-state heat engines and have no moving parts, so they are extremely compact and reliable. These features are attractive for the waste heat

recovery scenarios where the extracted electrical power is relatively small compared to a primary power plant.

Despite the attractive potential of TEGs for increasing energy efficiency via waste heat harvesting in various scenarios, the current applications of TEGs are still very limited. This limitation is primarily due to the low efficiency and high cost of the current TE materials. Therefore, it is extremely important to develop efficient and inexpensive thermoelectric materials that would enable the widespread use of TEGs.

The efficiency of the TEGs  $\eta$  is determined by the TE figure of merit referred to as ZT, defined as follows<sup>6</sup>:

$$ZT = S^2 \sigma T / \kappa \tag{1}$$

where S is the Seebeck coefficient,  $\sigma$  is electrical conductivity, T is the absolute temperature, and  $\kappa$  is the total thermal conductivity that contains both the lattice ( $\kappa_{\rm L}$ ) and electronic ( $\kappa_{\rm e}$ ) components. The maximum efficiency of a TEG in power generation is given by the following relationship:

$$\eta_{\mathrm{max}} = \left[ \frac{T_{\mathrm{h}} - T_{\mathrm{c}}}{T_{\mathrm{h}}} \right] \left[ \frac{\sqrt{1 + Z\bar{T}} - 1}{\sqrt{1 + Z\bar{T}} + T_{\mathrm{c}}/T_{\mathrm{h}}} \right]$$
 (2)

where  $T_{\rm h}$  and  $T_{\rm c}$  are the temperatures of the hot and the cool sides respectively, and  $\bar{T}$  is the average of  $T_{\rm h}$  and  $T_{\rm c}$ . The first part of Eq. 2 shows that the maximum efficiency is associated with the temper-

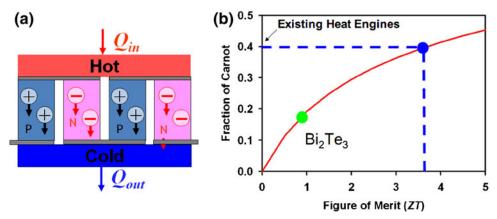


Fig. 1. (a) Schematic of a thermoelectric device that generates electricity from heat current. (b) Maximum efficiency of a thermoelectric device versus the figure of merit (ZT).

ature difference, as dictated by the Carnot efficiency. The relationship between the efficiency  $\eta$  and ZT is depicted in Fig. 1b.

It is apparent that the figure of merit ZT of TE materials directly determines the efficiency of TE devices made from the materials. Enhancing ZT requires concerted engineering efforts to optimize S,  $\sigma$ , and  $\kappa$ , which contains the electronic ( $\kappa_e$ ) and the lattice or phonons ( $\kappa_L$ ) components. In conventional bulk semiconductor materials, the parameters S,  $\sigma$ , and  $\kappa_e$  are often interdependent, which makes it very challenging to independently control these quantities. For example, an increase in S in bulk materials generally results in a simultaneous decrease in  $\sigma$ ; also, an increase in  $\sigma$  leads to a comparable increase in electronic contribution to the thermal conductivity  $(\kappa_e)$ . As a result, for more than five decades, Bi-Sb-Te-, Pb-Te-, and Si-Gebased alloys have been the primary TE materials with peak ZT around the unity for low, intermediate, and high temperature ranges, respectively,6 due to their relatively high power factor  $(S^2\sigma)$  and low lattice  $\kappa_{\rm L}$ .

Additionally, one also needs to consider other factors when using thermoelectric materials for large-scale applications, such as materials abundance, cost, toxicity, and stability at high temperatures.

