

0. NOTATION AND CONVENTION

0.1. A topological space is called nice if it is Hausdorff, locally compact, paracompact and with a countable basis for its topology.

0.2. If A is a topological space and $X \subset A$, then $\text{cl}_A(X)$ (resp. $\text{int}_A(X)$) denotes the closure (resp. interior) of X in A .

0.3. If A and B are topological spaces, then $A \sqcup B$ denotes their disjoint union.

0.4. For any set A , 1_A (or id_A) denotes the identity map of A .

0.5. Smooth means always differentiable of class C^∞ .

0.6. The connected components of a smooth manifold may have different dimensions. Given a smooth manifold M we denote by TM its tangent bundle. If $x \in M$, TM_x denotes the tangent space of M at x . If N is another smooth manifold and $f : M \rightarrow N$ is smooth, $df : TM \rightarrow TN$ denotes the differential of f ; if $x \in M$, then $df_x : TM_x \rightarrow TN_{f(x)}$ denotes the restriction of df . The smooth map f is called submersive if df_x is surjective for any $x \in M$.

0.7. Let A be a topological space and let X, Y and Z be subsets of A . Let f and g be maps defined on X and Y respectively. We say that f equals g near Z (denoted $f = g$ near Z) if there exists a neighborhood U of Z such that $f|_{X \cap U} = g|_{Y \cap U}$. The same terminology is also used in other similar situations (for example $X = Y$ near Z means that there exists a neighborhood U of Z such that $X \cap U = Y \cap U$).

0.8. \mathbb{R} denotes the field of real numbers; $\mathbb{R}_+ = \{r \in \mathbb{R}; r \geq 0\}$ and $\mathbb{R}_+^* = \{r \in \mathbb{R}; r > 0\}$.