



Ultrasonic constraint of the microfracture anisotropy of flysch rocks from the Podhale Synclinorium (Poland)

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Abstract

This paper attempts to show the relationship between joints observed in flysch formations in the field and microfracture fabrics invisible to the naked eye in hand specimens. Ultrasonic measurements demonstrate that the intensity and orientations of domains “memorised” by rock specimens are associated with the historical stresses within the rock mass rather than the rock lamination. The spatial orientations of these microfractures have been measured, and their dynamic-elastic properties have been found to correlate with the orientation of macroscopic joint sets measured in the field. The elastic properties measured vary because of sedimentary diagenetic processes that occurred during the tectonic deformations of these flysch rocks in the Podhale Synclinorium of Poland. The structural discontinuities detected by ultrasonic measurements can be perceived as an incipient phase of the macroscopic joints already visible in the field and are attributed to the in situ residual tectonic stresses. Such historical stresses impart a hidden mechanical anisotropy to the entire flysch sequence. The microfractures will develop into macroscopic joints during future relaxation of the exposed rock mass. Understanding the nature and orientation of the invisible microfracture anisotropy that will become macroscopic in the future is vital for the safe and efficient engineering of any rock mass.

Keywords Joints · Microfractures · Flysch rocks · Ultrasonic waves · Dynamic elastic properties

Introduction

The mechanical properties of any rock mass must be known in appropriate detail to design safe and efficient future engineering projects in, on, or under it. For example, one can deduce the effective density of a rock mass when density varies inside it along specific directions (Mukherjee 2017a, b, c, 2018). Detailed investigations of the mechanical properties (e.g. Mukherjee et al. 2010; Mukherjee 2011, 2013; Mukherjee and Mulchrone 2012; Pinińska 2011) should follow routine analyses of the overall geological structure and hydrogeological conditions of the rock mass. Such studies should characterise the rock mass in terms of its mineralogical and petrographic characteristics as well as its structural heterogeneity, discontinuities and anisotropy of physical and mechanical properties (Thiel 1980). Typical rock properties required are the types, proportions and size of the constituent

minerals and their orientations together with the proportions, size and orientations of any pores and any cement filling them. The presence of discontinuities in the form of visible joints or hidden internal weaknesses such as microfractures reduces the overall strength of the rock mass, increases its deformability and permeability and facilitates the movement of rock blocks (Van der Pluijm and Marshak 2004; Pinińska and Dziedzic 2006; Domanik 2012).

Geologic fractures are generally thought to initiate at flaws randomly dispersed throughout the host rock (e.g. Olson 1993), based on the experimental works of Griffith (1921) as well as field evidence that joints propagated from microfractures located at fossils or sedimentary structures (e.g. Helgeson and Aydin 1991; Savalli and Engelder 2005). The issue of explaining fracture patterns, in particular how to start from an unorganised flaw distribution and produce a non-random pattern, is currently being investigated (Hooker et al. 2017). Kieslinger (1958) expressed the view that the presence of joints in the rock mass is primarily attributed to in situ residual tectonic stresses. Decrease of the overburden results in relaxation of the rock mass, which is manifested in the form of less or more advanced disintegration of the rocks

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into blocks. Furthermore, Boretti-Onyszkiewicz (1968a) interpreted such disintegration of rocks into blocks as a result of hidden, potential surface discontinuities. She found that the directions of increased stresses are as if “memorised” by the rock mass and are revealed in favourable circumstances for example during uniaxial compression tests or as the rock mass relaxes as it weathers. It should be noticed that most rocks experience several different stress regimes during their history with the result that several joint sets are frequently found superimposed on each other to produce a joint network. The complex stress history, which the Podhale Synclinorium has been subjected to, implies that the local rocks are predisposed to further degradation by more of the joints than those already observed; this in turn will increase its anisotropy of elasticity.

From a practical point of view, a penetrative fracture anisotropy is of crucial importance to the capacity of the rock mass to expand laterally. The rock blocks are mainly formed as a result of joint disclosure and the related expansion of rock masses, which is connected with the increase of rock mass capacity sideways with further advancement of the relaxation process as well as during weathering. Therefore the fracture anisotropy would be especially dangerous in slope and edge zones of valleys (Boretti-Onyszkiewicz 1968a).

This paper is a continuation of the geo-mechanical research on joints in the Polish Carpathian Mountains initiated by Boretti-Onyszkiewicz (1968a), Domonik (2003, 2005, 2008), Kłopotowska and Łukasiak (2017) as well as the studies on the evolution of the joint network in the Inner Carpathians (Boretti-Onyszkiewicz 1968b; Halicki 1963; Książkiewicz 1968; Ludwiniak 2006, 2010) and the Outer Carpathians (Rubinkiewicz 1996, 1998; Mastella and Zuchewicz 2000; Mastella and Konon 2002; Śmigielski 2007). This paper also develops the subject of the relationship between joints and the elastic properties of rock masses, which has received plenty of attention by engineering geologists in recent years, especially to predict the mechanical competency of formations targeted for future hydrocarbon exploration (Gueguen and Schubnel 2003; Eyninla and Olanunjoye 2014). That subject concerns the assessment of the elastic properties of rock masses in the field (Vilhelm et al. 2010; Živor et al. 2011; Stan-Kłęczek et al. 2012; Stan-Kłęczek and Idziak 2013) and laboratory (Pinińska et al. 2015; Stan-Kłęczek and Idziak 2008; Shkuratnik et al. 2015; Stan-Kłęczek 2016). It also concerns comparing the results obtained from static and dynamic test methods (Mockovčičaková and Pandula 2003; Barton 2007; Najibi et al. 2015). The static strength moduli can be measured by loading cylindrical core samples of standard sizes to destruction while the dynamic strength moduli can be measured by the non-destructive ultrasonic testing presented in this work.

Dynamic rock parameters can also be obtained directly in outcrops using geophysical methods.

This paper aims to demonstrate the existence of a hidden anisotropy and the resulting variability of the rocks' dynamic elastic properties revealed by directional attenuation of ultrasonic waves. The work does not aim to establish a conversion factor between static and dynamic measurement. However, the results of the elastic properties derived from both static and dynamic methods are actually presented.

