# Erratum to: Localizing the latent structure canonical uncertainty: entropy profiles for hidden Markov models 

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## Erratum to: Stat Comput

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In the original publication of this article, equation layouts are aligned incorrectly. Now the correct version is appears in this erratum.

## Layout of equations

In Sect. 2.1 paragraph 1, the equation should read

$$
\begin{aligned}
& P\left(X_{0}=x_{0}, \ldots, X_{T-1}=x_{T-1} \mid S_{0}=s_{0}, \ldots, S_{T-1}=s_{T-1}\right) \\
& \quad=\prod_{t=0}^{T-1} P\left(X_{t}=x_{t} \mid S_{t}=s_{t}\right)
\end{aligned}
$$

Equation (6) should read

$$
\begin{align*}
& H\left(S_{0} \mid S_{1}=j, X_{0}^{1}=x_{0}^{1}\right) \\
& \quad=-\sum_{i=0}^{J-1} P\left(S_{0}=i \mid S_{1}=j, X_{0}^{1}=x_{0}^{1}\right) \\
& \quad \times \log P\left(S_{0}=i \mid S_{1}=j, X_{0}^{1}=x_{0}^{1}\right) \tag{6}
\end{align*}
$$

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Equations in (7) should read

$$
\begin{align*}
& H\left(S_{0}^{t-1} \mid S_{t}=j, X_{0}^{t}=x_{0}^{t}\right) \\
& =-\sum_{s_{0}, \ldots, s_{t-1}} P\left(S_{0}^{t-1}=s_{0}^{t-1} \mid S_{t}=j, X_{0}^{t}=x_{0}^{t}\right) \\
& \times \log P\left(S_{0}^{t-1}=s_{0}^{t-1} \mid S_{t}=j, X_{0}^{t}=x_{0}^{t}\right) \\
& =-\sum_{s_{0}, \ldots, s_{t-2}} \sum_{i=0}^{J-1} P\left(S_{0}^{t-2}=s_{0}^{t-2} \mid S_{t-1}=i, S_{t}=j, X_{0}^{t}=x_{0}^{t}\right) \\
& \times P\left(S_{t-1}=i \mid S_{t}=j, \quad X_{0}^{t}=x_{0}^{t}\right) \\
& \times\left\{\log P\left(S_{0}^{t-2}=s_{0}^{t-2} \mid S_{t-1}=i, S_{t}=j, X_{0}^{t}=x_{0}^{t}\right)\right. \\
& \left.+\log P\left(S_{t-1}=i \mid S_{t}=j, X_{0}^{t}=x_{0}^{t}\right)\right\} \\
& =-\sum_{i=0}^{J-1} P\left(S_{t-1}=i \mid S_{t}=j, X_{0}^{t-1}=x_{0}^{t-1}\right) \\
& \times\left\{\sum_{s_{0}, \ldots, s_{t-2}} P\left(S_{0}^{t-2}=s_{0}^{t-2} \mid S_{t-1}=i, X_{0}^{t-1}=x_{0}^{t-1}\right)\right. \\
& \times \log P\left(S_{0}^{t-2}=s_{0}^{t-2} \mid S_{t-1}=i, X_{0}^{t-1}=x_{0}^{t-1}\right) \\
& \left.+\log P\left(S_{t-1}=i \mid S_{t}=j, X_{0}^{t}=x_{0}^{t}\right)\right\} \\
& =\sum_{i=0}^{J-1} P\left(S_{t-1}=i \mid S_{t}=j, X_{0}^{t-1}=x_{0}^{t-1}\right) \\
& \times\left\{H\left(S_{0}^{t-2} \mid S_{t-1}=i, X_{0}^{t-1}=x_{0}^{t-1}\right)\right. \\
& \left.-\log P\left(S_{t-1}=i \mid S_{t}=j, X_{0}^{t-1}=x_{0}^{t-1}\right)\right\}, \tag{7}
\end{align*}
$$

Page 4, the equation in the remark at the bottom of the second column should read

$$
\begin{aligned}
& H\left(S_{0}^{t-1} \mid S_{t}=j, X_{0}^{t}=x_{0}^{t}\right) \\
& \quad=H\left(S_{0}^{t-2} \mid S_{t-1}, S_{t}=j, X_{0}^{t}=x_{0}^{t}\right) \\
& \quad \quad+H\left(S_{t-1} \mid S_{t}=j, X_{0}^{t}=x_{0}^{t}\right)
\end{aligned}
$$

Page 7, the first equation of the first column should read

$$
\begin{aligned}
& P(\boldsymbol{S}=\boldsymbol{s} \mid \boldsymbol{X}=\boldsymbol{x}) \\
& \quad=\prod_{u} P\left(S_{u}=s_{u} \mid \boldsymbol{S}_{p a(u)}=\boldsymbol{s}_{p a(u)}, \boldsymbol{X}=\boldsymbol{x}\right)
\end{aligned}
$$

Equation (13) should read

$$
\begin{align*}
& P\left(\boldsymbol{S}_{A}=\boldsymbol{s}_{A} \mid \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=\prod_{v \in A} P\left(S_{v}=s_{v} \mid \boldsymbol{S}_{\mathrm{pa}(v)}=\boldsymbol{s}_{\mathrm{pa}(v)}, \boldsymbol{X}=\boldsymbol{x}\right) . \tag{13}
\end{align*}
$$