## ENHANCED ZT BY NANOSTRUCTURING APPROACHES

During the last decade, the field of thermoelectrics has progressed enormously as evidenced by numerous reports showing enhanced ZT in nanostructured materials such as superlattices of  ${\rm Bi_2Te_3/Sb_2Te_3}$  (Ref. 8) and PbSeTe/PbTe (Ref. 9), nanowires,  $^{10,11}$  and in new bulk materials with complex structures such as silver antimony lead telluride (LAST) and skutterudites.  $^{14}$ 

The enhanced *ZT* values in these nanostructured and/or complex-structured materials are attributed

to reduced lattice thermal conductivity caused by phonon boundary and defect scattering by nanostructures. This idea is best illustrated by a very recent report by Kanatzidis and co-workers<sup>15</sup> in which ZT beyond 2 is achieved in PbTe. The high ZT is due to extremely low  $\kappa_{\rm L}$  caused by hierarchical structures with different length scales that scatter the full spectrum of phonons. This approach has been shown to be quite generic provided that the characteristic nanostructure sizes are smaller than phonon mean free path in corresponding bulk materials, which is usually dictated by Umklapp and alloy scattering.

More recently, the trend in thermoelectric research has been shifted to toward developing a scalable route for making thermoelectric nanostructures, and new bulk-nanostructuring approaches have been developed and have achieved very notable success. As shown in Fig. 2, this new approach is based on the production of bulk thermoelectric composites from nanopowders containing a high density of grain boundaries. The key idea of the nanocomposites is to use the high density of grain boundaries to scatter phonons without significantly adversely affecting the charge transport. The thermoelectric properties of various nanocomposite materials have been reported. 16–20

Among numerous reports, the most popular methods for producing thermoelectric nanopowders are based on top-down approaches. For example, Poudel et al. <sup>17</sup> reported the fabrication of nanocomposite p-type  $\mathrm{Bi}_{0.5}\mathrm{Sb}_{1.5}\mathrm{Te}_3$  by ball milling the bulk alloys for extended hours to nanometer dimensions in inert environments and hot-pressing these nanopowders to produce the sintered compacts. They have achieved a high ZT of 1.4 at  $100^{\circ}\mathrm{C}$ . The same groups also reported a similar ball milling-hot pressing approach for other materials including Si-Ge alloy <sup>16</sup> and n-type Si, <sup>21</sup> among many others. Another recently developed approach is melt-spinning ribbons of the appropriate alloy, hand-grinding them, and compacting them by spark

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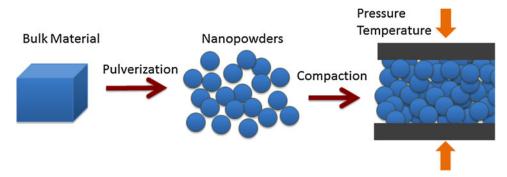


Fig. 2. Schematic of the process for making nanocomposites of thermoelectric materials. The starting bulk material is pulverized into nanopowders by different methods, which are subsequently pressed into compact pellets using processes such as hot pressing and spark-plasma sintering.

plasma sintering (SPS).  $^{19}$  A similarly high ZT of  $\sim\!1.5$  at 360 K was observed in these  $\rm (Bi,Sb)_2Te_3$  nanocomposites.

# SILICIDE AS A THERMOELECTRIC MATERIAL

While nanostructured thermoelectric materials have significantly increased the ZT beyond the unity, the materials (Se, Te, Sb, Ge, and Ag) involved are often not easy-to-scale to high-volume applications such as solar energy utilization and industrial waste heat harvesting, and some materials are toxic (e.g., Pb) that would limit their applications in systems such as automobiles. Therefore, there is an increasing amount of effort devoted to alternative thermoelectric materials that are less expensive, more abundant, and nontoxic. This trend has been facilitated by the aforementioned nanostructuring approaches that are used to enhance ZT in materials that are traditionally poor thermoelectric materials, such as Si<sup>10,11,21</sup> PbSe.<sup>22</sup>

A very promising class of Earth-abundant thermoelectric materials is based on silicide,  $^{6,23}$  such as Mg<sub>2</sub>Si (Ref. 24), higher manganese silicides (MnSi<sub>x</sub>),  $^{25,26}$   $\beta$ -FeSi<sub>2</sub> (Ref. 27), and Ru<sub>2</sub>Si<sub>3</sub> (Ref. 28). Silicide alloys are attractive for thermoelectric applications due to their low toxicity, thermal stability, low density, relative abundance, and low cost of production. They are especially attractive for waste heat recovery in the mid-to-high temperature range (400 K to 800 K) where they exhibit the peak  $ZT.^{6,23}$ 