The study was conducted in the Podhale Synclinorium where well-developed joints are common in rocks that have been only slightly deformed by tectonic forces.

According to Hancock (1985) and Dunne and Hancock (1994), the label “joint” is a useful field term for a barren, closed fracture on which there is no measurable slip or dilation at the scale of observation. In this paper, the term “joint” refers to systematic penetrative fractures that are perpendicular to any layering (such as bedding), cut individual layers, and on which there is no measurable shear or dilatation offsets or having only a marked tendency for offset and with spacings roughly equal to the thickness of the host layer (Jaroszewski 1972; Mastella 1972; Dadlez and Jaroszewski 1994; Mastella and Zuchewicz 2000; Mastella and Konon 2002). Joint-related arrays of en echelon fractures have also been studied in the field. The term “microfractures”, on the other hand, refers to high aspect ratio, lens or tabular-shaped cracks in rock, which are so small that it usually requires a microscope to detect them. Such microfracture fabrics are usually attributed to the effects of natural differential stresses. Microfractures commonly form as Mode I (opening) fractures where the minimum principal stress exceeds the elastic tensile strength creating a narrow opening displacement; in isotropic rocks, such fractures mark the plane perpendicular to the least compressive principal stress during fracture growth (Anders et al. 2014).

Tectonic and geological setting

The Podhale Synclinorium is a vast latitudinal trough in a Paleogene part of the Inner Carpathians (Fig. 1). Its northern limb borders the Pieniny Klippen Belt and its southern part is adjacent to Sub-Tatric units (Książkiewicz 1972). The synclinorium developed because of the inversion of a basin filled with Paleogene flysch during Miocene. In its southern limb, basal members of the Podhale succession are represented by shallow water, clastic and carbonate formations of the “nummulitic” Eocene (Roniewicz 1969; Żelaźniewicz et al. 2011). These beds are overlain by thick beds of a younger Podhale flysch (Watycha 1977; Książkiewicz 1972; Stupnicka 1997; Gedl 2000). This younger sequence has been divided into individual lithostratigraphic complexes based on the percentage of shale and sandstone beds

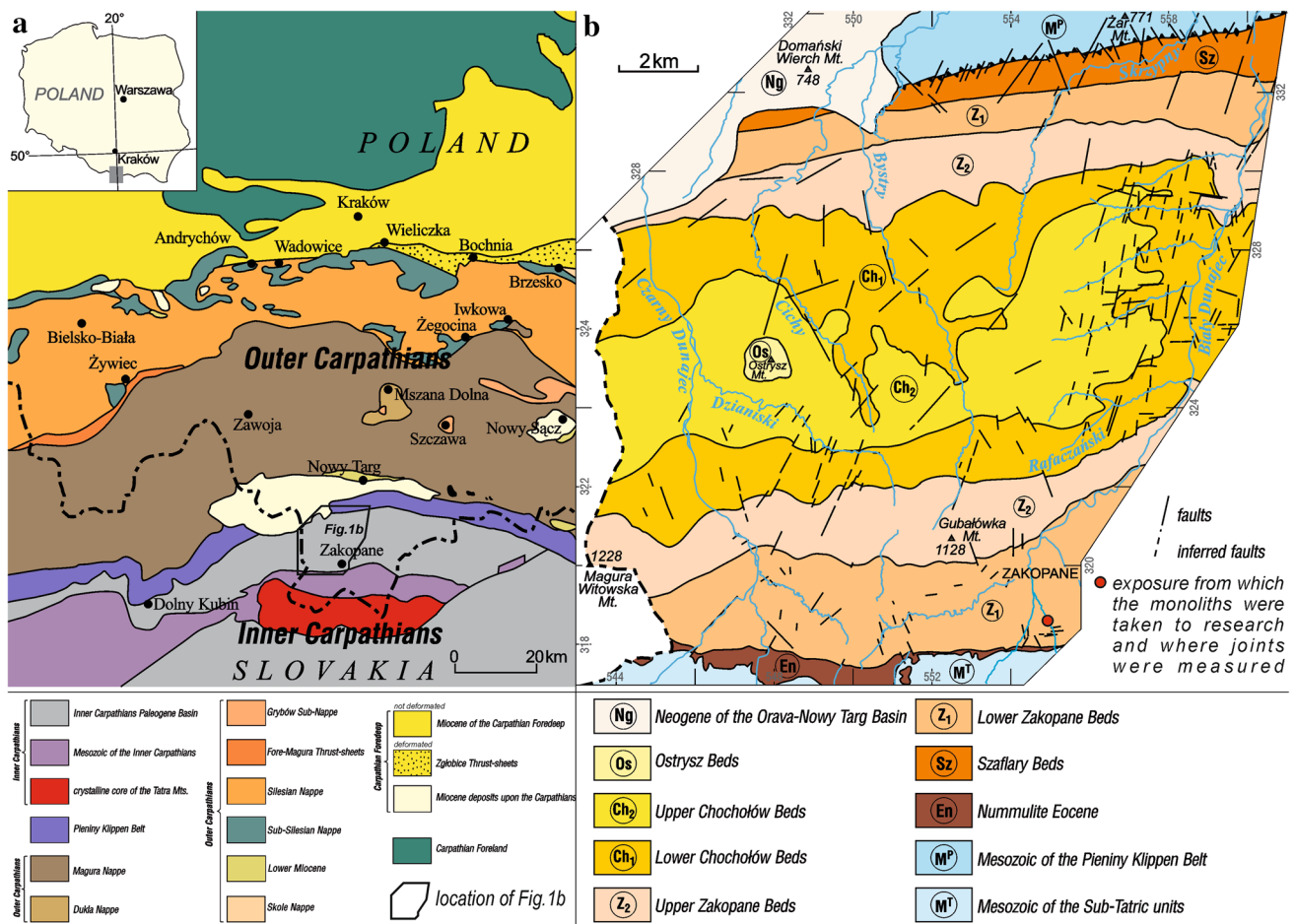


Fig. 1 a Fragment of the Polish Carpathians (based on Oszczypko et al. 2008, modified); b geological sketch map of the western Podhale Synclinorium (compiled after Watycha 1976; Mastella et al. 1988, 2000; Mastella and Klimkiewicz 2008; Ludwiniak 2008, modified)

following suggestion by Gołab (1959) and subsequently modified by Watycha (1959, 1968). According to this division, the Podhale flysch is divided into informal beds: Szaflary, Zakopane, Chochoków and Ostrysz.