Page 7, the first equation of the second column should read

$$
\begin{aligned}
& P\left(\boldsymbol{S}_{A^{\prime}}=\boldsymbol{s}_{A^{\prime}} \mid \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=P\left(S_{u}=s_{u} \mid \boldsymbol{S}_{\mathrm{pa}(u)}=\boldsymbol{s}_{\mathrm{pa}(u)},\right. \\
& \left.\quad \boldsymbol{S}_{A \backslash \mathrm{pa}(u)}=\boldsymbol{s}_{A \backslash \mathrm{pa}(u)}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad \times P\left(\boldsymbol{S}_{\mathrm{pa}(u)}=\boldsymbol{s}_{\mathrm{pa}(u)}, \boldsymbol{S}_{A \backslash \mathrm{pa}(u)}=\boldsymbol{s}_{A \backslash \mathrm{pa}(u)} \mid \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=P\left(S_{u}=s_{u} \mid \boldsymbol{S}_{\mathrm{pa}(u)}=\boldsymbol{s}_{\mathrm{pa}(u)}, \boldsymbol{X}=\boldsymbol{x}\right) P\left(\boldsymbol{S}_{A}=\boldsymbol{s}_{A} \mid \boldsymbol{X}=\boldsymbol{x}\right)
\end{aligned}
$$

In Appendix 1 the first equation (Proposition 2) should read

$$
\begin{aligned}
& P\left(\overline{\boldsymbol{S}}_{\mathcal{V}}=\overline{\boldsymbol{s}}_{\mathcal{V}} \mid \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=P\left(S_{r}=s_{r} \mid \boldsymbol{X}=\boldsymbol{x}\right) \prod_{\substack{u \in \mathcal{V} \\
u \neq r}} P\left(S_{u}=s_{u} \mid S_{\rho(u)}=s_{\rho(u)}, \boldsymbol{X}=\boldsymbol{x}\right)
\end{aligned}
$$

In Appendix 2, equations in (19) and (20) should read

$$
\begin{align*}
& P\left(\overline{\boldsymbol{S}}_{c(u)}=\overline{\boldsymbol{s}}_{c(u)} \mid S_{u}=j, \overline{\boldsymbol{S}}_{0 \backslash u}=\overline{\boldsymbol{s}}_{0 \backslash u}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=P\left(\overline{\boldsymbol{S}}_{c(u)}=\overline{\boldsymbol{s}}_{c(u)} \mid S_{u}=j, S_{\rho(u)}=s_{\rho(u)}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=P\left(\overline{\boldsymbol{S}}_{c(u)}=\overline{\boldsymbol{s}}_{c(u)} \mid S_{u}=j, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=\prod_{v \in c(u)} P\left(\overline{\boldsymbol{S}}_{v}=\overline{\boldsymbol{s}}_{v} \mid S_{u}=j, \boldsymbol{X}=\boldsymbol{x}\right) \\
& =\prod_{v \in c(u)} P\left(\overline{\boldsymbol{S}}_{v}=\overline{\boldsymbol{s}}_{v} \mid S_{u}=j, \overline{\boldsymbol{X}}_{v}=\overline{\boldsymbol{x}}_{v}\right)  \tag{19}\\
& \quad=P\left(\overline{\boldsymbol{S}}_{c(u)}=\overline{\boldsymbol{s}}_{c(u)} \mid S_{u}=j, \overline{\boldsymbol{X}}_{u}=\overline{\boldsymbol{x}}_{u}\right) \tag{20}
\end{align*}
$$

In Appendix 2, the equations following (20) should read

$$
\begin{aligned}
& P\left(\overline{\boldsymbol{S}}_{u}=\overline{\boldsymbol{s}}_{u} \mid \overline{\boldsymbol{S}}_{0 \backslash u}=\overline{\boldsymbol{s}}_{0 \backslash u}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=P\left(\overline{\boldsymbol{S}}_{u}=\overline{\boldsymbol{s}}_{u} \mid S_{\rho(u)}=s_{\rho(u)}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=P\left(\overline{\boldsymbol{S}}_{u}=\overline{\boldsymbol{s}}_{u} \mid S_{\rho(u)}=s_{\rho(u)}, \overline{\boldsymbol{X}}_{u}=\overline{\boldsymbol{x}}_{u}\right) .
\end{aligned}
$$

In Appendix 2, the equations in (21) should read

$$
\begin{align*}
& H\left(\overline{\boldsymbol{S}}_{c(u)} \mid S_{u}=j, \overline{\boldsymbol{X}}_{u}=\overline{\boldsymbol{x}}_{u}\right) \\
& \quad=H\left(\overline{\boldsymbol{S}}_{c(u)} \mid S_{u}=j, \overline{\boldsymbol{X}}_{c(u)}=\overline{\boldsymbol{x}}_{c(u)}\right) \\
& \quad=\sum_{v \in c(u)} H\left(\overline{\boldsymbol{S}}_{v} \mid S_{u}=j, \overline{\boldsymbol{X}}_{v}=\overline{\boldsymbol{x}}_{v}\right) \tag{21}
\end{align*}
$$

In Appendix 2, the equations in (25) should read

$$
\begin{align*}
& H\left(\overline{\boldsymbol{S}}_{u} \mid S_{\rho(u)}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=H\left(S_{u} \mid S_{\rho(u)}, \boldsymbol{X}=\boldsymbol{x}\right)+H\left(\overline{\boldsymbol{S}}_{c}(u) \mid S_{u}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad=H\left(S_{u} \mid S_{\rho(u)}, \boldsymbol{X}=\boldsymbol{x}\right) \\
& \quad+\sum_{j} L_{u}(j) H\left(\overline{\boldsymbol{S}}_{c(u)} \mid S_{u}=j, \boldsymbol{X}=\boldsymbol{x}\right) \tag{25}
\end{align*}
$$