In this overview, we will focus on  $Mg_2Si$  and its alloy because it has been most widely studied for the thermoelectrics and has shown the highest ZT among the silicide family.  $Mg_2Si$  belongs to the family of magnesium (IV) compounds that crystallizes in the antifluorite structure with Si in face-centered cubic positions and Mg in tetrahedral sites<sup>29</sup> (Fig. 3a).  $Mg_2Si$  is a semiconductor with an indirect bandgap of  $\sim 0.78$  eV, and its room tem-

perature mobility is as high as  $406 \text{ cm}^2/\text{V-sec}$  for n-type and  $56 \text{ cm}^2/\text{V-sec}$  for p-type material. The exhibited mobilities and bandgap are favorable for thermoelectrics. In 2006, Zaitsev et al. Peroted an optimal ZT of 1.1 at around 800 K for polycrystalline  $Mg_2Si_{0.4}Sn_{0.6}$  and  $Mg_2Si_{0.6}Sn_{0.4}$  (Fig. 3b). This high ZT value in Mg-Si-Sn alloy is comparable to the best conventional TE materials such as Pb-Te, CoSb<sub>3</sub>, and Si-Ge alloys within the temperature range of 400 K to 800 K. However, unlike these conventional TE materials, the Mg-Si-Sn alloy contains some of the most abundant elements (Mg, Si, and Sn)

Honda et al.<sup>31</sup> carried out a very interesting study on Mg<sub>2</sub>Si alloys using reused-Si sludge ( $\sim$ 3.5 N) as a Si source and recycled Mg-alloys as a Mg source at a stoichiometric ratio (Mg:Si = 2:1). The Mg<sub>2</sub>Si alloy was formed by homogeneous melting at 1423 K while Bi and Al were added as *n*-type and *p*-type dopants. The synthesized polycrystalline Mg<sub>2</sub>Si was then pulverized into powders and sintered using a plasma-activated sintering technique. The ZT values were 0.6 at 860 K for the samples fabricated from reused-Si and recycled Mg-alloys, showing no notable difference compared with specimens fabricated from high-purity Si and Mg sources. This study shows that the impurities (such as Al) presented in the recycled Mg-alloys can be utilized as dopants for Mg2Si without significantly deteriorating its carrier transport properties.

Furthermore, many of the processes creating the nanostructures, such as thin film deposition, are expensive and not scalable. Ball milling  $^{17}$  is a process that can make high-volume production of thermoelectric nanopowders, but they often require very long and energy-intensive milling time to make fine powders (more than 10 h). In addition, Ball milling is more suitable for brittle materials but not applicable to ductile materials with low Young's modulus. The bottom-up approach for making thermoelectric materials is potentially more scalable but has not been able to produce thermoelectric nanostructures with ZT > 1.

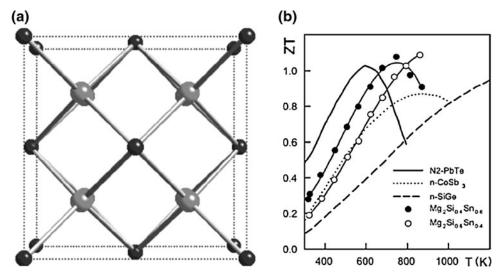


Fig. 3. (a) Unit cell of  $Mg_2Si$ . It is a face-centered (Fm3m) lattice, with a simple cubic lattice of Mg atoms such that each Mg (large gray circles) is coordinated by four Si atoms in a regular tetrahedron, while each Si (small black circles) is surrounded by a regular cube of eight Mg atoms (Reprinted with permission from Ref. [29], Copyright 2003, American Chemical Society). (b) TE figure of merit ZT of the  $Mg_2Si-Mg_2Sn$  alloys, in comparison with the best bulk TE materials within the similar temperature range (Reprinted with permission from Ref. [24], Copyright 2006, American Physical Society).

# FABRICATION AND THERMOELECTRIC PROPERTIES OF SILICIDE NANOPOWDERS

In view of the success of various nanostructuring approaches for enhancing ZT in conventional thermoelectric materials, it is then natural to extend the ideas to silicide, in particular  $Mg_2Si$  and its alloys. Here, we summarized some of the popular techniques that have been employed to fabricate nanopowders of  $Mg_2Si$  and its alloys and their thermoelectric properties.