The beds in the northern limb represent a monoclinical structure and dip generally southward at 10–25°. The most common bedding strikes in the eastern part of Western Podhale are 74–130° (Ludwiniak 2006; Mastella et al. 1988). The southern limb has also a monoclinical structure (Mastella and Mizerski 1977; Mastella and Ozimkowski 1979) with beds striking 70–90° and dips changing southward from 5° to 30°N (Ludwiniak 2010). However, dips can reach 40–50°N in the vicinity of the Tatra’s border. The axis of synclinorium plunges westward at 8° (Mastella and Mizerski 1977) into direction of 280° in that part of Podhale (Ludwiniak 2010). The synclinorium is cut by regular joints network (Halicki 1963; Boretti-Onyszkiewicz 1968a; Morawski 1972; Mastella and Mizerski 1977; Mastella and Ozimkowski 1979; Ludwiniak 2006, 2010). The particular joint sets, however, occurred in different stress fields. The newest Ludwiniak’s

research on geometry, morphology and the attitude of joints with respect to bedding as well as joint-related structures and veins occurring in the flysch rocks of Western Podhale showed that the local joint network have been developed in several stages connected with the structural evolution of the Podhale Synclinorium (Ludwiniak 2010, see Fig. 18 therein). It follows from theoretical considerations (e.g. Mandl 1988) that S_R and S_L sets were formed during the initial stage of the diagonal system development as “potential shear surfaces” in a triaxial, compressive stress field ($\sigma_1 > \sigma_2 > \sigma_3$) in the form of initial microcracks. The “shear” nature of the initiation of diagonal joints manifests itself among others by smooth joint surfaces. Moreover, the geometry of joint-related arrays of en echelon fractures points to a tendency to strike-slip movement along these joints. In the discussed area, the process of forming of the oldest sets, i.e. S_R and S_L started when horizontal flysch strata became sufficiently lithified to enable the accumulation of stresses arising from NNE to SSW regional compression caused by the convergence of the European plate with the ALCAPA (Ludwiniak 2010 after;

Oszczypko and Ślącza 1989; Csontos et al. 1992; Plašienka et al. 1997; Fodor et al. 1999; Zoetemeijer et al. 1999) and lasted to the Late Oligocene (Golonka et al. 2000). Therefore, the σ_1 and σ_3 axes were oriented horizontally and the σ_2 axis vertically. The regionally dominating direction of the σ_1 axis was in the 11–15° class, while the σ_3 axis in class 101–105° (Ludwiniak 2010). It should be mentioned that there is only limited field evidence to suggest that these joints started to develop within poorly lithified rocks (e.g. Mastella 1988; Mastella et al. 1997). The opening joints of the S_R and S_L sets took place later in the Late Oligocene/Early Miocene (Birkenmajer 1986), in the extensional mode, when residual stresses acted. The other sets of joint were formed as a result of the WNW–ESE extension connected with the uplift of the synclinorium and subsequent in consequence of stress relaxation in the rock masses during postorogenic uplift (Ludwiniak 2008).

Materials and methods

Eight rock-oriented monoliths were collected (using sledge hammer and crowbar) from beds of sandstone 10 cm thick cropping out in the Biały Stream near the town of Zakopane on the southern limb of the Podhale Synclinorium (Figs. 1, 2a, 4a). In lithostratigraphic terms, these formations classify as the lower Zakopane beds. These consist of continuous packets of dark clay or calcareous shale and dark grey mudstones separated by thin beds of sandstones with calcareous

cements; there are also occasional sandstone beds thicker than 10 cm (Gołab 1959; Ludwiniak 2006; Watycha 1959, 1968). Detailed laboratory tests were performed on fine- and very fine-grained grey sandstones with abundant carbonate cement. Weakly sorted, poorly and averagely rounded grains of monocristalline quartz are the dominant component of these detrital sandstones. There are also minor quantities of polycristalline quartz, and fragments of quartz and carbonate rocks with occasional grains of partially altered plagioclases and muscovite laminae. The rock texture is random, solid and non-porous. The intergranular spaces are tightly filled by a polycristalline calcite cement with local of clusters of crystalline pyrite cubes 100 μm across. According to the Pettijohn's classification (Pettijohn et al. 1972), the Zakopane sandstone should be considered as sub-lithic or sub-arkosic arenite. Ultrasonic tests in the Laboratory of the Department of Geomechanics at the Faculty of Geology of Warsaw University were preceded by field measurements of joint orientations, style and their crosscutting relationships in the same beds of sandstone (Fig. 2a). The measurements are estimated to have been made by Meridian compass to an accuracy of $\pm 2^\circ$. The measurements covered about 100 surfaces of joints ($\sim 8 \text{ m}^2$) that were subsequently analysed in structural terms following the general rules of statistical studies (Mastella 1988; Rubinkiewicz 1998). As suggested by some authors, e.g. Dunne and Hancocok (1994), Twiss and Moores (2001) and Ludwiniak (2006), the division of joints into the sets was made directly in the field by observing the surface traces

