

Erratum: All orders results for self-crossing Wilson loops mimicking double parton scattering

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1. Equations (D.14)–(D.17) were computed from an incorrect eq. (D.13), the correct equation is

$$\rho \equiv \frac{\mathcal{A}_6^{\text{NMHV}}}{\mathcal{A}_6^{\text{BDS-like}}} = \frac{1}{2(1+w^*)} \left[E(u, v, w) + \tilde{E}(u, v, w) + E(w, u, v) - \tilde{E}(w, u, v) \right] + \frac{w^*}{2(1+w^*)} \left[E(v, w, u) + \tilde{E}(v, w, u) + E(w, u, v) - \tilde{E}(w, u, v) \right]. \quad (\text{D.13})$$

In the original version a complex conjugation and factor of 1/2 were missing. Equations (D.14)–(D.17) below are the corrected versions, based on the corrected (D.13) above. Also, in the original text, equations (D.14)–(D.17) were intended to be for $2 \rightarrow 4$ kinematics with $v \rightarrow 0^+$. However, the $v \rightarrow 0^-$ limit of $3 \rightarrow 3$ kinematics is simpler, having no double discontinuity. The corrected equations (D.14)–(D.17) below are analytically continued to $3 \rightarrow 3$ kinematics by the method discussed in section 3.1 of the main text, and then the limit $v \rightarrow 0^-$ is taken:

$$\rho^{(1)} = -\frac{1}{2} \ln^2 |v| + 2\zeta_2 + \pi i \left[\frac{1+w}{1+w^*} + 1 \right], \quad (\text{D.14})$$

$$\rho^{(2)} = \frac{1}{8} \ln^4 |v| - \frac{1}{2} \zeta_2 \ln^2 |v| + \pi i \left[\frac{1+w}{1+w^*} \left(-\frac{1}{2} \ln^2 |\delta| + \ln |\delta| + \zeta_2 - 1 \right) - \frac{1}{2} \ln^2 |v| - \ln |v| - \zeta_3 + \zeta_2 - 1 \right], \quad (\text{D.15})$$

$$\begin{aligned}
\rho^{(3)} = & -\frac{1}{48} \ln^6 |v| - \frac{1}{4} \zeta_4 \ln^2 |v| + \frac{91}{12} \zeta_6 \\
& + \pi i \left[\frac{1+w}{1+w^*} \left(\frac{1}{8} \ln^4 |\delta| - \frac{1}{2} \ln^3 |\delta| + \frac{3}{2} \ln^2 |\delta| - (\zeta_3 + 3) \ln |\delta| + \frac{1}{2} \zeta_4 + \zeta_3 + 3 \right) \right. \\
& \quad + \frac{1}{8} \ln^4 |v| + \frac{1}{2} \ln^3 |v| - \frac{1}{2} (\zeta_3 - 3) \ln^2 |v| + (\zeta_3 + 3) \ln |v| \\
& \quad \left. + 7\zeta_5 - 3\zeta_2\zeta_3 + \frac{1}{2} \zeta_4 + \zeta_3 + 3 \right], \tag{D.16}
\end{aligned}$$

$$\begin{aligned}
\rho^{(4)} = & \frac{1}{384} \ln^8 |v| + \frac{1}{48} \zeta_2 \ln^6 |v| + \frac{7}{16} \zeta_4 \ln^4 |v| + \left(\frac{13}{48} \zeta_6 + \frac{1}{2} (\zeta_3)^2 \right) \ln^2 |v| - \frac{1325}{36} \zeta_8 - 2\zeta_2 (\zeta_3)^2 \\
& + \pi i \left[\frac{1+w}{1+w^*} \left(-\frac{1}{48} \ln^6 |\delta| + \frac{1}{8} \ln^5 |\delta| - \frac{1}{8} (\zeta_2 + 5) \ln^4 |\delta| + \left(-\frac{1}{6} \zeta_3 + \frac{1}{2} \zeta_2 + \frac{5}{2} \right) \ln^3 |\delta| \right. \right. \\
& \quad - \left(\frac{7}{4} \zeta_4 - \frac{1}{2} \zeta_3 + \frac{3}{2} \zeta_2 + \frac{15}{2} \right) \ln^2 |\delta| + \left(4\zeta_5 - 3\zeta_2\zeta_3 + \frac{7}{2} \zeta_4 - \zeta_3 + 3\zeta_2 + 15 \right) \ln |\delta| \\
& \quad - \left. \frac{13}{24} \zeta_6 - 2(\zeta_3)^2 - 4\zeta_5 + 3\zeta_2\zeta_3 - \frac{7}{2} \zeta_4 + \zeta_3 - 3\zeta_2 - 15 \right) \\
& \quad - \frac{1}{48} \ln^6 |v| - \frac{1}{8} \ln^5 |v| + \left(\frac{3}{8} \zeta_3 - \frac{1}{8} \zeta_2 - \frac{5}{8} \right) \ln^4 |v| + \left(\frac{1}{12} \zeta_3 - \frac{1}{2} \zeta_2 - \frac{5}{2} \right) \ln^3 |v| \\
& \quad + \left(\frac{25}{8} \zeta_5 + 2\zeta_2\zeta_3 - \frac{7}{4} \zeta_4 + \frac{1}{4} \zeta_3 - \frac{3}{2} \zeta_2 - \frac{15}{2} \right) \ln^2 |v| \\
& \quad + \left(-\frac{3}{2} (\zeta_3)^2 - 5\zeta_5 + \zeta_2\zeta_3 - \frac{7}{2} \zeta_4 + \frac{1}{2} \zeta_3 - 3\zeta_2 - 15 \right) \ln |v| \\
& \quad - \frac{1381}{32} \zeta_7 + \frac{43}{2} \zeta_2\zeta_5 + 4\zeta_3\zeta_4 - \frac{13}{24} \zeta_6 - \frac{5}{2} (\zeta_3)^2 - 5\zeta_5 + \zeta_2\zeta_3 \\
& \quad \left. - \frac{7}{2} \zeta_4 + \frac{1}{2} \zeta_3 - 3\zeta_2 - 15 \right]. \tag{D.17}
\end{aligned}$$

2. The discussion immediately following equations (D.14)–(D.17) was based on the original, incorrect version of these equations. The main point originally read:

“We see that there are indeed logarithmically singular $\ln \delta$ terms in the imaginary part and in the double discontinuity $(2\pi i)^2$ term, beginning at two loops. However, there are no $\ln \delta$ terms in the part with the $(1+w^*)/(1+w)$ prefactor; that is, the terms depending on the azimuthal component of the vector \vec{z} in eq. (2.22) are finite.”

The correct version is:

“We see that there are indeed logarithmically singular $\ln |\delta|$ terms in the imaginary part beginning at two loops. However, the $\ln |\delta|$ terms appear only in the part with the $(1+w)/(1+w^*)$ prefactor; that is, the terms that are independent of the azimuthal component of the vector \vec{z} in eq. (2.22) are finite.”

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