#### **Ball Milling**

Ball milling/mechanical alloying is a simple and yet effective approach for making thermoelectric nanopowders and has been successfully applied for materials such as  $\mathrm{Bi}_{0.5}\mathrm{Sb}_{1.5}\mathrm{Te}$  (Ref. 17), Si (Ref. 21), and Si-Ge alloy,  $^{16}$  etc. Therefore, it can be an attractive technique for producing large-scale quantity of Mg<sub>2</sub>Si. In this process, either chucks of polycrystalline Mg<sub>2</sub>(SiSn) alloys or elemental powders are loaded into a milling vial, and the vial is inserted in a higher energy milling apparatus.<sup>32</sup> Schilz et al. 22 reported on the influence of the planetary ball mill setting parameters on the evolution of alloy formation on the thermoelectric semiconductor systems including Mg2Si and Mg<sub>2</sub>(SiSn) alloys. They observed that in the case of Mg<sub>2</sub>Si and Mg<sub>2</sub>(SiSn), the alloying proceeds on the surface of the Mg bulk particles.

However, Mg<sub>2</sub>Si and its alloys are ductile as opposed to the conventional TE materials that are brittle (e.g., Si-Ge). The "softness" of Mg<sub>2</sub>Si makes it difficult to synthesize via ball milling,<sup>35</sup> which tends to distort the material by plastic deformation instead of fracturing it, leading to Mg aggregation.<sup>35</sup>

Xiong et al.<sup>33</sup> reported the synthesis of nanocrystalline Mg<sub>2</sub>Si by mechanical milling and found that the content of Mg<sub>2</sub>Si phase increases with increasing milling time; however, pure Mg<sub>2</sub>Si phase cannot be obtained by direct ball milling. Moreover, monolithic Mg<sub>2</sub>Si phase could only be obtained when as much as 10% of excess Mg was blended in the raw mixtures. The excess Mg could be agglomerated and oxidized, resulting in impurities in the synthesized powders. Li and Kong<sup>36</sup> reported that even after 100 h of milling, phase pure Mg<sub>2</sub>Si could not be synthesized.

Recently, Bux et al.<sup>35</sup> used an incremental ball milling process to address the problem of Mg agglomeration. In this process, small amount of Mg (200-500 mg) was added into a stoichiometric amount of Si and Bi and ball milled for intervals of less than 1 h. An additional 200 to 500 mg of increments of Mg were added and ball milled until the correct stoichiometry was achieved. The reaction could be could be completed within 8 h depending on the amount of materials. The scanning electron microscope (SEM) shows the powders are made up of mostly large aggregates ranging from 50 nm to micron sizes (Fig. 4a), while transmission electron microscope (TEM) imaging shows smaller grains size (on the order of 30 nm) (Fig. 4b). The synthesized powders were than compacted into pellets via hot pressing for thermoelectric transport measurements. A maximum ZT value of 0.7 was obtained for the samples with optimal Bi concentration (0.15%) (Fig. 4c). The lower ZT obtained in Mg<sub>2</sub>Si compared to Mg<sub>2</sub>(SiSn) reported in Ref. 24 is mainly caused by the higher lattice thermal conductivity ( $\kappa_L$  are  $\sim 2.5$  and  $\sim 1.2$  W/m K at 800 K for Mg<sub>2</sub>Si, Ref. 35 and Mg<sub>2</sub>(SiSn), Ref. 12, respectively),

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presuming due to the stronger alloy scattering in  $Mg_2(SiSn)$  alloys.