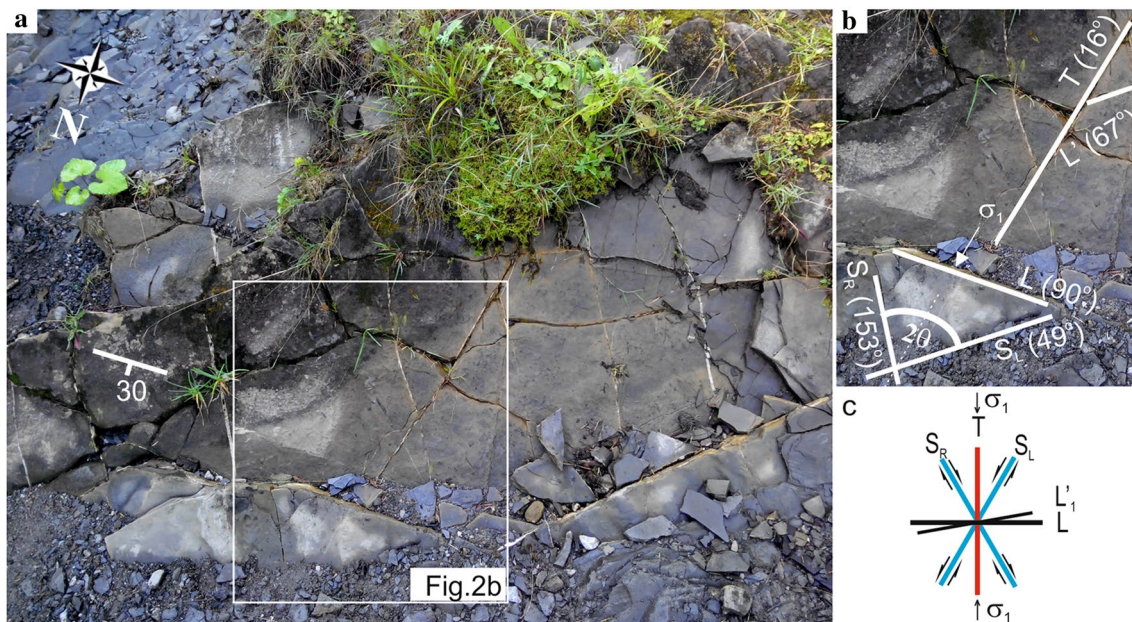


Fig. 2 **a** Joints in a Zakopane sandstone bed in the Biały Stream; **b** determination of the direction of the maximum stress axis (σ_1); **c** scheme of the joint pattern in a sandstone bed

of each set. Five sets of joints were recognised in the sandstone outcrops analysed. Specific sets were identified by their current orientation with respect to the regional extent of the Podhale Synclinorium (see Chap. 2). Of the five sets of joints, two sets are oblique to the axis of fold in which they are located and considered conjugate (S_R and S_L). Taking into account their arranged with respect to sedimentary layering and fold hinge lines, some researchers (e.g. Price 1967; Hancock 1985) named that system as conjugate *hk0* fractures enclosing an acute angle about the line parallel to sedimentary layering. There are also transverse (*T*) and longitudinal (*L*) sets named by the same authors as *ac joints* and *bc joints*, (respectively) as well as sub-longitudinal (L_1') sets (Figs. 2b, 3c, 7a). In addition to joint orientation, the strike and dip of the beds in monoliths containing the joints were also measured with respect to north (Fig. 2a).

It was assumed that the most joint sets S_R and S_L had an initial pre-folding origin (Price 1959, 1966; Książkiewicz 1968; Jaroszewski 1972). In consequence, following Murray (1967) and Al Kadhi and Hancock (1980), the strata together with joints were back-tilted to the horizontal (Rubinkiewicz 1998; Mastella and Zuchiewicz 2000; Mastella and Konon 2002; Ludwiniak 2006). The statistics of the joint measurements were analysed using Tectonics FP specialist software for Structural Geology written by Franz Reiter and Peter Acs (Fig. 3). The mode orientations of individual joint sets were determined using

contoured stereonet. It was deduced that the S_R set strikes at 138–159° (with dominant 153°) and the S_L set at 46–58° (with dominant 48°). The dihedral acute angle between S_R and S_L sets is 75° (Fig. 3c, d). Following Bucher (1920, 1921) and Ramsay and Huber (1984), the dihedral acute angle between S_R and S_L sets represents the double value of the shear angle (2θ). The bisector of this angle marks the position of the maximum compression axis σ_1 . Hence, the orientation of the axis of maximum compressive stress for diagonal system S_R and S_L ($\sigma_{1(S_R, S_L)}$) at the stage of forming joints was deduced as 11°. The other sets of joints strike at 6–24° (with dominant 13°) for *T* set, at 82–105° (with dominant 88°) for *L* set and at 62–78° (with dominant 70°) for L_1' set (Fig. 3c, d).

Taking into account fracturing at an initial pre-folding phase, the genesis of the most sets of joints are interpreted following Price (1959, 1966), Książkiewicz (1968) and Jaroszewski (1972). This implies that the directions of principle normal and shear stresses “memorised” by rock mass (Boretti-Onyszkiewicz 1968a) manifest themselves in the form of structural weaknesses in core samples drilled out of the rock monoliths perpendicular to the bedding (as shown in Fig. 4b). This direction of drilling was also chosen in order to exclude other factors like directional placement of grains, high porosity or lamination that could cause anisotropy of elastic properties of the sandstones. To determine whether the grains were

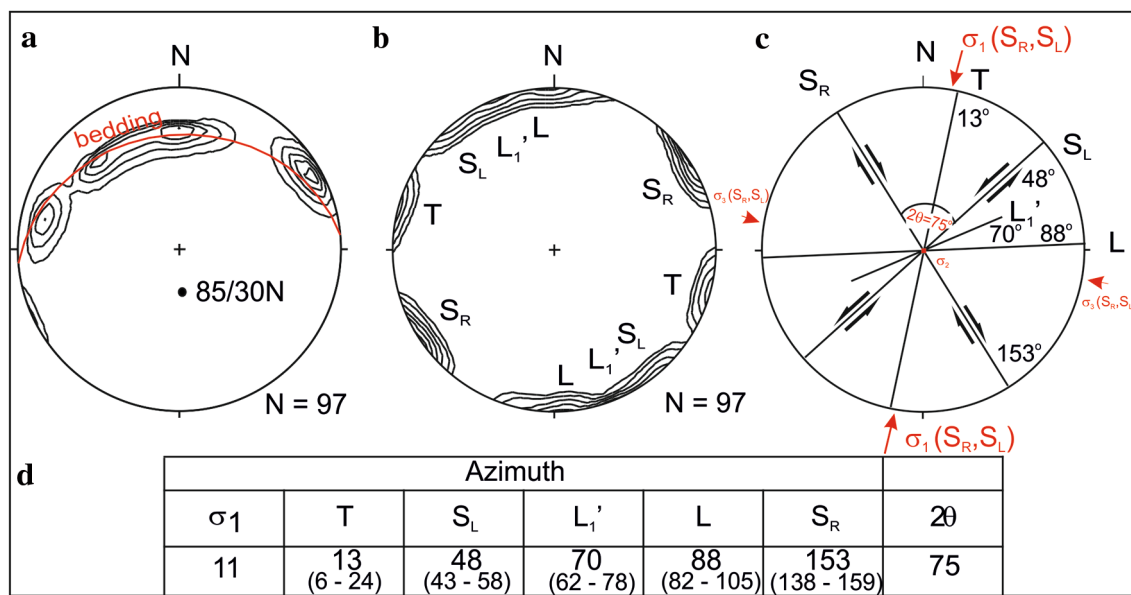


Fig. 3 Technique of determining the dominating directions and parameters of the joint network based on measurements in a Zakopane sandstone bed in the Biały Stream (*N*—number of measurements). **a** Diagrams with contours of joint planes before back tilting of beds to horizontal (recent position of joints); dot—pole to bedding plane; **b** the same diagram after bedding correction; **c** directions of

