

## Erratum to: Generalized Solution for 1-D Non-Newtonian Flow in a Porous Domain due to an Instantaneous Mass Injection

Vittorio Di Federico · Valentina Ciriello

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A review of the above work has revealed the following errors listed below.

- (i) In the expression of the mobility ratio  $k/\mu_{ef}$ , the factor  $(3 + n)$  is wrongly written for the factor  $(3n + 1)$ ; hence the correct formulations of Eqs. (4) and (15) should read:

$$\frac{k}{\mu_{ef}} = \frac{1}{2H} \left( \frac{n\phi}{3n + 1} \right)^n \left( \frac{8k}{\phi} \right)^{(1+n)/2}, \quad (4)$$

$$\chi_n = \frac{8^{(1+n)/2}}{2} \left( \frac{n}{3n + 1} \right)^n. \quad (15)$$

- (ii) There is a missing minus sign before the pressure gradient within parentheses on the r.h.s. of Eq. (5); the correct formulation is

$$\frac{\partial^2 p}{\partial r^2} + \frac{(d-1)n}{r} \frac{\partial p}{\partial r} = n(\phi \cdot c_0 + c_p) \left( \frac{\mu_{ef}}{k} \right)^{1/n} \left( -\frac{\partial p}{\partial r} \right)^{(n-1)/n} \frac{\partial p}{\partial t}; \quad (5)$$

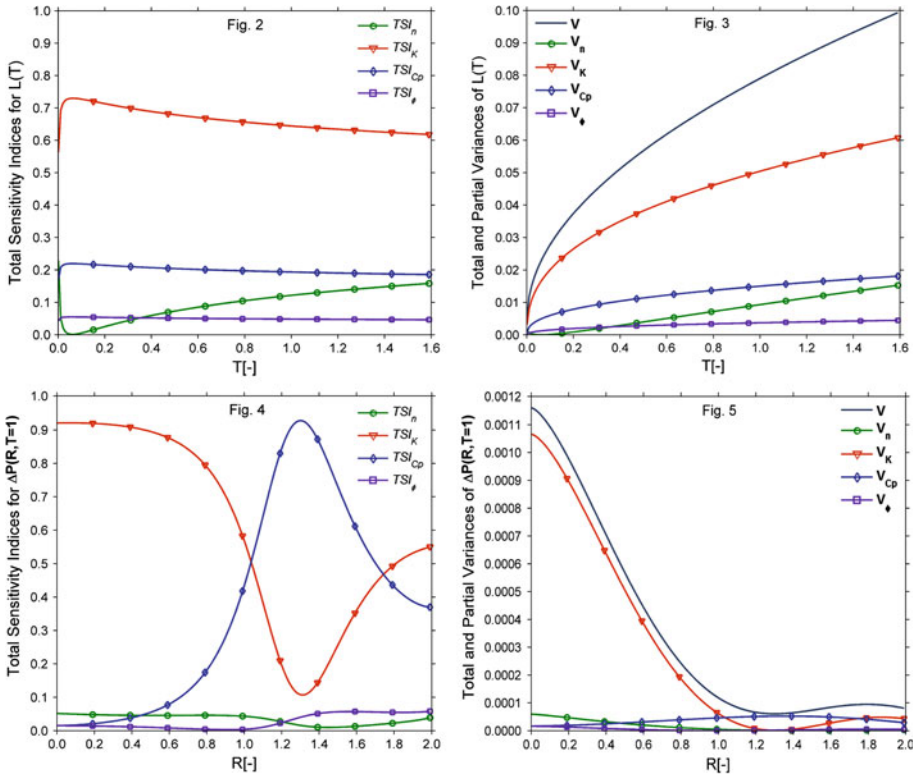
this does not affect further developments which are based on the correct dimensionless version (14).

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V. Di Federico (✉) · V. Ciriello  
Dipartimento di Ingegneria Civile, Chimica, Ambientale e dei Materiali (DICAM),  
Università di Bologna, Bologna, Italy  
e-mail: vittorio.diferedico@unibo.it

V. Ciriello  
e-mail: valentina.ciriello3@unibo.it



**Fig. 2–5** 2 Total sensitivity indices (*TSI*) of each random parameter (*n*, *K*, *C<sub>p</sub>*, *ϕ*) with respect to the front position *L(T)* versus time *T* for cylindrical geometry (*d* = 2), *S* = 1, *M*<sub>0</sub> = 1, *r<sub>c</sub>* = 1; **3** As **(2)** but total and partial variances (*V*); **4** As **(2)** but with respect to the excess pressure  $\Delta P$  versus radial distance *R* and *T* = 1; **5** As **(4)** but total and partial variances

(iii) There is a missing factor  $K^{(n+1)/2n}$  in the definition of dimensionless velocity *V*; hence the correct versions of Eqs. (13) and (31) are:

$$V = \frac{\chi_n^{1/n}}{\phi^{(1-n)/2n}} K^{(n+1)/2n} \left( -\frac{\partial P}{\partial R} \right)^{1/n}, \tag{13}$$

$$V = \frac{\chi_n^{1/n}}{\phi^{(1-n)/2n}} K^{(n+1)/2n} \left( \frac{1-n}{1+n} A\beta \right)^{1/(1-n)} T^{-[(1+d)]/[1+n+d(1-n)]} \eta(\eta_1^{1+n} - \eta^{1+n})^{1/(1-n)}. \tag{31}$$

(iv) The exponent of dimensionless permeability *K* in Eq. (16) is (1 + *n*)/2*n* and not (1 − *n*)/2*n*; the correct version is

$$A = (r_c\phi + C_p) \frac{\phi^{(1-n)/2n}}{\chi_n^{1/n} K^{(1+n)/2n}}. \tag{16}$$

As a consequence of corrections (i) and mainly of (iv), Figs. 2–5 in Di Federico and Ciriello (2012) need amendment. The revised version of the figures, drawn for dimensionless injected mass *M*<sub>0</sub> = 1, is shown below. It is seen that the overall trends discussed in

[Di Federico and Ciriello \(2012\)](#) remain valid, albeit with a larger influence of permeability on the variance of front position and pressure and, correspondingly, a higher total sensitivity index for permeability.

Moreover, the reference to [Di Federico et al. \(2010\)](#) in [Di Federico and Ciriello \(2012\)](#) contains a typographical error in page number. That reference should read as indicated in the reference section of this erratum.

## References

- Di Federico, V., Ciriello, V.: Generalized solution for 1-D non-Newtonian flow in a porous domain due to an instantaneous mass injection. *Transp. Porous Med.* **93**, 63–77 (2012). doi:[10.1007/s11242-012-9944-9](https://doi.org/10.1007/s11242-012-9944-9)
- Di Federico, V., Pinelli, M., Ugarelli, R.: Estimates of effective permeability for non-Newtonian fluid flow in randomly heterogeneous porous media. *Stoch. Environ. Res. Risk Assess.* **24**, 1067–1076 (2010). doi:[10.1007/s00477-010-0397-9](https://doi.org/10.1007/s00477-010-0397-9)