### **Microwave-Assisted Synthesis**

Another highly promising route for the synthesis of nanocrystalline Mg<sub>2</sub>Si is microwave heating, as developed by Gascoin and co-workers. 37-39 In this route, nanocrystalline Mg<sub>2</sub>Si powders were synthesized at a high vield by employing microwave radiation. The elemental precursors (Si and Mg) were first milled together under dry conditions to get fine particles. The resulting mixture of powders of Mg and Si was cold pressed before being heated by microwave irradiation. The found that that the power and time of the microwave irradiation can be used to control the grain growth of the Mg<sub>2</sub>Si and must be adequately controlled to avoid the decomposition of the phase. Their results show that the method can readily synthesize homogeneous nanocrystalline Mg<sub>2</sub>Si with particle size smaller than 100 nm, with a microwave power of 100 to 200 W for only a few minutes (on powders ball milled for  $^{37}$  Maximum ZT values of 0.7 and 0.35 at 770 K were obtained for n- and p-type Mg<sub>2</sub>Si-based materials (Fig. 5).3

#### **Spark Erosion**

Recently, Berkowitz and co-workers at the University of California at San Diego reported a new process, referred to as "spark erosion," for making nanopowders of thermoelectric materials. 40 The spark erosion process was originally invented by Berkowitz and Walter to produce micron-sized and amorphous powders of metals. 41 By tuning the process conditions, Nguyen et al. have demon-

strated the application of the spark erosion process in producing large quantity (>  $100~{\rm g}$  scale) of metal and semiconductor nanoparticles.

The basic idea and apparatus of the spark erosion process is shown in Fig. 6, which is a sketch of the spark erosion system. The diameter spark erosion cell, 10 cm in size, is mounted in a double-walled, vacuum-jacketed glass container that holds the dielectric liquid. Two electrodes of the material of interest are mounted in the cell and connected to the pulsed power source. "Charge" pieces of the same material,  $\sim\!\!2$  cm diameter in irregular shapes, fill the perforated Delrin support, making contact with the electrodes. The glass container is vibrated

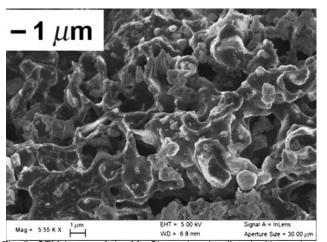


Fig. 5. SEM image of the Mg<sub>2</sub>Si powders irradiated with a microwave power of 200 W for 10 min (Reprinted with permission from Ref. [37], Copyright 2010, Royal Society of Chemistry).

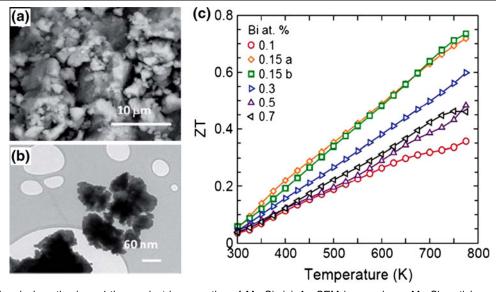


Fig. 4. Mechanochemical synthesis and thermoelectric properties of  $Mg_2Si$ . (a) An SEM image shows  $Mg_2Si$  particles ranging in size from nanometers to microns. (b) A TEM image shows that  $Mg_2Si$  aggregates are made up of smaller particles and crystallites. (c) ZT of samples with various Bi doping concentrations from 300 K to 800 K. For samples with near-optimum carrier concentrations, ZT values of 0.7 are obtained at 775 K (Reprinted with permission from Ref. [35], Copyright 2011, Royal Society of Chemistry).

so that contacts among the electrodes and charge pieces are made and broken frequently. Thus, electrical contact between the electrodes is made randomly. The pulsed power source is a charged capacitor. When the gaps among the electrodes and charge pieces are small enough so that the electric

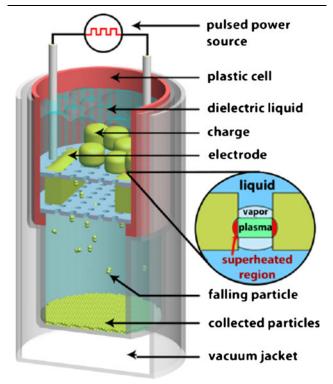


Fig. 6. Sketch of apparatus of the spark erosion process features (Reprinted with permission from Ref. [41], Copyright 2012, IOP Publishing).

field across them is larger than the dielectric breakdown field, the capacitor discharges, producing a spark (microplasma) between the pieces involved. This microplasma, consisting of electrons and positive ions, is very hot, at 10,000 K. The kinetic energies of the faster electrons and slower ions are deposited on localized regions where the spark was initiated, superheating them to boiling. When the spark collapses, vaporized alloy and molten droplets are violently ejected from the boiling regions and are propelled though the plasma region into the dielectric liquid, where they are very rapidly quenched. Since the quenching rate is very rapid, particles formed could be very small.