joint sets inferred from dominants of **b** (values of azimuths of the dominating directions of sets are given; the arrows indicate offset along the diagonal system; shear system: S_R —dextral, S_L —sinistral; *T*—transversal; *L* and L_1' —longitudinal sets; 2θ —double value of shear angle; $\sigma_{1(S_R, S_L)}$ —maximum compressive stress axis for diagonal system S_R and S_L); **d** selected parameters of joint network



Fig. 4 Methodology of ultrasonic tests (Domonik 2007, modified): **a** rock monoliths from which the samples were cut to the laboratory tests; **b** orientation of cylindrical sample within rock monolith; **c**

spatial orientation of measuring planes along with the directions of measurement of ultrasonic waves

placed directionally or if there were any structural defects, microscopic images were also taken (both perpendicularly as well as parallel to the sample axis), but they are not presented in this paper. In total, 69 cylindrical-oriented samples were prepared, each 5 cm in height and 5 cm in width. On each sample, 18 plane directions were marked every 10° starting from the north (0°, 10°, 20°, ..., 170°). The planes were then oriented according to markings (Fig. 4c). The material prepared and described this way was used to reconstruct paleo-stresses at the initial stage when the joints formed.

The heterogeneity of the internal structure and the variability of elastic properties of each of the 69 samples were assessed using ultrasound measurements. The research was conducted using the transition measurement method by means of a UMT-12 flaw detector made by Unipan with ULTRAMET-type digital processor fitted with heads with a frequency of 1 MHz. This method is based on the direct measurement of the sound pulse transition time between the transmitting and receiving heads along a length equal with, e.g. the sample diameter. This approach achieves a resultant of the wave front velocity (Dziedzic 2005). To get reliable results and undisturbed any errors, the measurements were made along diameter of 18 marked plane directions with accuracy at 10° to each other (180° in total) across each of 69 cylindrical samples and along the sample height. The measurement consisted of applying the transmitting and receiving heads and recording the time of wave transition through sample. In the following step, the sample was rotated round a vertical axis by 10°. This

procedure was repeated 18 times. The last one measurement consisted of applying the heads across the sample at its vertical axis. Altogether 19 measurements were made per sample.

Using the ultrasonic tests, the variability of the internal composition of rock material can be determined. It is due to the fact that pores, laminae, microfractures, directional placement of mineral grains and other heterogeneities of the internal composition are reflected by the variability of the ultrasonic wave propagation. The propagation of artificially generated ultrasonic elastic waves through the rock samples allows, not only the detection of defects and their spatial distribution in the sample, but also the characterisation of the spatial variations in dynamic elastic properties they impose. Each microfracture that was perpendicular or inclined at a high angle to the beam suppresses or entirely mutes the wave pulse that would normally be present in an area without defects (Domonik 2007).

The diagnosis of the anisotropy is most commonly based on the determination of the velocity of propagation of longitudinal (V_p) and shear waves (V_s), which in turn make it possible to calculate the dynamic modulus of elasticity (E_d) and dynamic Poisson's ratio (ν_d)—constants characterising the elastic properties of solid bodies (Burger 1992). Therefore, E_d was calculated using Eq. (1).

$$E_d = \rho \times V_s^2 \frac{(3V_p^2 - 4V_s^2)}{(V_p^2 - V_s^2)}, \quad (1)$$

while v_d was calculated using Eq. (1)

$$v_d = \frac{V_p^2 - 2V_s^2}{2(V_p^2 - V_s^2)}, \tag{2}$$

where ρ is the bulk density of a rock [kg/m³], and V_p and V_s are velocities of longitudinal and shear wave, respectively [m/s].

Results

The measured velocity of the ultrasonic waves depended on the direction of measurement as illustrated in Fig. 5. The maximum values of the longitudinal wave measured across the sample diameter (V_{p_D}) and the minimum measurements of the shear wave (V_{s_D}) were observed and listed in the following geographic directions measured from north: 10°, 50°, 70°, 90°, 110°–120° and 140°–150°. Except for 110°–120°, these directions correspond to the ranges of values assumed for joint sets measured in the field: T , S_L , L'_1 , L and S_R , respectively (Fig. 3c). The longitudinal waves that travelled parallel with the macroscopic joint

surfaces were much less attenuated (and hence had higher wave velocities Fig. 5a), and the shear wave velocities were attenuated much more (and hence have smaller wave velocities Fig. 5b).

The dynamic Poisson’s ratios calculated from these velocities are like those observed for V_p . The dispersions of the v_d values are significant for all adopted measurement directions; the highest values are measured parallel to the joint sets measured in the field (Fig. 6a). Directional variations in the velocity of longitudinal waves (V_p) and shear waves (V_s) along with bulk density (ρ) calculated for each sample result in corresponding variations in the distributions of the dynamic modulus of elasticity (E_d). Therefore, the elastic properties have a similar anisotropy to the individual directions of measured values of V_p (Fig. 6b). The highest E_d values were obtained in the directions that are within the range of the orientations interpreted for joint sets T , S_L , L'_1 , L and S_R .