Using this method, Nguyen et al. 40 reported the

Using this method, Nguyen et al. 40 reported the synthesis of thermoelectric Bi<sub>0.5</sub>Sb<sub>1.5</sub>Te<sub>3</sub> nanoparticles with a production rate as high as 135 g/h using the relatively small laboratory apparatus and low energy consumption. The compacted nanocomposite samples made from these nanoparticles exhibit a well-defined, 20 to 50-nm size nanograin microstructure and show an enhanced figure of merit, ZT, of 1.36 at 360 K. This technique is very promising for producing inexpensive and oxidation-free nanoparticles for fabricating high-performance thermoelectric materials.

Because the spark erosion technique does not relied on mechanical ball milling, it is particularly attractive for ductile materials such as  $Mg_2Si$ . In this respect, we have carried out the spark erosion process for  $Mg_2(SiSn)$ . The initial results are very promising. As shown in Fig. 7, the SEM image shows that the spark-eroded powders exhibit nanometer and micron particle sizes, while the TEM image shows a smaller grain size ( $\sim 20$  nm). Currently, the yield for producing the  $Mg_2(SiSn)$  nanopowders is around 5 g/h. Even though the yield is

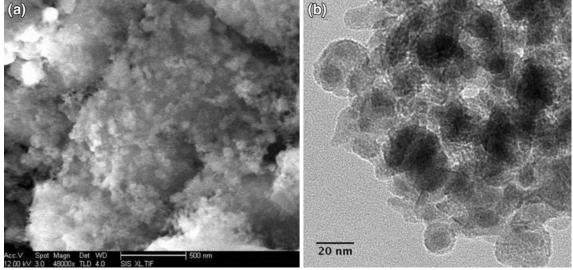


Fig. 7. Nanopowders of  $Mg_2(SiSn)$  made from the spark erosion process. SEM imaging (a) shows that the spark-eroded powders exhibit nanometer and micron particle sizes, while the TEM image (b) shows smaller grain size ( $\sim$ 20 nm) (from Moon et al., unpublished, Copyright 2013, University of California, San Diego).

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much lower than that of spark-eroded Bi-Sb-Te (presumably due to the higher melting point of the silicide), it is much faster than that of ball milling. In addition, since the entire process was carried out in dielectric liquids (liquid Ar or N, Ref. 40), oxidation-free nanoparticles of Mg<sub>2</sub>(SiSn) can be readily synthesized using this approach. Therefore, this method could be a very promising route for producing a large quantity of high-quality thermoelectric silicide nanopowders.

#### **CONCLUSION**

In conclusion, we summarized some recent development on the fabrication and thermoelectric properties of silicide nanopowders with a focus on Mg<sub>2</sub>Si and its alloys (Mg<sub>2</sub>(SiSn)). Thermoelectric energy conversion could be a transformative technology for improving energy efficiency and providing renewable energy, but the performance-to-cost ratio of thermoelectric devices has to be significantly improved. In this respect, silicide is a very attractive candidate because of Earth abundance, thermal stability, and low toxicity. It is especially attractive for waste heat recovery in the mid-to-high temperature range (400 K to 800 K) where it exhibits the peak ZT. Nanostructuring has been proven to be a very effective approach to enhance thermoelectric performance in a variety of conventional thermoelectric material systems including Bi-Sb-Te, CoSb<sub>3</sub>, and Si-Ge; therefore, an increasing amount of effort has been devoted to fabricating silicide nanopowders with the aim of enhancing the ZT values. Different approaches to fabricate Mg<sub>2</sub>Si nanopowders are discussed, including ball milling/mechanical alloying, microwave-assisted synthesis, and spark erosion. It is expected that silicide nanocomposite materials with enhanced ZT are within reach using these and other nanostructuring techniques.

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