The elastic properties were also assessed using static strength tests. The elastic properties were calculated along the sample length and compared with the dynamic values computed in the same direction. Each of the static

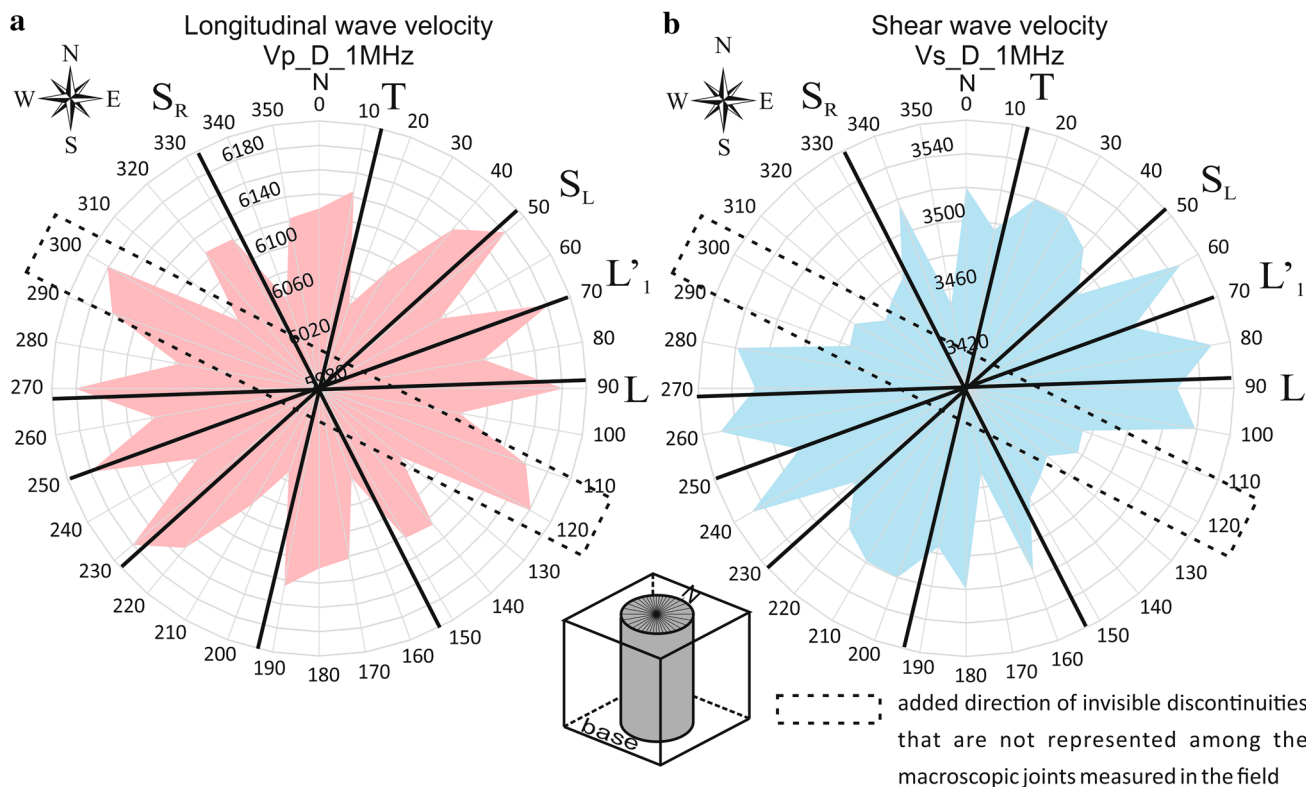


Fig. 5 Diagrams of distribution of ultrasonic wave velocity in oriented Zakopane sandstone depending on measuring directions against joint set dominants determined in the field drawn for arithmetic mean values of 69 samples: **a** longitudinal wave velocity; **b** shear wave velocity

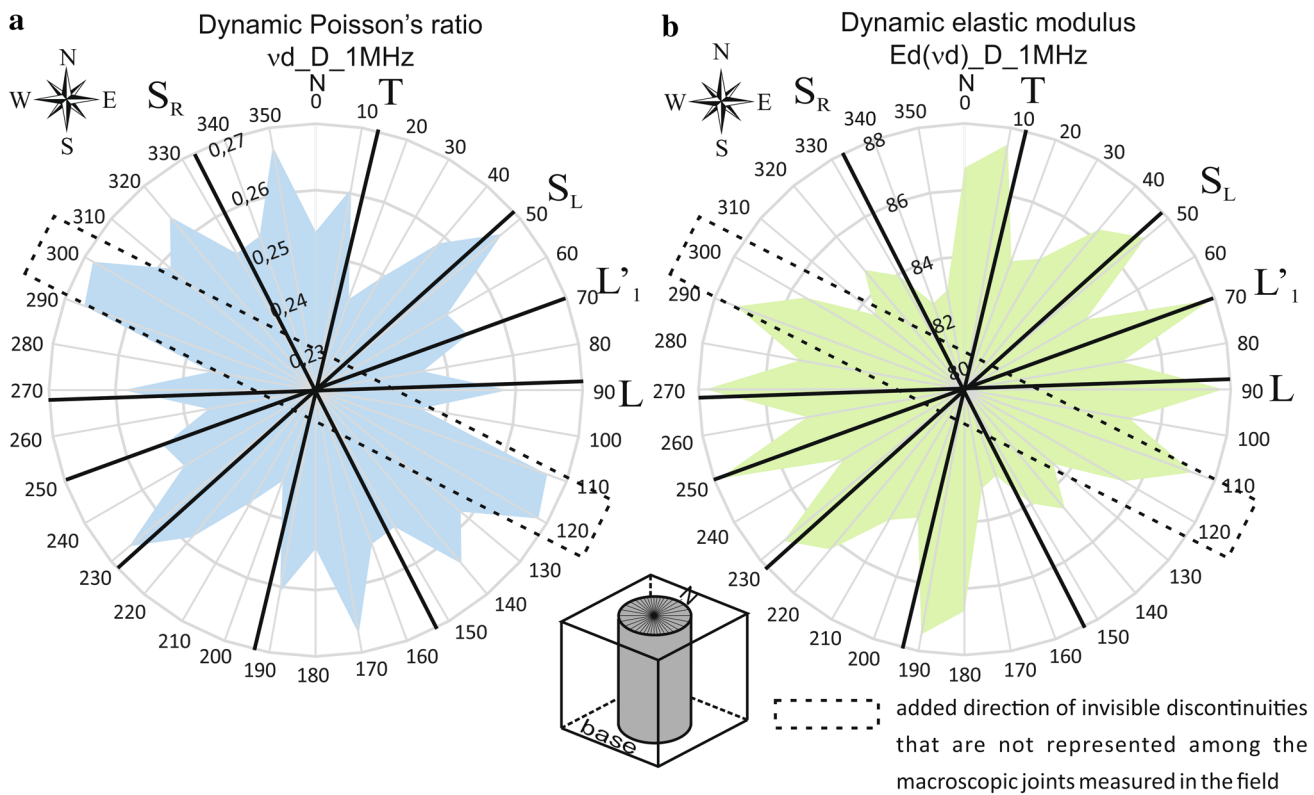


Fig. 6 Diagrams of distribution of dynamic elastic properties in oriented Zakopane sandstone depending on measuring directions against joint set dominants determined in the field drawn for arithmetic mean

values of 69 samples: **a** dynamic Poisson’s ratio; **b** dynamic elastic modulus (dynamic Young’s modulus)

Table 1 Results of elastic properties from uniaxial compression and ultrasonic tests on Zakopane sandstone

Values	E_d [GPa]	ν_d [-]	E_{st} [GPa]	ν_{st} [-]
Minimum	71.2	0.16	61.6	0.12
Average	75.1	0.20	70.9	0.23
Maximum	78.8	0.23	75.7	0.29

E_d dynamic modulus, ν_d dynamic Poisson’s ratio, E_{st} static modulus, ν_{st} static Poisson’s ratio

measurements is close to the equivalent dynamic measurements (Table 1).

Conclusions

In previous works, e.g. (Boretti-Onyszkiewicz 1968b; Halicki 1963; Książkiewicz 1968), mainly statistical methods were applied during the analysis of the joint direction. The issue of subdivision of the joint network into sets through observation of the morphology of joint traces as well as crosscutting relationships was not considered. It resulted in including joints having similar directions but different

morphological features and different origins (e.g. S_L and L'_1 or S_R and T) into one set, which in turn effects in a too wide range of directions of particular sets. Ludwiniak (2006, 2010) reviewed some of the opinions included in the aforementioned works, which was a great progress. It was possible due to his own more thorough measurements in individual outcrops. Among other things, Ludwiniak noticed, for example, that none of the above-mentioned authors distinguished the set T , despite the fact that there were many outcrops in situ, where this set occurred (although in less quantity than sets S_R and S_L). Moreover, insightful observations of the joint networks in the field, as suggested by Dunne and Hancocok (1994) as well as Twiss and Moores (2001), allowed the researcher to determine the origin of the joint network (five sets) in the Western Podhale region and reconstruct the paleo-stresses responsible for its development. On the other hand, Domonik (2003, 2005) determined only four sets of joints in the field (S_R , S_L , T as well as L), while not at all determining the L' set. The L' set was probably included in the adjacent S_L set. The joint sets determined this way could influence the assessment of the results of the strength as well as the ultrasonic tests. Domonik has in fact determined the acoustic and mechanical anisotropy, however, only for the above-mentioned four sets. Perhaps the

subtle variations of wave velocity were omitted, which could suggest the existence of additional planes of microfractures.

The directional variability of elastic properties in the sandstone specimens analysed demonstrates a strong anisotropy due primarily to the effects of the stress presumed to have been active during the folding in the Late Oligocene/Early Miocene (Birkenmajer 1986) and the uplift of the Carpathian Mountains which started in the Middle Eocene (Środoń et al. 2006). This relationship is reinforced by the distribution of orientations of the macroscopic joint sets measured in the field being so like the orientations of microfractures in samples of rock that look isotropic to the eye. Keep in mind that the ultrasonic tests were carried out along 18 diametric paths only 10° apart but the field measurements were estimated to an accuracy of $\pm 2^\circ$. This means that the value of dihedral angle may turn out to be slightly higher than in the field measurements. The velocities of the ultrasonic waves varied only with their direction of measurement. All variations in velocity (of the order of several tens of m/s) were taken as directly due to the internal structure of the tested sample. They were not due to changing measurement conditions, nor erroneous or accidental measurements. Similar relationships were observed in research on the Krosno sandstones from Mucharz (Dziedzic 2005). Therefore, it seems that measurements of the ultrasonic wave velocities through rock need to be only presented to an accuracy of the order of several tens of m/s at the maximum (100 m/s), as is usual in the literature.

In addition, structural discontinuities detected by ultrasonic measurements should be regarded as an incipient phase of a joint *sensu stricto* observed in situ. The same hidden joint anisotropy affects the entire flysch rock mass (Boretti-Onyszkiewicz 1968a). Domains in which elastic energy has accumulated will become increasingly obvious as they degrade during further relaxation of the historical stresses preserved in the rock mass.

The distribution of dynamic elastic constants revealed by the ultrasonic wave velocity measurements added the 110° – 120° direction of invisible discontinuities that are not represented among the macroscopic joints measured in the field. It is possible that the additional set of microfractures is a joint set conjugate with a low dihedral angle and with a bisector approximately parallel to the axis of the syncline and was produced within longitudinal joints (L) (Aleksandrowski 1989 after; Książkiewicz 1968). According to De Sitter (1964), such a system can develop where a syncline is horizontally shortened with the σ_1 axis parallel to the syncline axis and σ_3 perpendicular to it (Fig. 7). Therefore, the “hidden” direction of microfractures disclosed by ultrasonic measurements, and “memorised” by the rock mass, could represent the complementary sub-longitudinal set (L_2') and together with L_1' set produce a conjugate system named as

conjugate $hk0$ fractures enclosing an acute angle about the line parallel to the fold axis (Price 1967; Hancock 1985). This system was produced at a different stress field than S_R and S_L conjugate joints.

The absence of macroscopic L_2' joints in the field may be because both sets of conjugate joints do not always develop with equal intensity and it is not uncommon for one conjugate set of fractures to develop better than the other. Szichin (1960) suggested that a slightly earlier shear plane may have “delayed”, hindered or even prevented the formation of the other. Conjugate shears can also result from the influence of a strong anisotropy in the failing medium (Jaroszewski 1974). The influence of a planar anisotropy (foliation) on the shear surfaces formed in static strength tests have been reported by, among others, Jaeger (1960), Donath (1961), Paterson (1958, 1978). These authors demonstrated that, if the mechanical anisotropy in the sample is strong, one of the two potential sets of shear surface develops along the weakest plane; meanwhile, the complementary shear plane either does not develop at all, or only develops poorly at an increased but still acute angle to its conjugate partner. It, therefore, seems reasonable to expect that the 110° – 120° discontinuities “memorised” by the rock mass will eventually activate with further relaxation of the rock mass caused by other factors as weathering, mining, earthquakes or faulting.

It is also worth noting that as found by Boretti-Onyszkiewicz (1968a), strength tests conducted on the same apparently isotropic samples demonstrated the orientation of a hidden mechanical anisotropy and oriented similarly as the regional set of joints which she measured in the field. However, the direction range of the measurements conducted in the field was too wide so the directions obtained in the strength tests were, therefore, grouped into wrong sections.

The author of this work attempted to combine the current knowledge about the evolution of joint networks in the Polish Carpathian Mountains and the rules of field data gathering with the possibility of applying and developing geo-mechanical tests for joint anisotropy. This approach allowed confrontation of the field tests results with the results of the tests conducted in the laboratory, which in turn enabled discovery of new directions of potential internal weaknesses that are not represented among the macroscopic joints measured in the field.

The results of the research reported here indicate that ultrasonic measurements can accurately determine the internal mechanical heterogeneities in the elasticity of the rock mass and constrain its in situ stress field. This knowledge can be used, e.g. for the safe design of a tunnel lining and its interaction with the rock mass (Furtak 2004) as well as design stable slopes and excavations in flysch formations. However, it should be borne in mind that ultrasonic methods alone are not sufficient to determine the

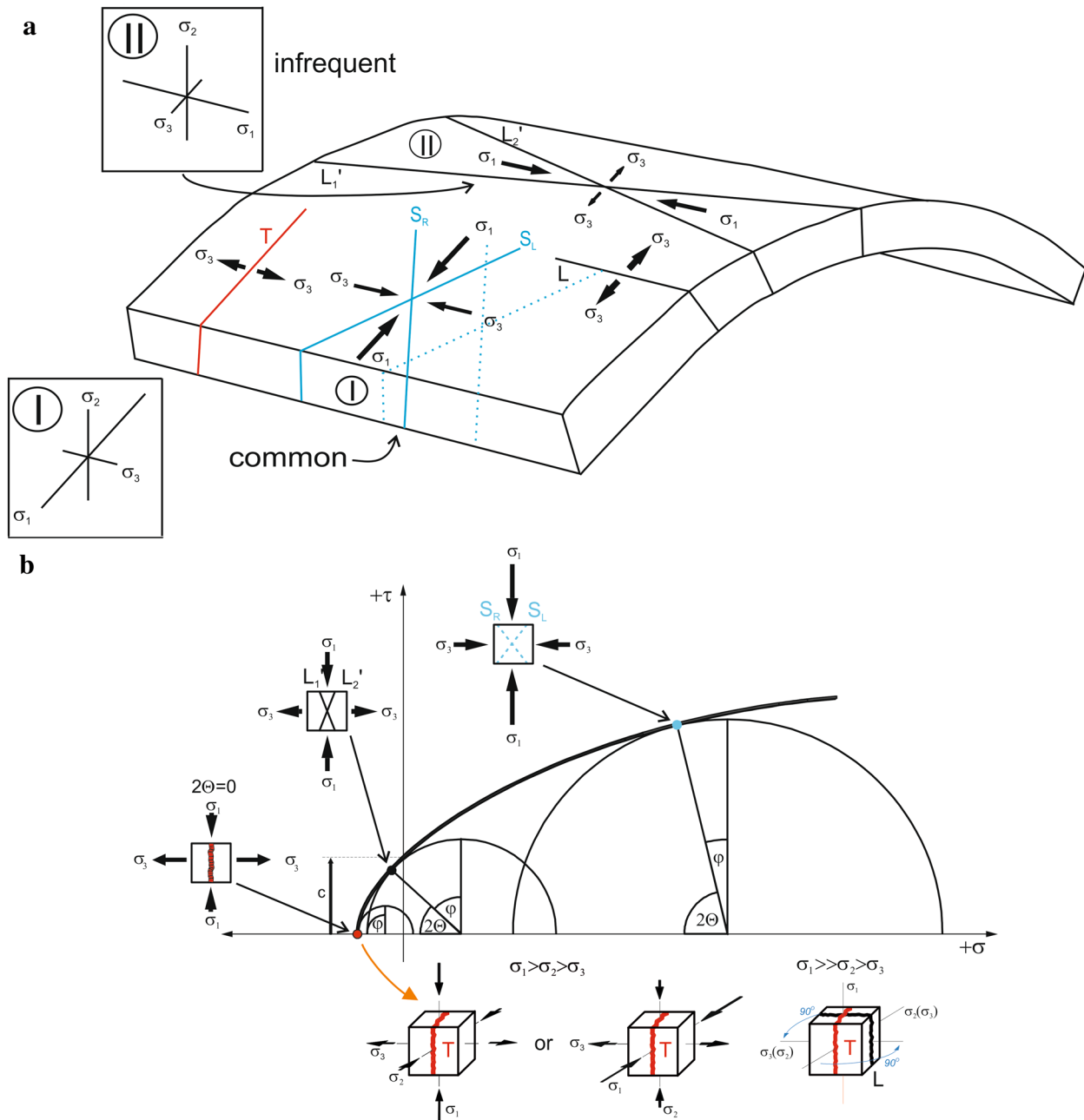


Fig. 7 **a** Typical relationship to a fold and orientation of extensional (dilatational) and shear joints in a thin, bedded layer, with associated stress systems (Price and Cosgrove 1990, modified); **b** theoretical Mohr's diagram showing stress condition for development of the joint network according to ultrasonic test (Ludwiniak 2010 after; Price and

Cosgrove 1990; Dadlez and Jaroszewski 1994, modified). ϕ —angle of internal friction, c —cohesion, τ —shear stress, 2θ —double value of shear angle, opened joints are indicated as solid lines and initial microcracks as dashed ones

geo-mechanical parameters of any rock mass intended for sophisticated engineering.

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